

1. given an empty heap perform the following operations.

Give the state of the heap (draw the tree) at each step.

push 1

push 5

push 3

push 4

push 2

pop

pop

pop

pop

pop

What order do the nodes come out in?

If I were to do this with  $n$  elements, what's the total running time?

2. (a) Give an algorithm to find the sum of all of the elements in a linked list.

(b) Give an algorithm to count the number of nodes in a binary tree.

(c) Give an algorithm to find the smallest number in a linked list.

(d) Give an algorithm to find the smallest number in a binary tree.

3. Use structural induction to prove that:

(a) for linked lists:  $count(a + b) = count(a) + count(b)$

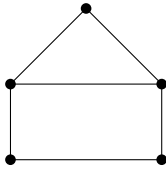
(b) for trees:  $height(mirror(t)) = height(t)$

4. Given a graph  $G$ , we can define a relation  $\rightsquigarrow$  where  $u \rightsquigarrow v$  if there's a path from  $u$  to  $v$  in  $G$ .

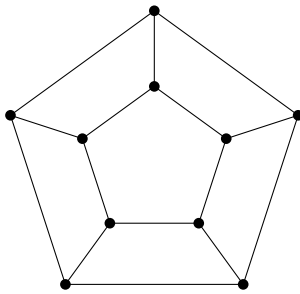
Show that  $\rightsquigarrow$  is an equivalence relation.

5. Give An adjacency list, adjacency matrix, and edge list for the following graphs.

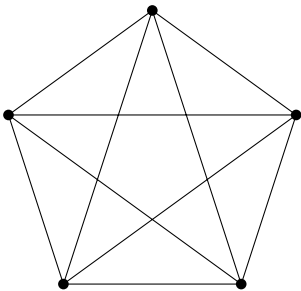
(a)



(b)



(c)



(d)

