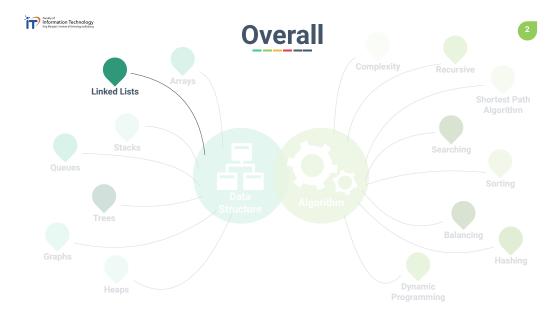


# **Chapter 5: Linked Lists**

**Dr. Sirasit Lochanachit** 







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**Linked lists** 



To avoid these limitations, an alternative to array is linked list.

# Array 2 7 8 4 Value 0 1 2 3 Index



- Length of array has to be pre-allocated, empty space wasted.
- Adding or removing elements between values in the array is expensive O(n)



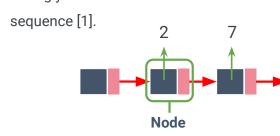
#### **Linked Lists**

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#### **Singly Linked Lists**

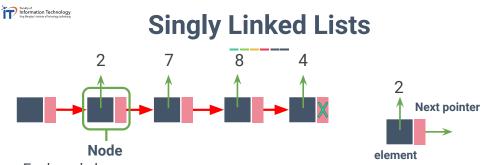
6

A singly **linked list** is a collection of nodes that form a linear order of a



[1] Michael T. Goodrich et al., Data Structures and Algorithms in Python, 2013

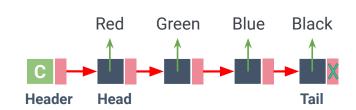




- Each node keeps:
- A reference to an object/value which is its element.
- Link/Pointer: One or more references to adjacent nodes or subsequent nodes.
  - Reference to None if there is no further node.



# **Singly Linked Lists**



- Head and tail identify the first and last node, respectively.
- **Header** node can contain a counter to keep track the number of nodes that form a list.

#### **Linked Lists**



## **Singly Linked Lists**

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#### Real-life examples of Linked Lists:







Retrieved from https://live.staticflickr.com/5610/15429943089\_edc7011843\_o\_d.jpq CC BY 2.0 https://live.staticflickr.com/23/26472155\_8cc5066b66\_o\_d.jpq CC BY-SA 2.0



For simplicity, the linked list illustration will embed element within the node.

Note that each node still contains a reference to the element, not the element itself directly.



# **Singly Linked Lists**



- Traversing or link hopping is the process of moving from one node to another according to each node's subsequent pointer.
- Linked Lists provides sequential access only.
  - $\circ$  Locating the element in a linked list requires O(n) time to traverse the list from the beginning.



# **Singly Linked Lists**

Suppose that it takes 1 byte to store an integer.

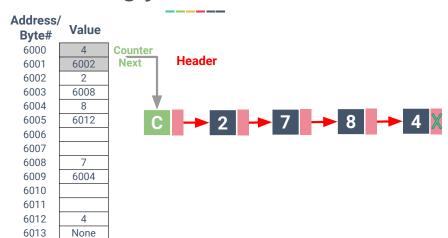


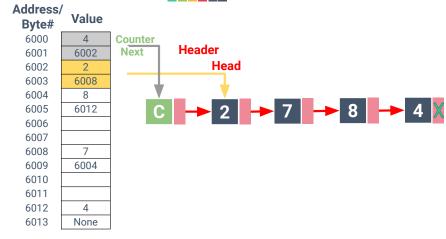




#### **Singly Linked Lists**





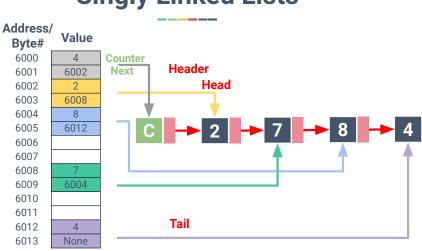


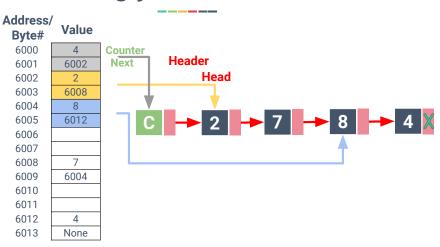
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#### **Singly Linked Lists**



#### **Singly Linked Lists**





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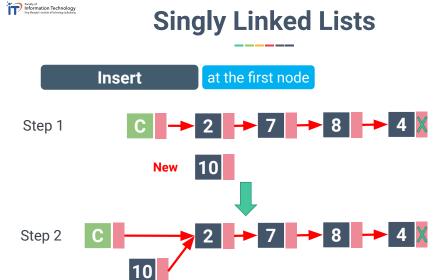
#### **Singly Linked Lists**

Step 1: Create a new node storing reference to an element.

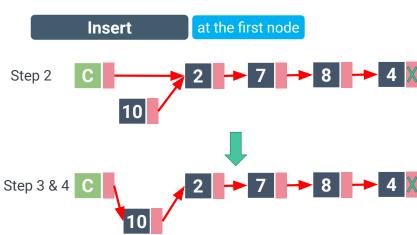
Step 2: Set new node's next pointer to the current/old head.

Step 3: Set the list's head to reference the new node.

Step 4: Increment the node count.



Singly Linked Lists





Address/

Byte#

6000

6001

6002

6003 6004

6005 6006

6007

6008

6009

6010

6011

6012

6013

Value

4

6002

6008

8

6012

6004

4

None

Step 1

Create a

new node

#### **Singly Linked Lists**

**Value** 

6002

6008

8

6012

10

6004

4

None

Step 2, 3 & 4

Set

**Pointers** 

Address/

Byte#

6000

6001

6002

6003

6004

6005

6006

6007

6008

6009

6010

6011

6012

6013

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Address/

Byte#

6000

6001

6002

6003

6004

6005

6006

6007

6008

6009

6010

6011

6012

6013

Value

6006

2

6008

8

6012

10

6002

4

None

#### **Singly Linked Lists**

22

Insert

at the first node

Algorithm add\_front(L, e):

new\_node = Node(e)

new node.next = L.head

L.head = new node

L.size = L.size + 1

if L.tail == None:

L.tail = L.head

# Create new node instance

# Set new node's next pointer to the old head

# Update the list's head to reference the new node

# Increment the node count

# List was empty O(1)

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## **Singly Linked Lists**

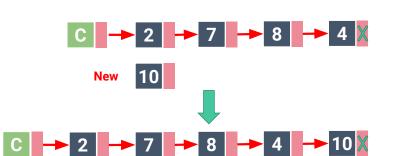
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**Singly Linked Lists** 

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Insert

at the last node



Insert

at the last node



Step 1: Create a new node storing reference to an element.

Step 2: Set new node's next pointer to None.

O(1)

Step 3: Update the list's tail to reference the new node.

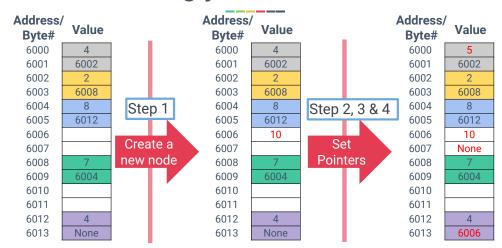
Step 4: Increment the node count.



Insert at the last node New C → 2 → 7 → 8 → 4 X Step 1 C → 2 → 7 → 8 → 4 X Step 3 & 4 C  $\longrightarrow$  2  $\longrightarrow$  7  $\longrightarrow$  8  $\longrightarrow$  4  $\longrightarrow$  10  $\times$ 



#### **Singly Linked Lists**





#### **Singly Linked Lists**

0(1)



#### **Singly Linked Lists**

#### Insert

#### at the last node

Algorithm add\_last(L, e):

else:

new\_node = Node(e) # Create new node instance

new node.next = None # Set new node's next pointer to None

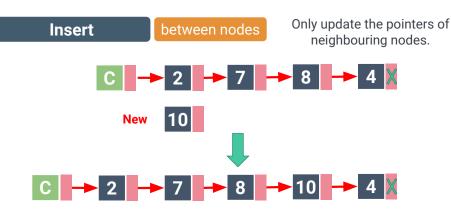
if I tail == None: # List was empty

L.head & L.tail = new node

L.tail.next = new\_node # Make old tail point to new node

L.tail = new\_node # Update the list's tail to reference the new node

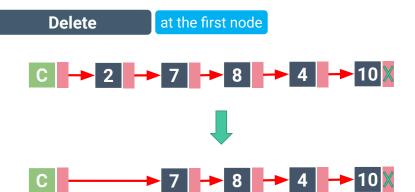
L.size = L.size + 1 # Increment the node count



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#### **Singly Linked Lists**





Step 1: Set head node's next pointer to the subsequent node.

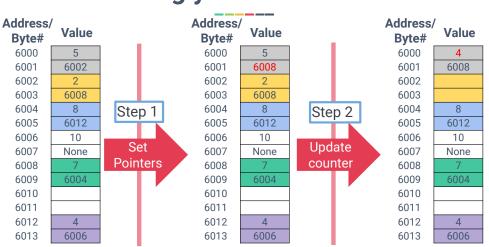
• If head is **None**, then the list is empty, return error.

Step 2: Decrement the node count.

0(1)



#### **Singly Linked Lists**



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#### **Singly Linked Lists**

Delete

at the first node

Algorithm remove\_first(L):

if L.head == None: # List is empty

return Error

L.head = L.head.next # Make head point to next node or None if empty

L.size = L.size - 1 # Decrement the node count

if L.head == None: # List is empty after first node is removed

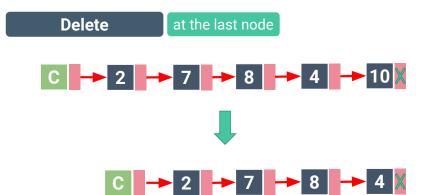
L.tail = None

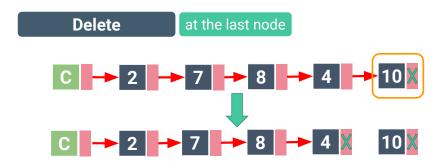
O(1)





#### **Singly Linked Lists**





Step 1: Find the next to last node, then update the next pointer to None.

Step 2: Decrement the node count.

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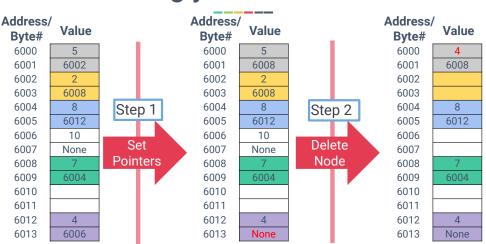
**Singly Linked Lists** 

**Deletion** of the last node in Singly Linked Lists:

- No direct link from the tail node to the node before the tail.
  - There is only a link from the node before the tail to the tail node.
- To access the node before the tail, need to start from the head node and search through the list - O(n).
- To address this problem, **doubly linked list** is proposed as an alternative to singly linked list. also keeps links in backward direction.

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#### **Singly Linked Lists**





O(n) - why?





**Singly Linked Lists: Stacks** 

**Delete** 

at the last node

Algorithm remove\_last(L):

if L.head == L.tail:

if L.head == None: return Error # List is empty

L.head & L.tail = None

else:

p = L.head # Initialise pointer to traverse the list

while p.next.next != None: # Traverse until next to last node is found

# List has one node

p = p.next

p.next = None, L.tail = p # Update tail pointer

L.size = L.size - 1 # Decrement the node count O(n)



How to Implement a Stack?

Array!!

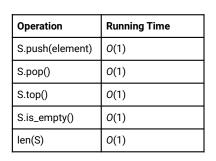
and

**Linked Lists!!** 

• Singly Linked Lists

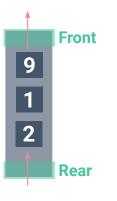


#### **Asymptotic Performance**





#### **Singly Linked Lists: Queues**



How to Implement a Queue?

Array!!

and

**Linked Lists!!** 

• Singly Linked Lists





#### **Asymptotic Performance**

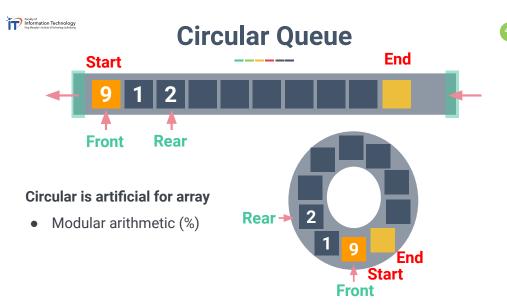
| Operation    | Running Time |
|--------------|--------------|
| Q.enqueue(e) | 0(1)         |
| Q.dequeue()  | 0(1)         |
| Q.first()    | 0(1)         |
| Q.is_empty() | 0(1)         |
| len(Q)       | 0(1)         |





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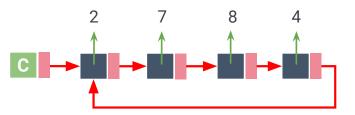


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#### **Circularly Linked Lists**

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A **circularly linked list** adds the notion of having the tail of the list to point back to the head of the list as the next node.



# **Circularly Linked Lists**



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#### **Circularly Linked Lists**

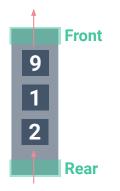
| Address/ |       |
|----------|-------|
| Byte#    | Value |
| 6000     | 4     |
| 6001     | 6002  |
| 6002     | 2     |
| 6003     | 6008  |
| 6004     | 8     |
| 6005     | 6012  |
| 6006     |       |
| 6007     |       |
| 6008     | 7     |
| 6009     | 6004  |
| 6010     |       |
| 6011     |       |
| 6012     | 4     |
| 6013     | 6002  |
|          |       |

Suppose that it takes 1 byte to store an integer.





#### **Circularly Linked Lists: Queues**



How to Implement a Queue?

Array!!

and

Linked Lists!!

- Singly Linked Lists
- Circularly Linked Lists

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# **Asymptotic Performance**

| Operation    | Running Time |  |
|--------------|--------------|--|
| Q.enqueue(e) | 0(1)         |  |
| Q.dequeue()  | 0(1)         |  |
| Q.first()    | 0(1)         |  |
| Q.is_empty() | 0(1)         |  |
| len(Q)       | 0(1)         |  |

48

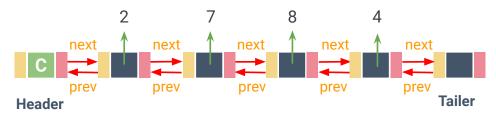
Singly Linked List

Circularly Linked List

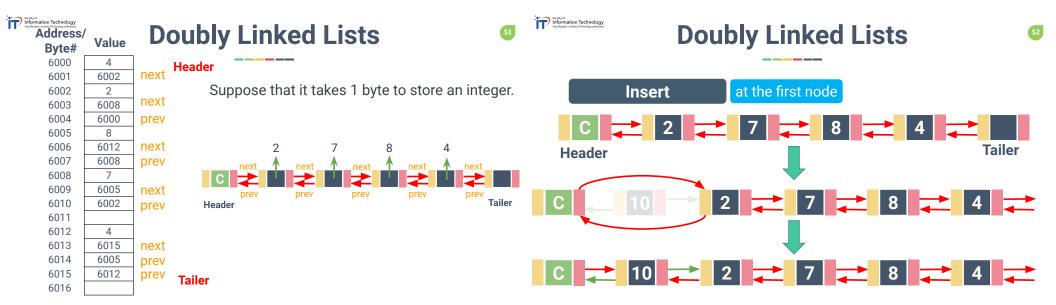
Doubly Linked List

Doubly Circularly Linked List

To add more symmetry to the list, **doubly linked lists** allow each node to keep a reference to the node <u>before</u> it and a pointer to the node <u>after</u> it.



[1] Michael T. Goodrich et al., Data Structures and Algorithms in Python, 2013



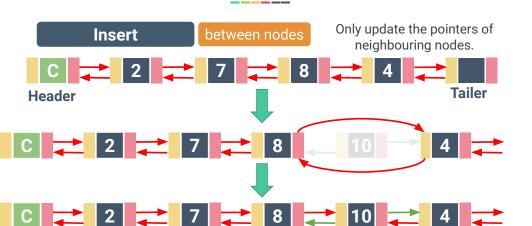


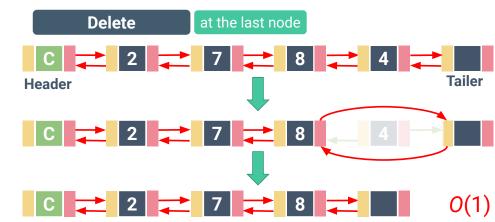
#### **Doubly Linked Lists**

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#### **Doubly Linked Lists**

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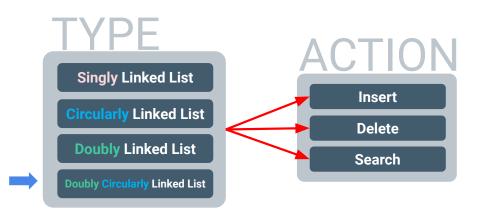


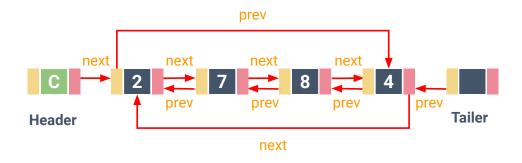
## **Linked Lists**

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#### **Doubly Circularly Linked Lists**

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#### **Linked Lists**







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#### Linked list properties:

- Each node contains an element and a pointer(s) to the next node (and previous node).
- Sequential access only: nodes are read from the beginning.
  - Not convenient to have an index, unlike array-based sequences.
- No pre-allocated fixed size of memory, resizeable.
- Insertion and deletion operations are more efficient compared to array.
  - $\circ$  Take O(1) constant time to add and remove elements at any part in linked lists.

#### Linked list's limitations:

- Accessing the data/node in lists takes linear time O(n)
  - To find the item or node at certain location, linked list has to start from the first node and traversing until the target is found.
  - For example, find the 10th node, has to traversing 10 times.
  - Unable to perform binary search.
- Use extra storage than the array to keep next pointers/references.
  - o Impractical for storing small data such as characters.



#### **Linked Lists vs Arrays**



| Operations                    | Array<br>(Dynamic size) | Linked List  |
|-------------------------------|-------------------------|--|
| Indexing/searching            | 0(1)                    | O(n)   |
| Add/remove at beginning       | O(n)                    | 0(1)   |
| Add/remove at end             | 0(1)                    | O(1) when last element is known<br>O(n) when last element is unknown |
| Add/remove in between         | O(n)                    | O(1)   |
| Wasted memory space (average) | O(2n)                   | O(2n) - Singly linked list or<br>O(3n) - Doubly linked list          |



#### **Individual Assignment**



- Assignment#3: Queues
- Due 09.00 am, Tuesday 01/09/2020.
- Submission
  - Email: sirasit@it.kmitl.ac.th
  - o Paper: in classroom next week
- Can be either written by hand or typing.
- Make sure to submit on time!!
  - o Late submission has penalty on the score.
- If unable to submit on time for reasonable reasons, let me know asap.



# **Group Assignment**

- 61
- Presentation slides are due to be submitted via email by midnight (12AM) the day before the presentation.
- Make sure to submit on time!!
  - o Late submission has penalty on the score.
- If unable to submit on time for reasonable reasons, let me know asap.