

Calculus



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Parametric Equations and Polar Coordinates

Vectors and Vector-Valued Functions

Partial Derivatives

Multiple Integrals

Vector Calculus

Second-Order Differential Equations

Limits and Continuity



Limits

Limits of a Functions and Sequences

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Properties of Limits

- o Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magna aliqua.
- o Ut enim ad minim veniam, quis nostrud exercitation ullamco laboris nisi ut aliquip ex ea commodo consequat. Duis aute irure dolor in reprehenderit in voluptate velit esse cillum dolore eu fugiat nulla pariatur.
- o Excepteur sint occaecat cupidatat non proident, sunt in culpa qui officia deserunt mollit anim id est laborum.
- o Donec aliquam viverra (lorem a fermentum) donec dignissim augue id diam laoreet, in vulputate mi blandit. In placerat aliquam felis, at porta arcu. Integer mollis consectetur ipsum, et gravida est tincidunt vel. Sed gravida hendrerit diam, dapibus pulvinar ipsum semper.
- o Duis aute irure dolor in reprehenderit in voluptate velit esse cillum dolore eu fugiat nulla pariatur. Excepteur sint occaecat cupidatat non proident, sunt in culpa qui officia deserunt mollit anim id est laborum.

One-Sided Limit

- o black black
- o minimal minor white white white
- o red red
- o orange orange
- o yellow yellow
- o green green
- o cyan cyan
- o blue blue
- o magenta magenta
- o pink pink

Continuity

- up[↑]
- down[↓]
- limit[🔗]
- 🌐 lex [📺]
- Thomas (2.1–2.2) [📖]

Continuous Functions

-

Intermediate Value Theorem

-

Limits Involving Infinity

Limits at Infinity and Infinite Limits

-

Asymptotes of functions

-

Derivatives



Derivative Fundamentals

Derivative Notation

- ...

Differentiation Rules

Linear, Product, Chain, Inverse

-

Powers, Polynomials, Quotients, Reciprocals

-

Exponential, Logarithmic

-

Trigonometric, Hyperbolic

-

Differentials and Related Concepts

Differentials

-

Linearization

-

Implicit Differentiation

-

Related Rates

-

Applications of Derivatives



Stationary Point

Maxima and Minima

-

Extreme Value Theorem

-

Interior Extremum Theorem

-

Mean Value Theorem

Rolle's Theorem

-

Corollaries of the Mean Value Theorem

-

Monotonic Functions

Derivative Tests

First-Derivative Test

-

Second-Derivative Test

-

Concavity

-

Higher-Order Derivative Test

-

Differential Methods

Newton's Method

-

Taylor's Theorem

-

General Leibniz Rule

-

Integrals



Integral Fundamentals

Terminology and Notation

-

Primer: Formal Definitions

-

Definite Integrals

Riemann Integral

-

Integrability

-

Properties of Definite Integrals

-

The Fundamental Theorem of Calculus

Fundamental Theorem, Part 1

-

Fundamental Theorem, Part 2

-

The Integral of a Rate

-

Total Area

-

Integration By Substitution

Indefinite Integrals

-

Definite Integrals

-

Symmetric Functions

-

Area Between Curves

-

Applications of Definite Integrals



Solid of Revolution

Disc Integration

-

Shell Integration

-

Arc Length

Dealing with Discontinuities

-

Differential Arc Length

-

Surface of Revolution

Revolution about the y-Axis

○

Transcendental Functions



Inverse Functions

One-to-One Functions

-

Derivative Rule for Inverses

-

Logarithmic Functions

Natural Logarithm

-

Properties of Logarithms

-

Trigonometric Integrals

-

Logarithmic Differentiation

-

Exponential Functions

Euler's Number

-

Natural Exponential Function

-

Laws of Exponents

-

General Exponential Function

-

Exponential Change

- Separable Differential Equations

-

Examples of Exponential Change

-

Indeterminate Forms

Indeterminate Form 0/0

-

L'Hôpital's Rule

-

Infinite Indeterminate Forms

-

Indeterminate Powers

-

Inverse Trigonometric Functions

Principal Trigonometric Values

-

Inverse Trigonometric Tables

-

Hyperbolic Functions

Hyperbolic Function Tables

○

Techniques of Integration



Integration by Parts

Definite Integrals by Parts

○

Trigonometric Integral Methods

Trigonometric Products and Powers

-

Trigonometric Square Roots

-

Trigonometric Substitutions

-

Partial Fraction Decomposition

Partial Fraction Principles

-

General Statement

-

Numerical Integration

Trapezoidal Rule

-

Simpson's Rule

-

Improper Integrals

Indirect Evaluation

-

Infinite Sequences and Series



First-Order Differential Equations



- yes no

Parametric Equations and Polar Coordinates



Vectors and Vector-Valued Functions



- yes yes ye:w
 - yes yes yes
 - yes yes yes
 - yes yes yes

Partial Derivatives



Multiple Integrals



Vector Calculus



Second-Order Differential Equations

