

# Chapter 5: Linked Lists



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# Today's Outline



1. Circular Linked Lists
  - Queue Implementation
2. Doubly Linked Lists
  - Traversing
  - Insert a node
  - Delete a node
3. Circular Doubly Linked Lists

# Linked Lists



## TYPE



**Singly** Linked List

**Circular** Linked List

**Doubly** Linked List

**Circular Doubly** Linked List

## ACTION

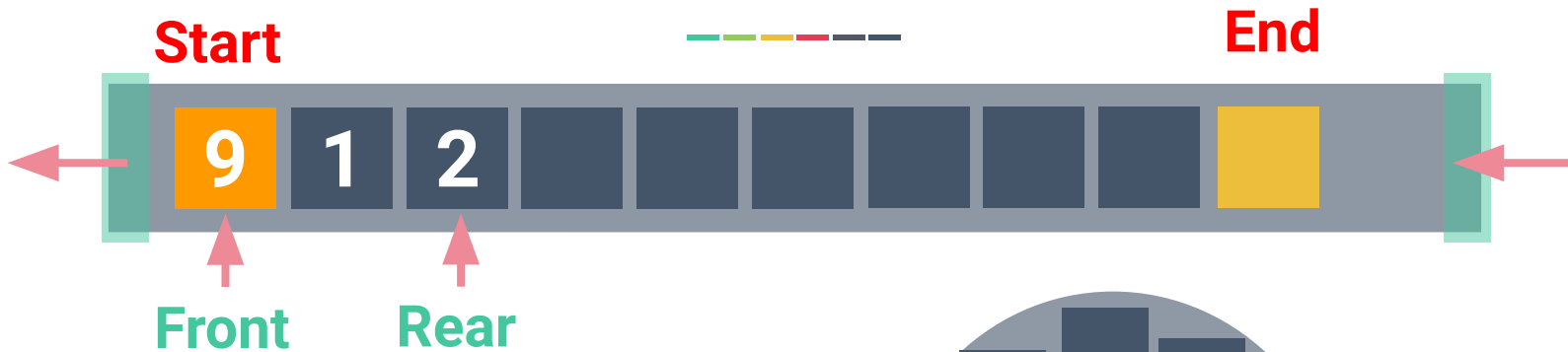


Traversing

Insert

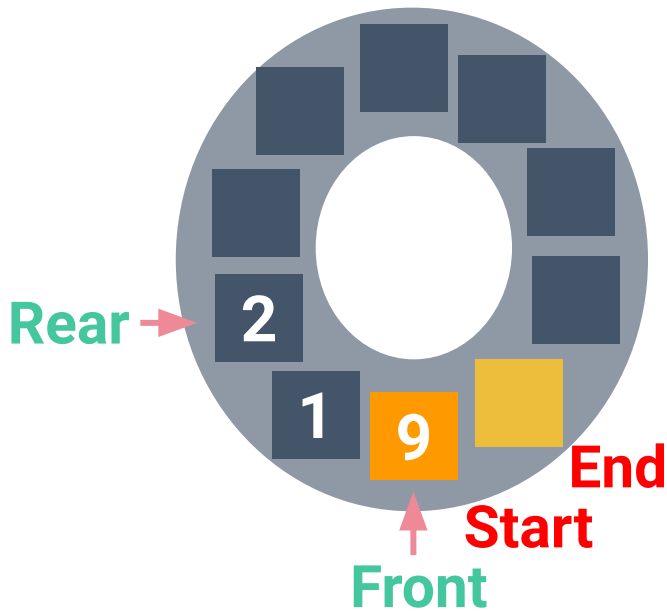
Delete

# Circular Queue

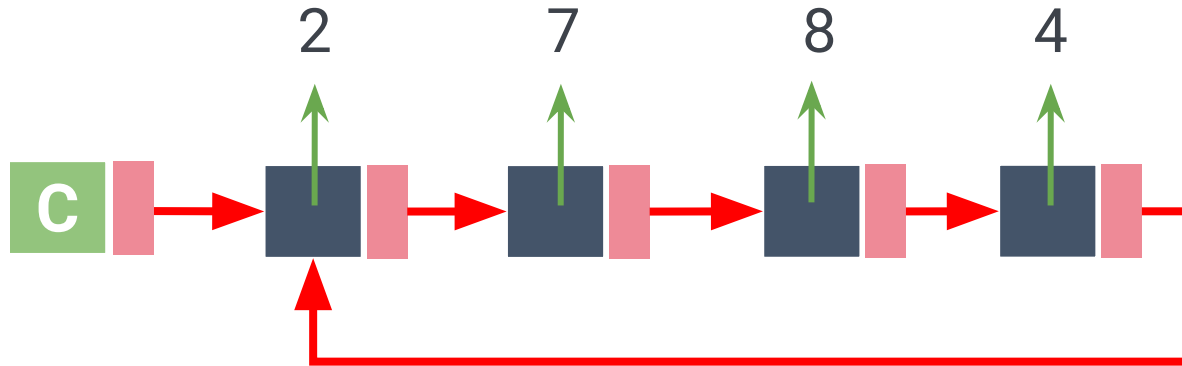


Circular is artificial for array

- Modular arithmetic (%)



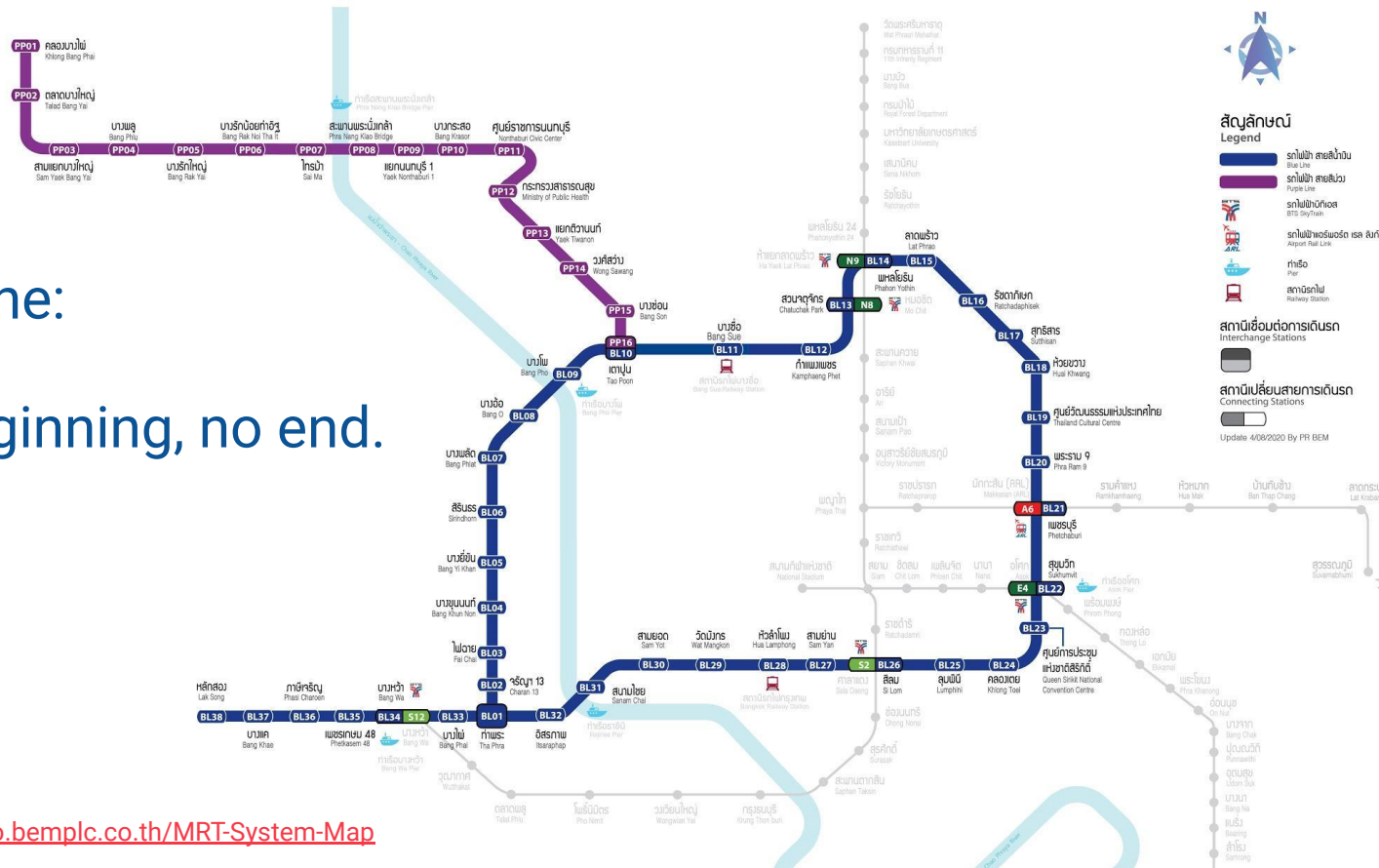
# Circular Linked Lists



# Circular Linked Lists

Blue line:

No beginning, no end.

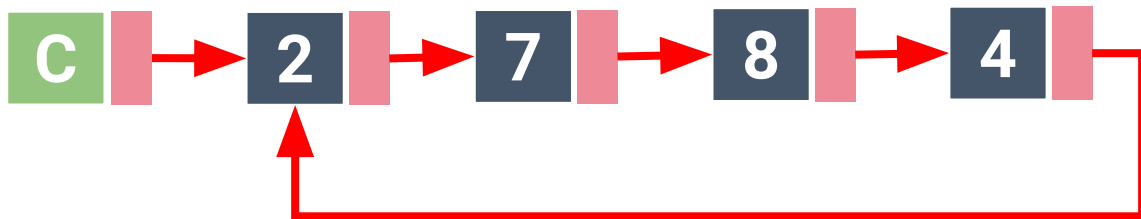


# Circular Linked Lists



Address/  
Byte#      Value

6000	4
6001	6002
6002	2
6003	6008
6004	8
6005	6012
6006	
6007	
6008	7
6009	6004
6010	
6011	
6012	4
6013	6002

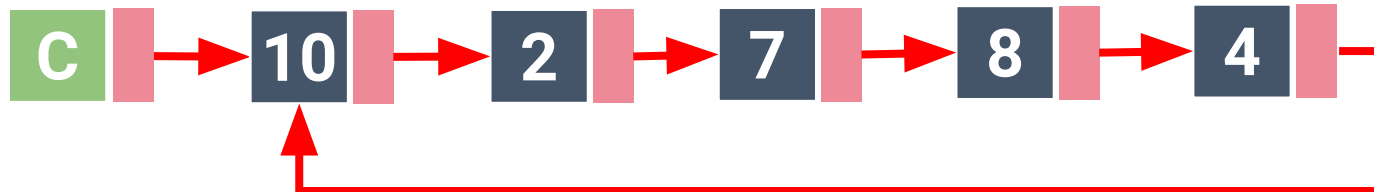
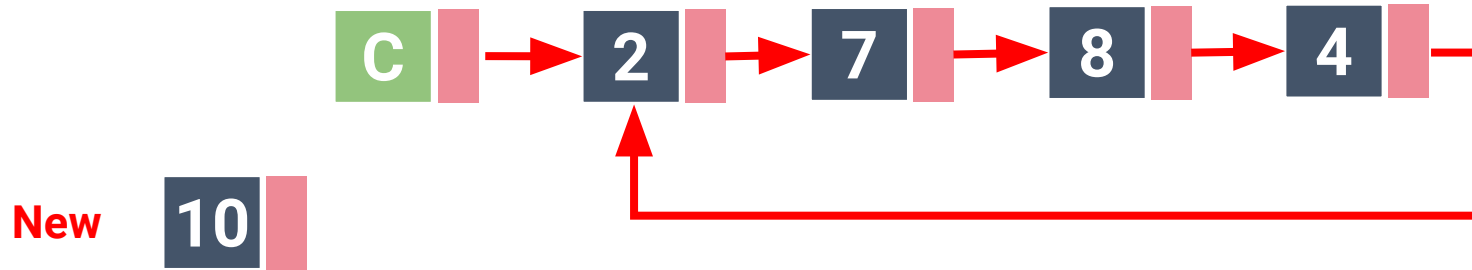


# Circular Linked Lists



**Insert**

at the head of the list





# Circular Linked Lists

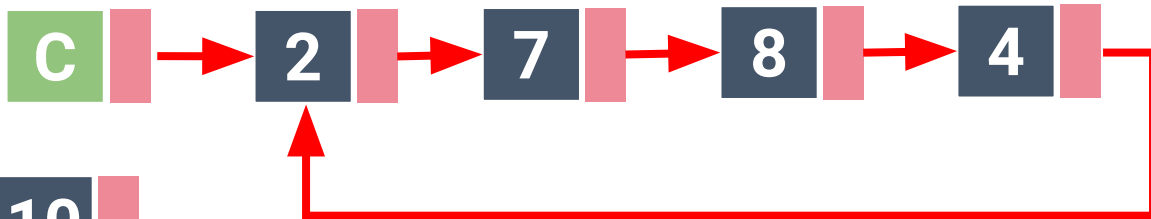


**Insert**

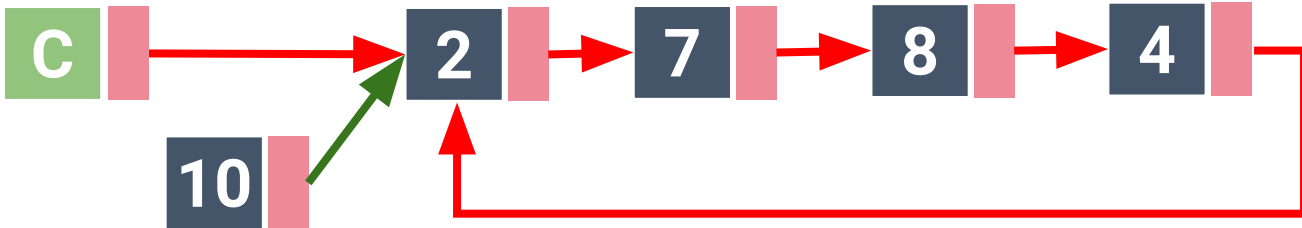
at the head of the list

Step 1

**New**



Step 2



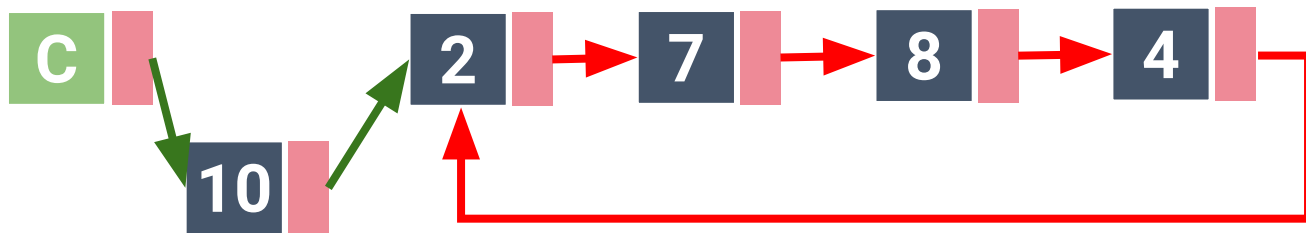
# Circular Linked Lists



**Insert**

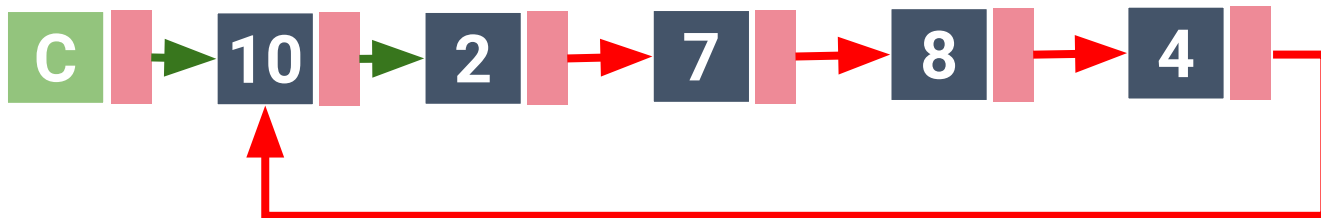
at the head of the list

Step 3



count += 1

Step 4&5

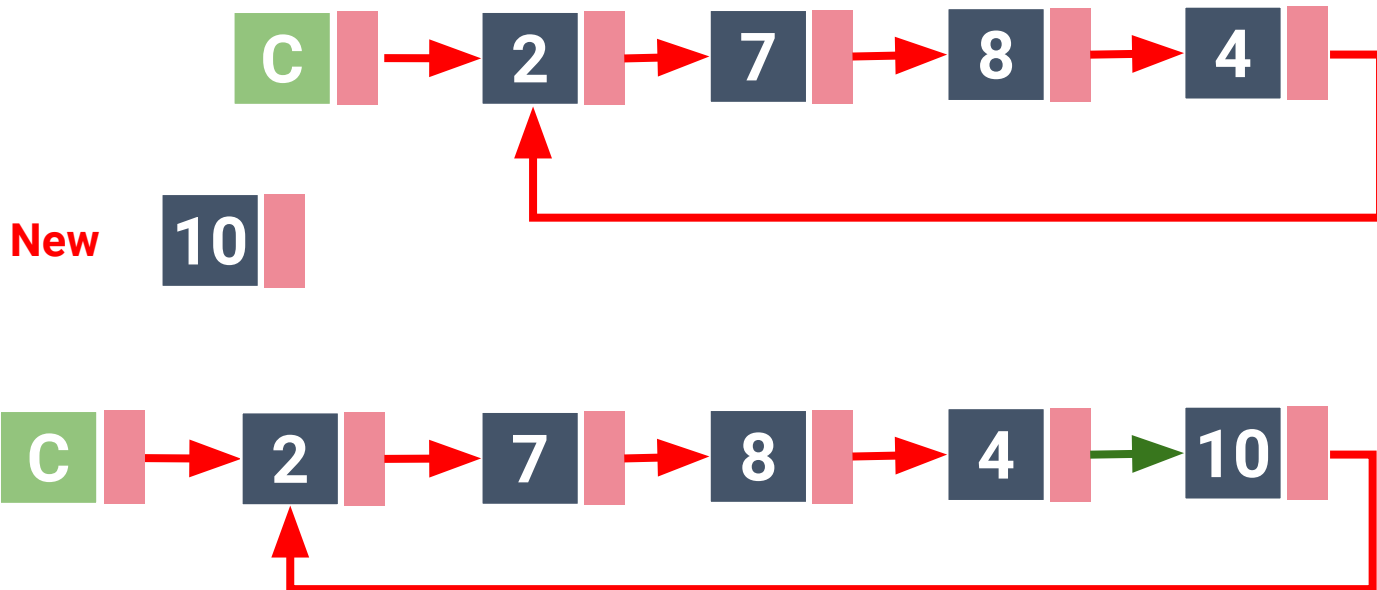


# Circular Linked Lists



Insert

at the tail of the list



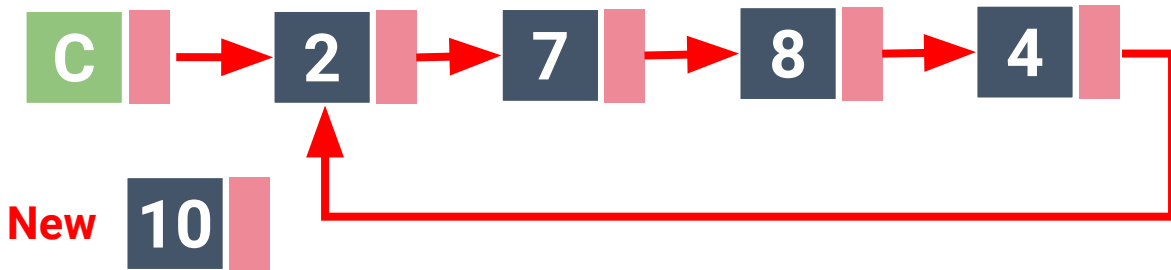
# Circular Linked Lists



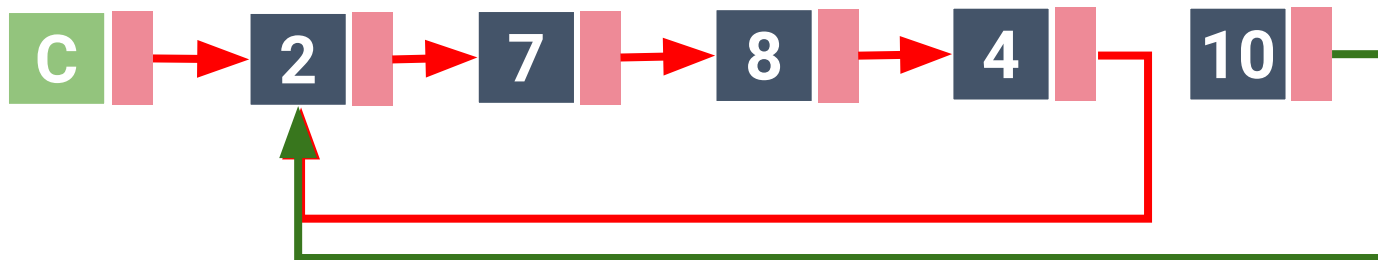
**Insert**

at the tail of the list

Step 1



Step 2



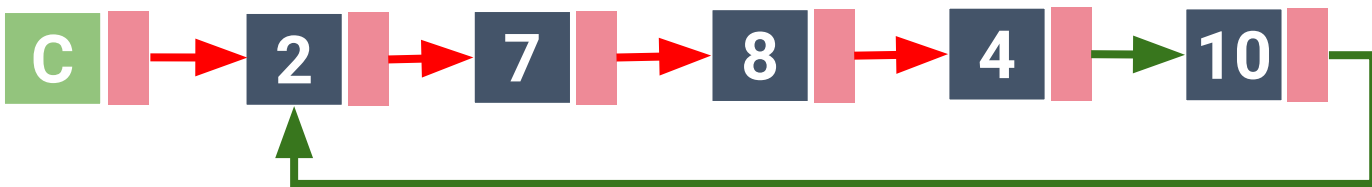
# Circular Linked Lists



**Insert**

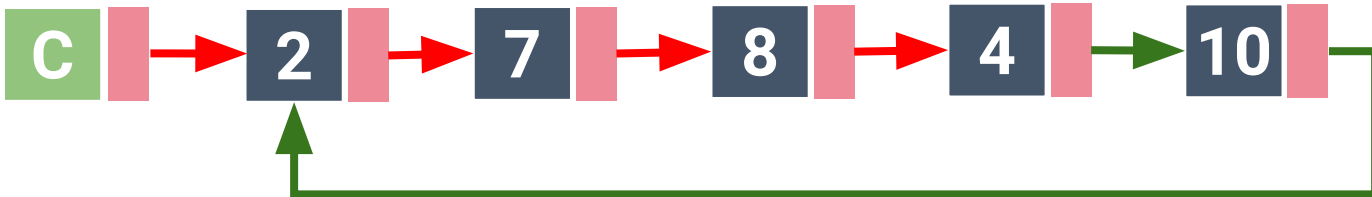
at the tail of the list

Step 3

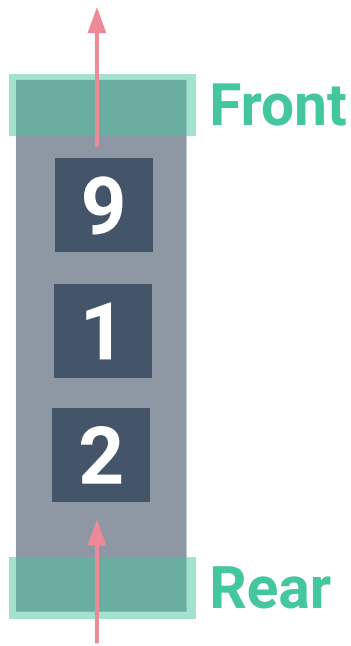


Step 4

count += 1



# Circular Linked Lists: Queues



How to Implement a Queue?

Array!!

and

**Linked Lists!!**

- Singly Linked Lists
- **Circular Linked Lists**

# Asymptotic Performance



	Queue		Circular Queue	
Operation	Running Time - Array	Running Time - Singly Linked List	Running Time - Array	Running Time - Circular Linked List
Q.enqueue(e)	$O(n)$	$O(1)$	$O(1)$	
Q.dequeue()	$O(n)$	$O(1)$	$O(1)$	
Q.first()	$O(1)$	$O(1)$	$O(1)$	$O(1)$
Q.is_empty()	$O(1)$	$O(1)$	$O(1)$	$O(1)$
len(Q)	$O(1)$	$O(1)$	$O(1)$	$O(1)$

# Linked Lists



## TYPE

**Singly** Linked List

**Circular** Linked List

**Doubly** Linked List

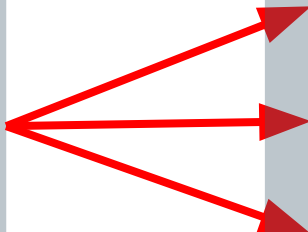
**Circular Doubly** Linked List

## ACTION

Traversing

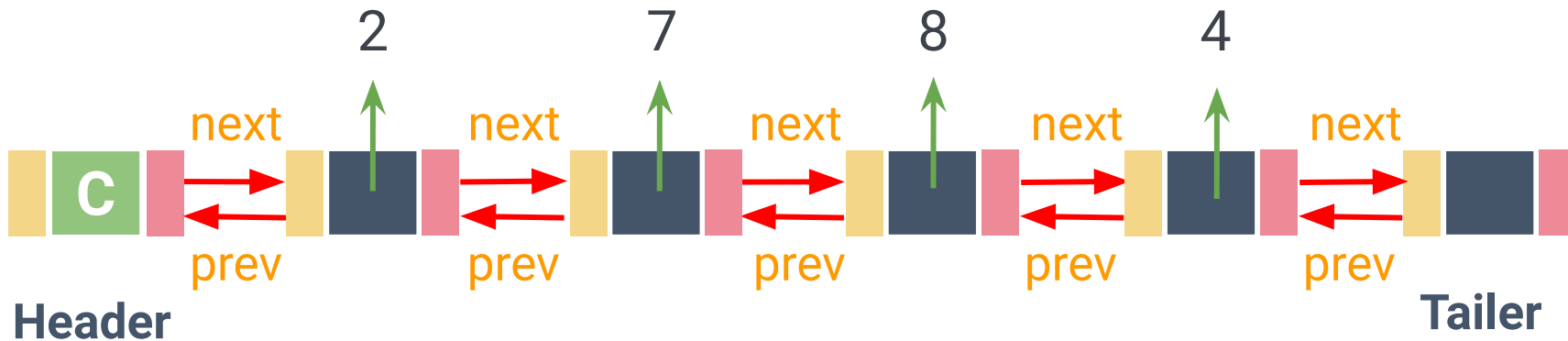
Insert

Delete





# Doubly Linked Lists



# Doubly Linked Lists

Address/Byte# Value

6000	4
6001	6003
6002	
6003	2
6004	6009
6005	6000
6006	8
6007	6013
6008	6009
6009	7
6010	6006
6011	6003
6012	
6013	4
6014	6016
6015	6006
6016	T
6017	6013

next Header



Suppose that it takes 1 byte to store an integer.

next  
prev

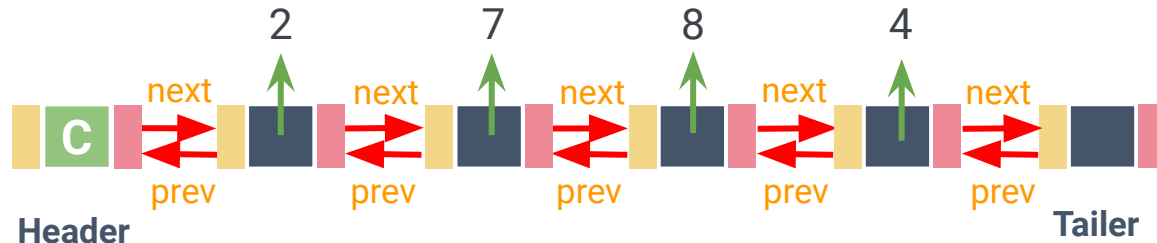
next  
prev

next  
prev

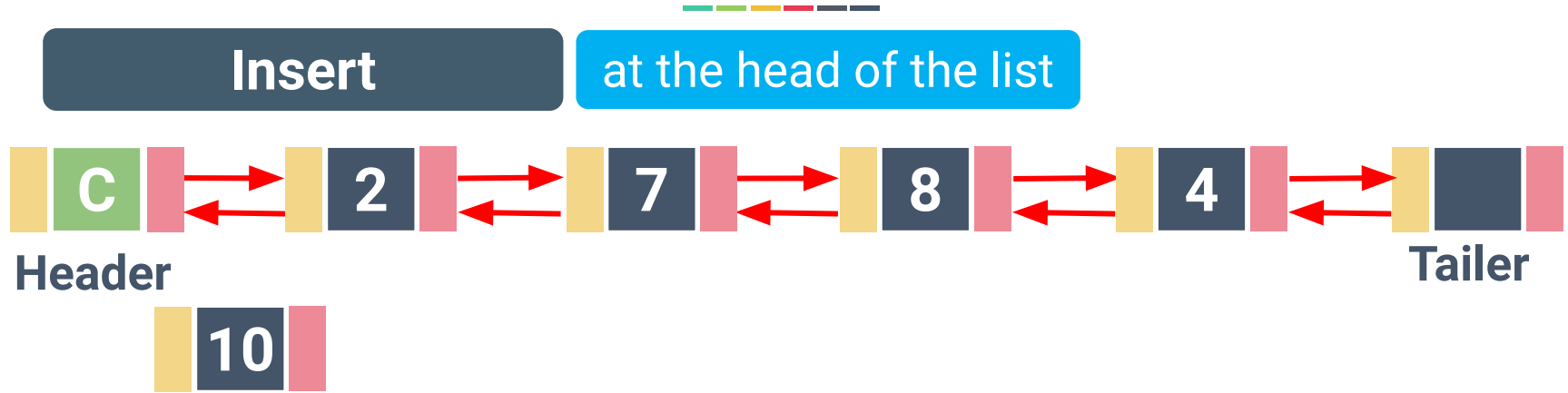
next  
prev

prev

Tailer



# Doubly Linked Lists



Step 1: Create a new node storing reference to an element

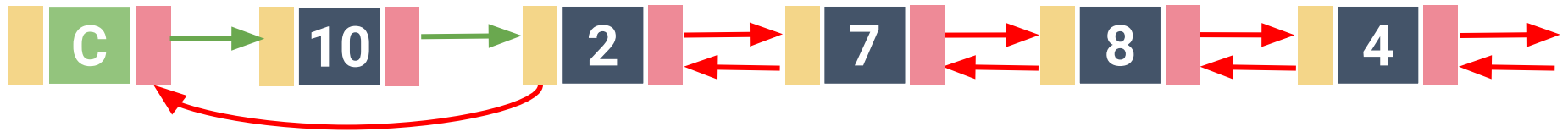
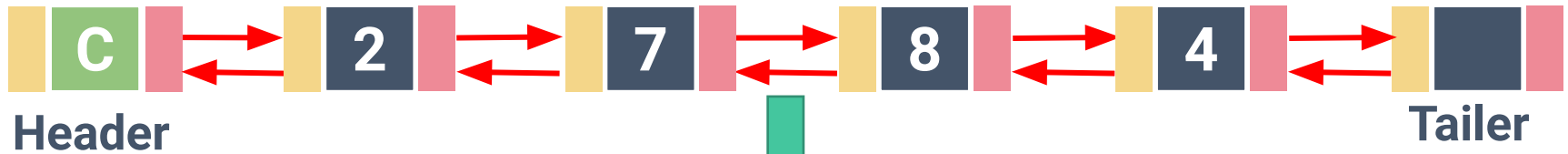
Step 2: Set a new node's next pointer to the current head node

Step 3: Set the list's head to refer to the new node

# Doubly Linked Lists

**Insert**

at the head of the list

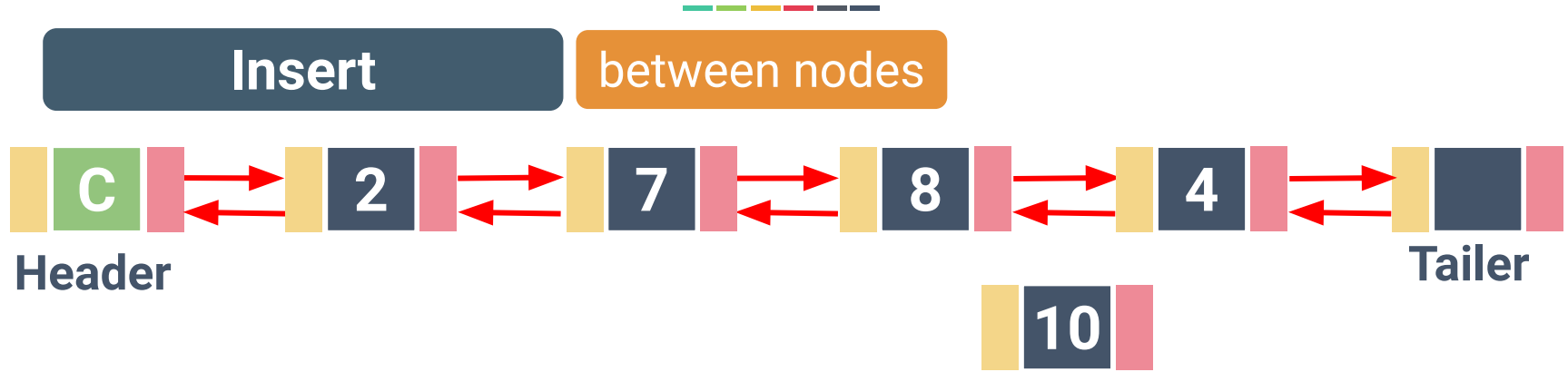


Step 4:

Step 5:

Step 6: Increment the node count

# Doubly Linked Lists

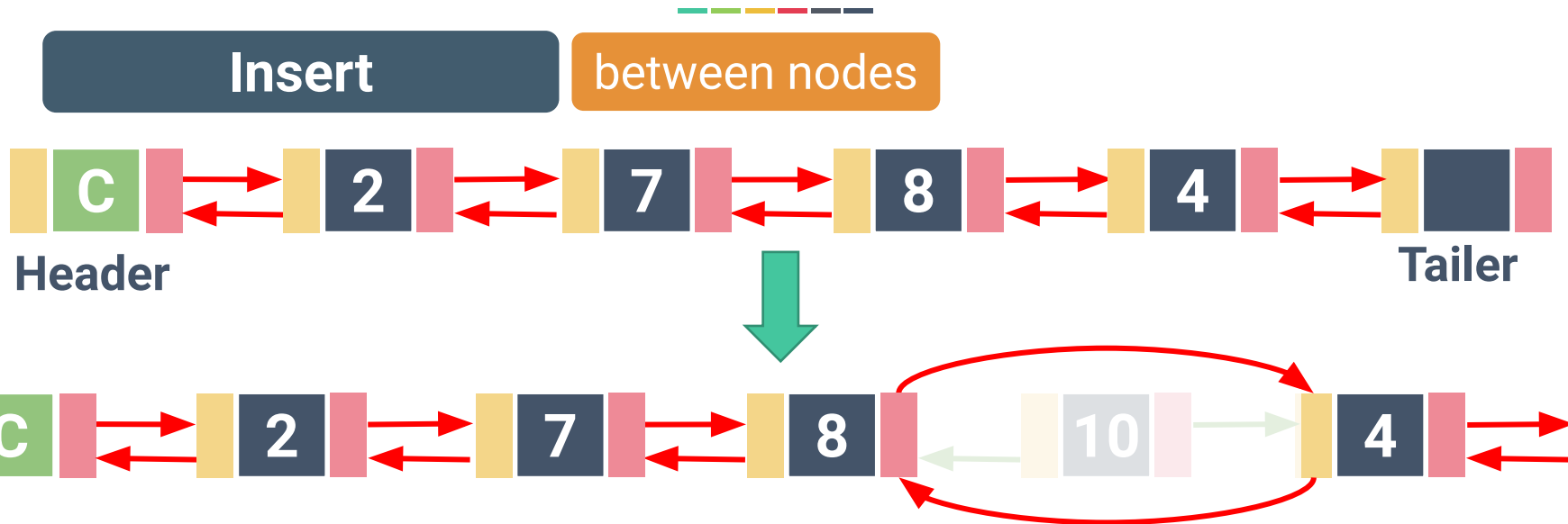


Step 1: Create a new node storing reference to an element

Step 2: Set a new node's next pointer to the next node

Step 3:

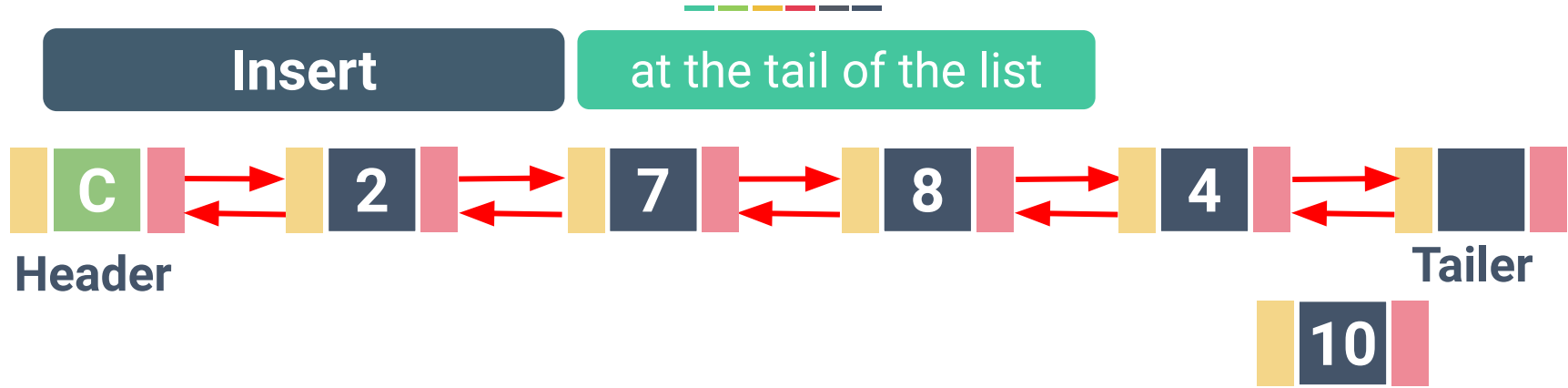
# Doubly Linked Lists



Step 5:

Step 6: Increment the node count

# Doubly Linked Lists



Step 1: Create a new node storing reference to an element

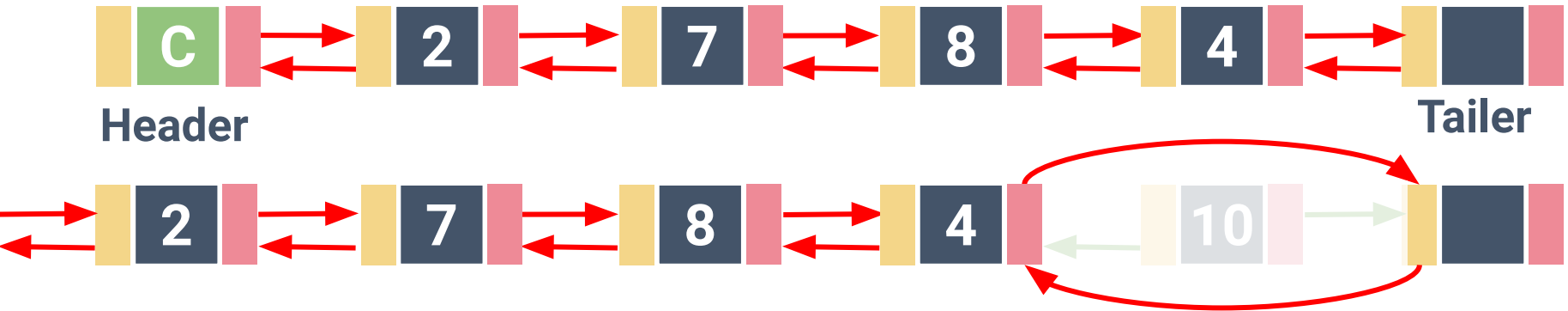
Step 2: Set a new node's next pointer to the tailer node

Step 3: Set the new node's previous pointer to the previous node.

# Doubly Linked Lists

Insert

at the tail of the list



Step 4:

Step 5: Set the previous node's next pointer to the new node.

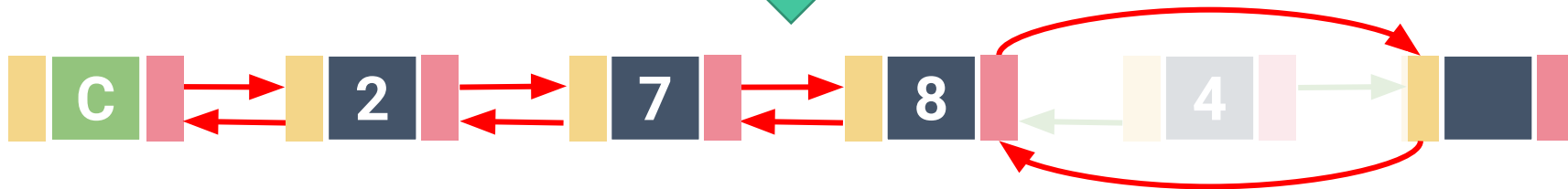
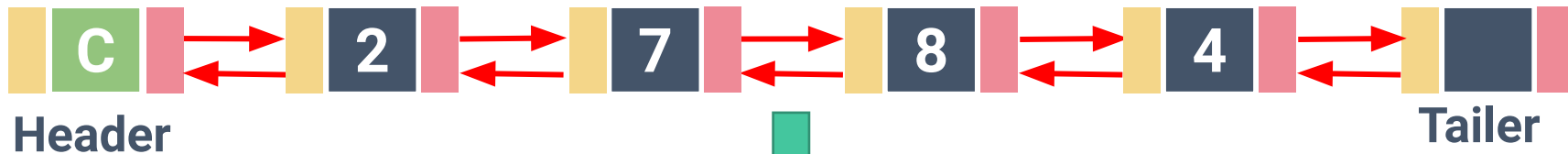
Step 6: Increment the node count



# Doubly Linked Lists

**Delete**

at the tail of the list



Step 1:

Step 2:

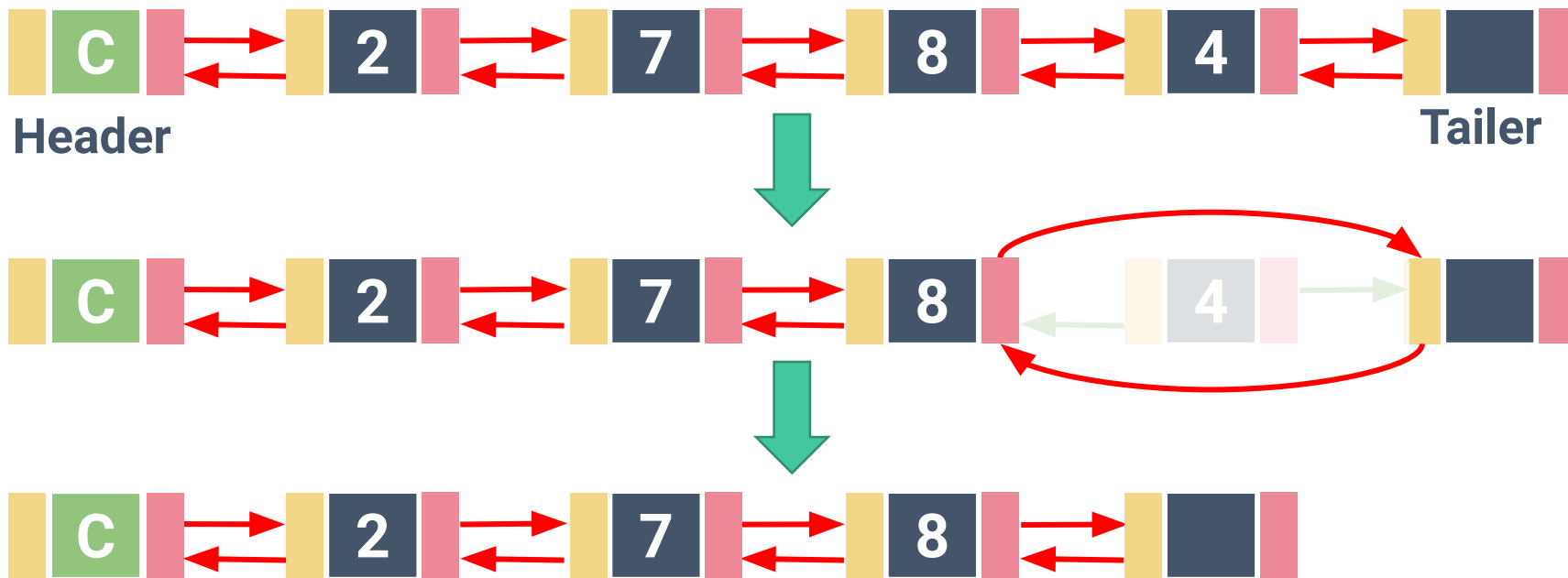
Step 3:

# Doubly Linked Lists



Delete

at the tail of the list



# Asymptotic Performance



Operation		Running Time - Singly Linked List	Running Time - Doubly Linked List
Insert	At the head	$O(1)$	
	Between nodes	$O(1)$	
	At the tail	$O(1)$	
Delete	At the head	$O(1)$	
	Between nodes	$O(n)$	
	At the tail	$O(n)$	

# Linked Lists



## TYPE

**Singly** Linked List

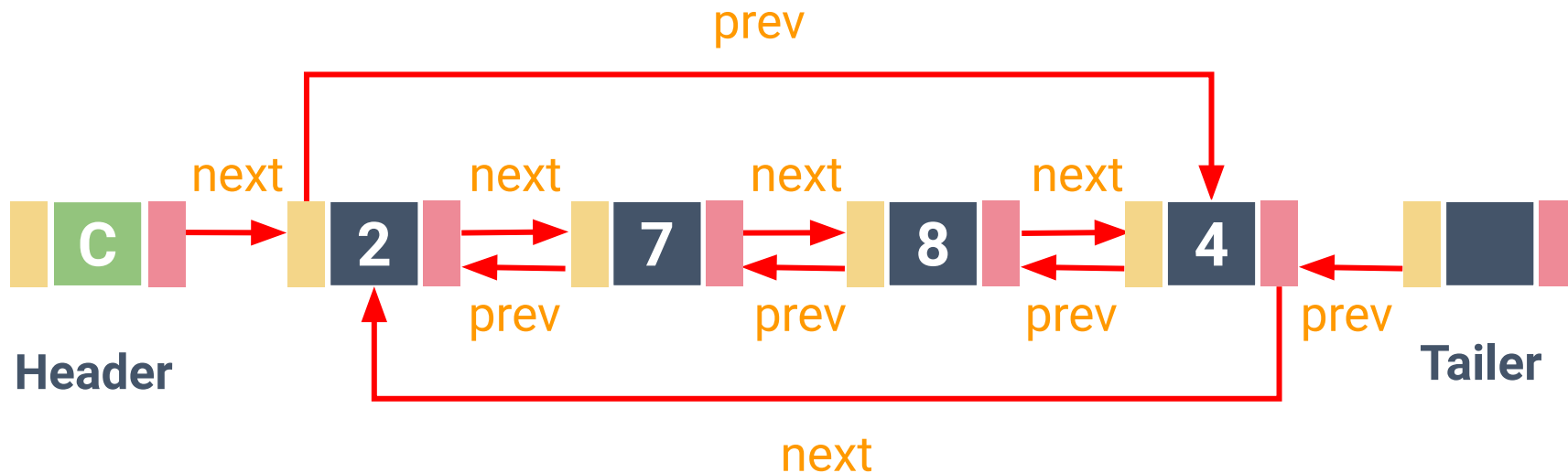
**Circular** Linked List

**Doubly** Linked List

**Circular Doubly** Linked List



# Circular Doubly Linked Lists



# Summary



## Linked list properties:

- Each node contains an element and a pointer(s) to the next node (and previous node).
- **Sequential access** only: nodes are read from the beginning.
  - Not convenient to have an index, unlike array-based sequences.
- No pre-allocated fixed size of memory, resizable.
- Insertion and deletion operations are more efficient compared to array.
  - Take  $O(1)$  - constant time to add and remove elements at any part in linked lists.

# Summary



## Linked list's limitations:

- Accessing the data/node in lists takes linear time -  $O(n)$ 
  - To find the item or node at certain location, linked list has to start from the first node and traversing until the target is found.
  - Unable to perform binary search.
- Use extra storage than the array to keep pointers/references.
  - Impractical for storing small data such as characters.