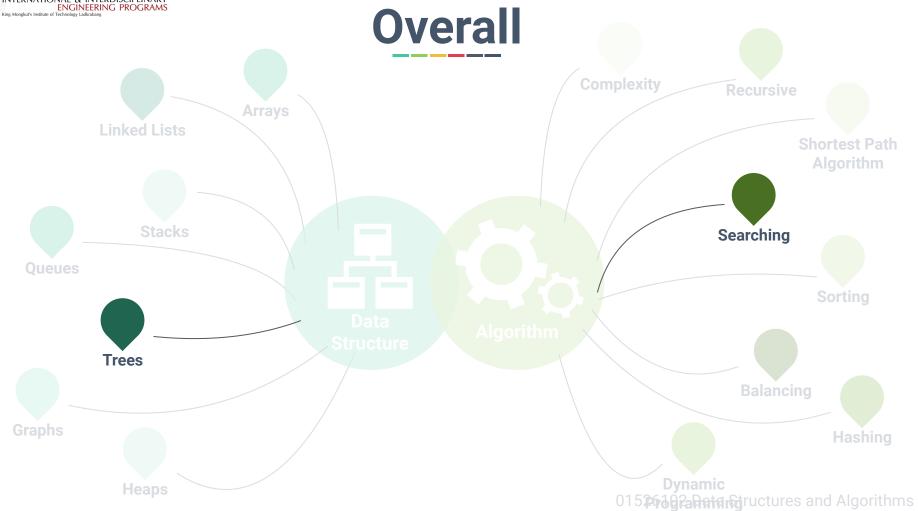


Chapter 8: Search Trees

Dr. Sirasit Lochanachit







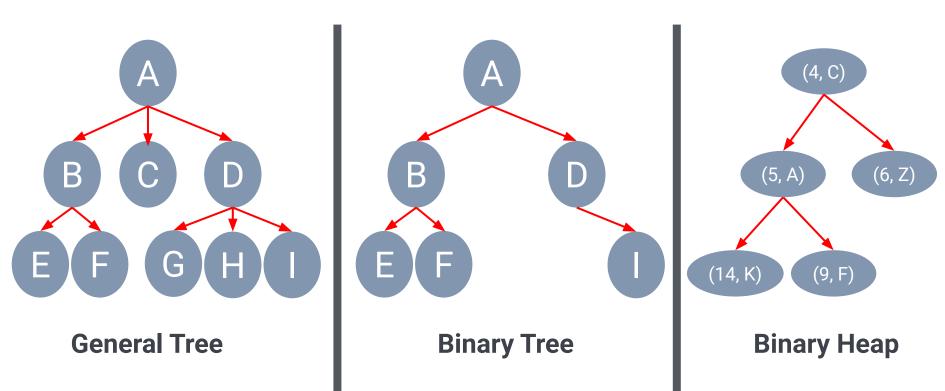
Outline

Binary Search Trees:

- Definition, properties and methods (search, add, delete)
- Algorithms and Operation examples



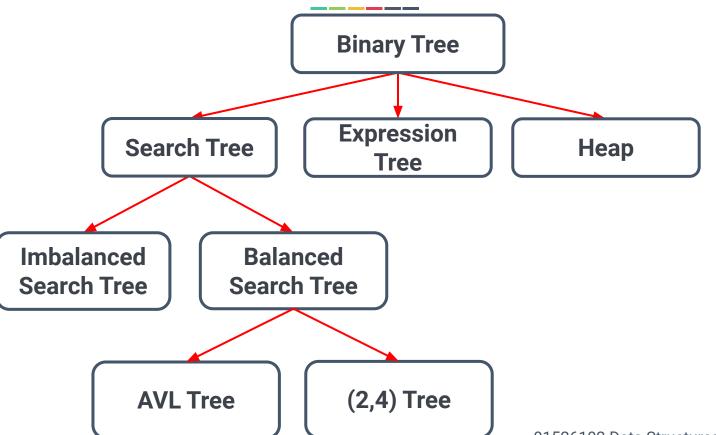
Types of Trees (Revisited)



01526102 Data Structures and Algorithms



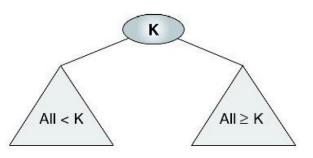
Types of Binary Trees



01526102 Data Structures and Algorithms



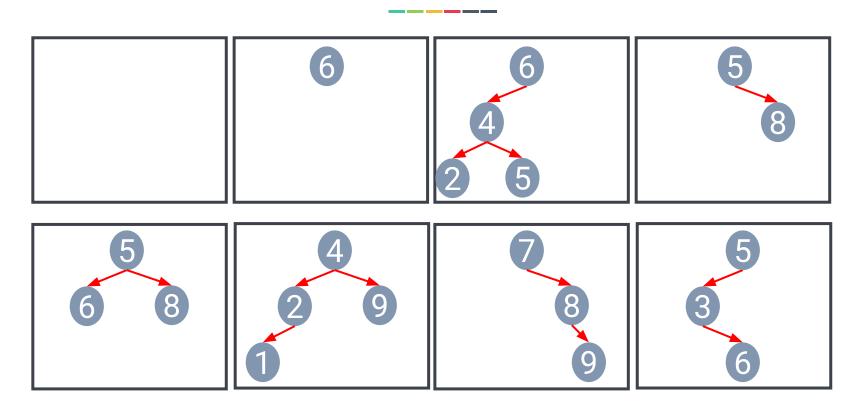
What is a Binary Search Tree?



- A binary search tree (BST) is a binary tree that stores an ordered sequence of elements or pairs of keys and values and has the following properties [1]:
 - All keys/elements in the *left subtree* are **less** than their *root*.
 - All keys/items in the **right subtree** are **greater than** or **equal to** their **root**.
 - Each subtree itself is a binary search tree.

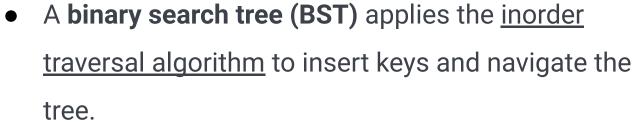


SCHOOL OF INTERNATIONAL & INTERDISCIPLINARY ENGINEERING PROCESS. Valid/Invalid Binary Search Trees?

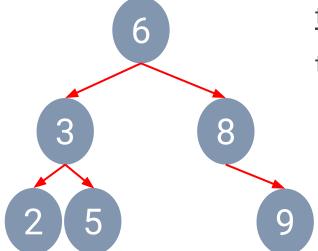




Binary Search Tree



Produces a sorted keys in linear time.





BST Node Implementation

class BST_Node:

```
def __init__(self, key, val, left=None, right=None, parent=None):
```

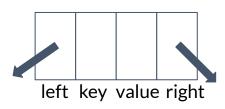
```
self._key = key
```

self._value = val

self._leftChild = left

self._rightChild = right

self._parent = parent





BST Implementation

class BinarySearchTree:

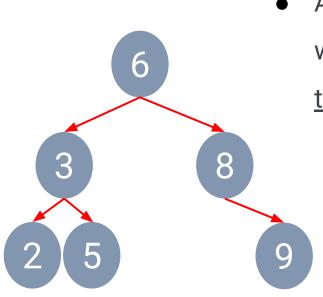
```
def __init__(self):
    self._root = None
    self._size = 0
```

def

def



Search in Binary Search Tree

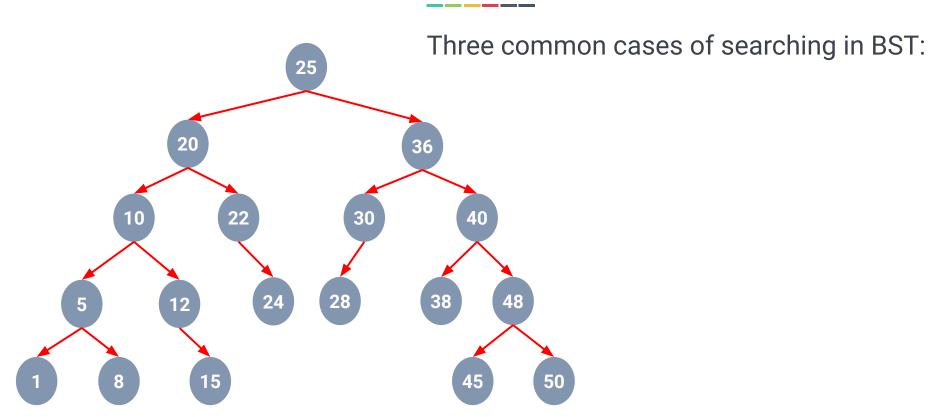


A **binary search tree (BST)** can be used to find whether a given key is stored in a tree by <u>starting at the root</u>.

For each position p, the searched key are compared with the key stored at position p, which is denoted as p.key().

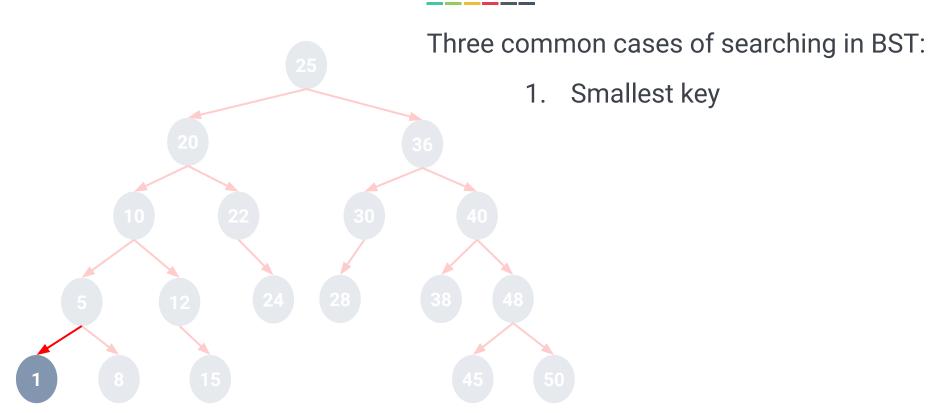


Searching in BST



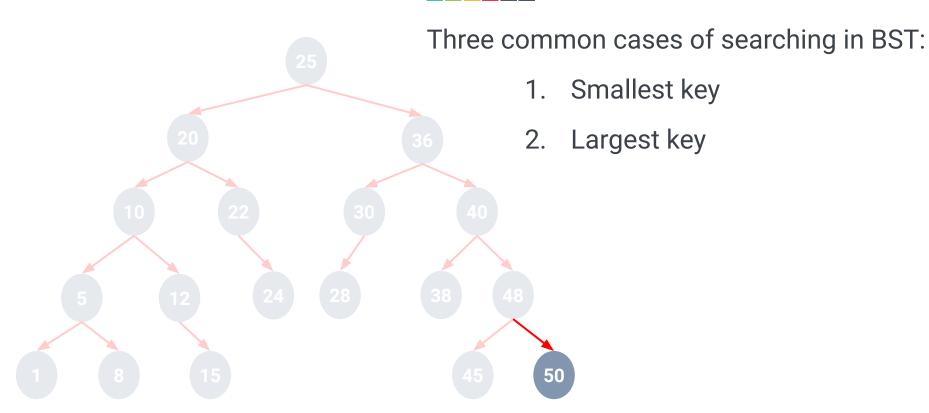


Find the Smallest Node



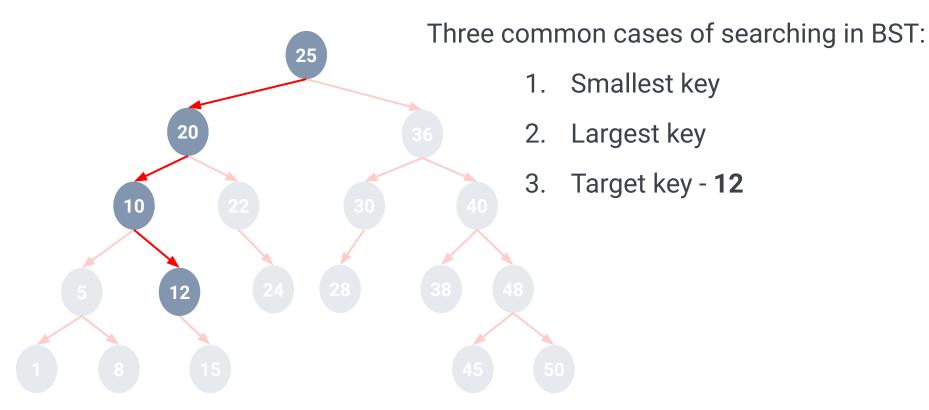


Find the Largest Node



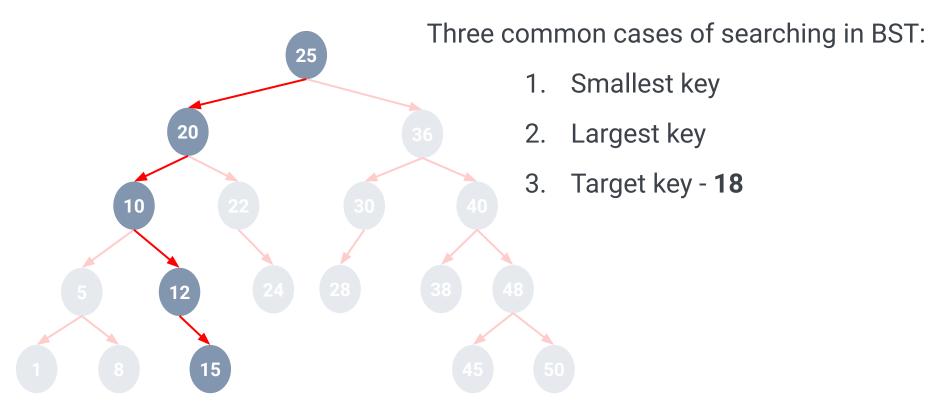


Searching a Target in a BST





Searching a Target in a BST

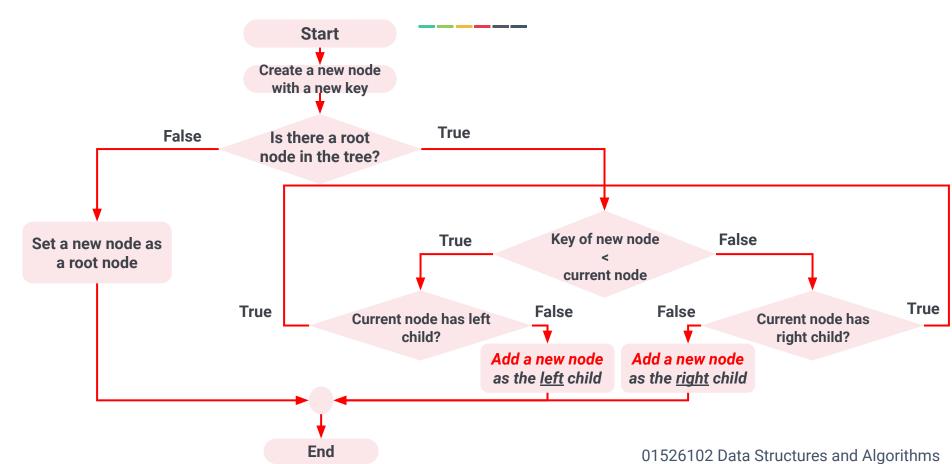




Binary Search Tree Algorithm Binary Search Tree Algorithm



BST Construction and Insertion BST Construction and Insertion



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BST Insertion Exercise 1



BST Construction and Insertion Algorithm

```
Algorithm treeInsert(key, value):
```

```
if rootNode is not empty then
```

```
_treeInsert(key, value, rootNode)
```

Root node exists

else:

create a new tree and put key & value as the root #Root node not exists

```
self._size = self._size + 1
```

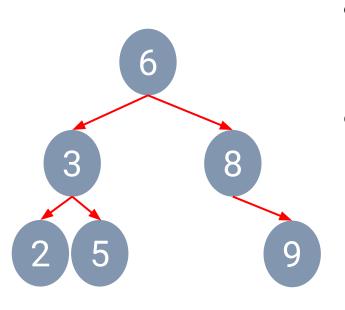


EST Construction and Insertion Algorithm

Algorithm _treeInsert(key, value, currentNode): if key < currentNode.key then</pre> # Recur on left subtree else else: # Recur on right subtree else

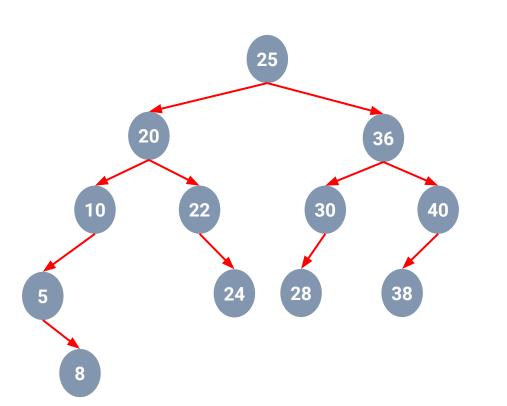


BST Deletion



- The deletion of a key from a BST can be performed on any node.
- Once a target node is found, three cases to consider:





#1: The node has zero child.





BST Deletion Algorithm (cont.)

Algorithm _deleteNode(currentNode):

```
if currentNode is a leaf node then #1: The node has zero childif currentNode is the left child of the parent node thenSet the parent node's left child to Noneelse
```

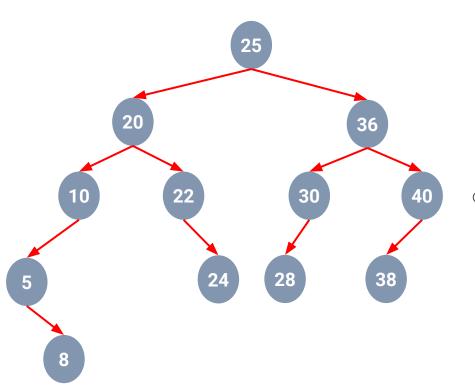
Set the parent node's right child to **None**



If a node has only a **single** child, the child could be promoted and replace its parent.

- 6 Sub-cases to consider:
 - A node has a left child
 - A node itself is a left child.
 - A node itself is a right child.
 - A node itself is the root node, no parent.





#2: The node has **one** child.

10

A node has a left child

A node itself is a left child.



BST Deletion Algorithm (cont.)

Algorithm _deleteNode(currentNode) (cont.):

```
elif currentNode.hasAnyChildren():
                                               #2: The node has one child
    if currentNode has a left child then
         if currentNode is the left child of the parent node then
              Update the parent pointer of its left child to currentNode's parent
              Set the parent node's left child to currentNode's left child
         else if currentNode is the right child of the parent node then
              Update the parent pointer of its left child to currentNode's parent
              Set the parent node's right child to currentNode's left child
         else
```

Replace the currentNode with the left child if currentNode has a right child then

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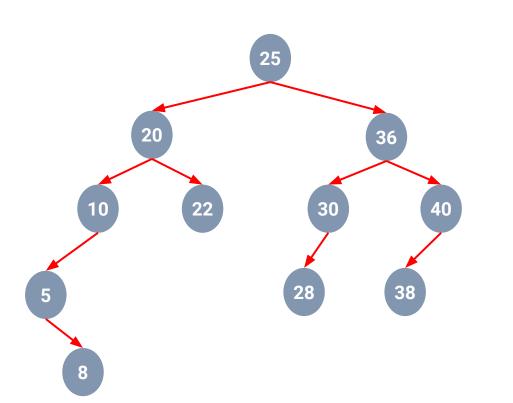


• If a node has **two** children, one of the child could not be simply promoted and replace its parent since the other child would be left out of the tree.



- To preserve a binary tree property, need to search the tree for a successor node, which is the next largest key after the deleted node:
 - If the successor has one child, it can be removed using case #1 or #2.
 - Then the successor node replaces the deleted node.
- The successor node could be either:
 - The <u>minimum</u> key node in the <u>right subtree</u>. Or
 - The <u>maximum</u> key node in the <u>left subtree</u>.





#3: The node has two child.





BST Deletion Algorithm (cont.)

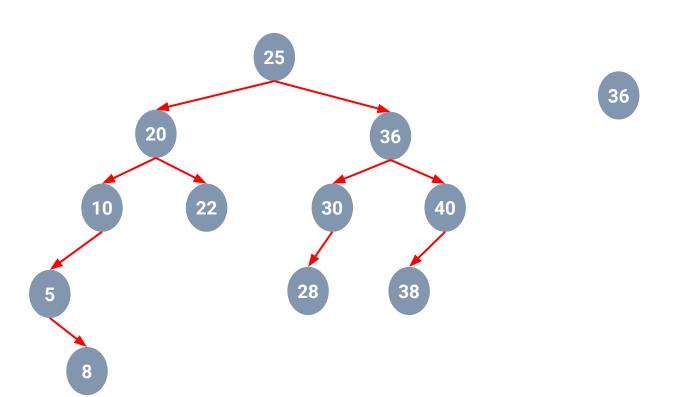
Algorithm _deleteNode(currentNode) (cont.):

```
elif currentNode.hasBothChildren(): #3: The node has two children
    successor = currentNode._rightChild
    while successor.hasLeftChild(): # find min key in a right subtree
        successor = current._leftChild()
    Update the parent and children (if any) nodes of the minimum key
node
```

Replace the currentNode with the minimum key node

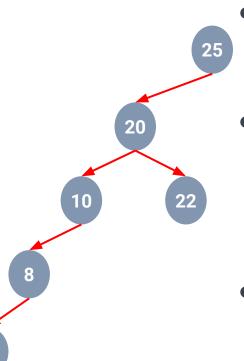


BST Deletion Exercise#1





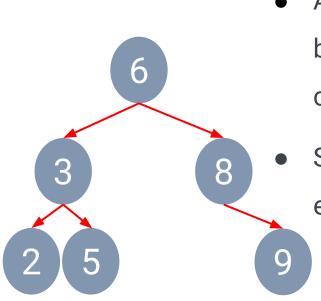
Binary Search Tree



- Running time of <u>inserting node</u> is also proportional to the **height of tree** (i.e. $log_2 n$ or n) == O(h).
- A balanced search tree has the same number of nodes in both left and right subtree.
 - Worst-case performance is $O(\log_2 n)$.
- Inserting keys in sorted order would construct an imbalanced tree.
 - Provides poor performance of Data nuctures and Algorithms



Balanced Binary Search Tree



- A balanced binary search tree (BST) maintains the balance through a <u>rotation operation</u> which consequently provides a better performance.
 - Several types of binary tree that automatically ensure balance
 - AVL tree
 - Splay tree
 - Red-black tree