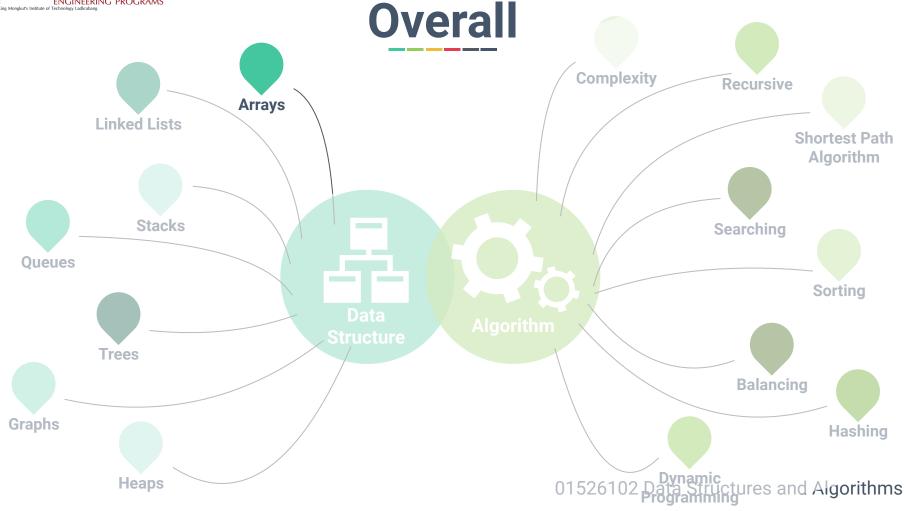


Chapter 2: Arrays

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Today's Outline

- 1. What is an Array?
- 2. 2D Arrays
- 3. 3D Arrays
- 4. Array Operations and Asymptotic Performance



Python Sequence Types

- Built-in class
 - list
 - tuple
 - o str



What is an Array?





What is an Array?



- It has a memory address to keep track of where a data is stored.
 - o Each byte has a unique number as its address.
- Although the number is sequential, any byte/element in a RAM can be accessed to read or write with a constant time O(1).



What is an Array?



- An array is a chunk of memory, consisting of equal-size elements.
- Each of those elements has an integer index, which uniquely refers to the value stored.
- The values are all of the same type (integer, character, etc.).1d Algorithms



Array of Characters



- In Python, it represents a unicode character with 16 bits (i.e. 2 bytes).
- Since each cell has an equal-size bytes, any element can be accessed constantly with this formula:
 - start_address + cell_size * index



Exercise

Given an array:

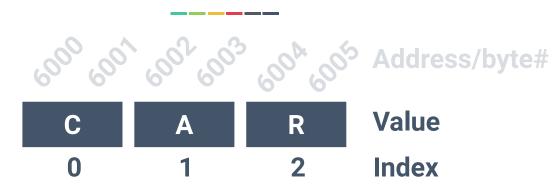
Start Address is 6000, cell size is 8,

What is the address of the element at index 6?

start_address + cell_size * index



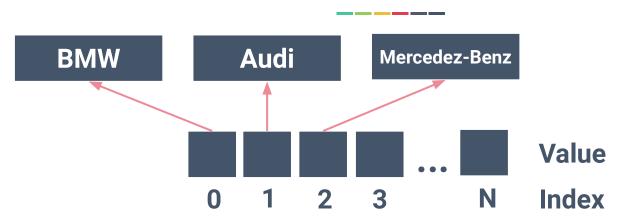
Array of Characters



 Luckily, a programming language calculate memory addresses of an array automatically.



Python List



- Python list is a referential-type array that stores the memory addresses (references) of a value instead of the value itself.
- Strings can be in any length, but memory addresses are fixed-size.

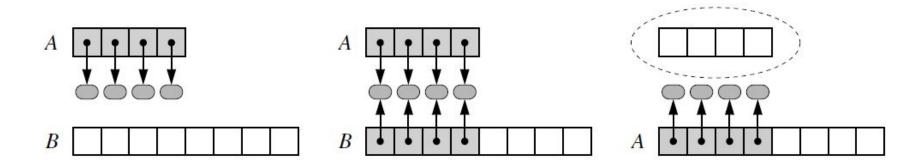


Static Array

- Once an array in C or Java has been created, it's size is fixed.
- Python tuple and str instances are <u>immutable</u>.
 - Unable to change size and value



Dynamic Array

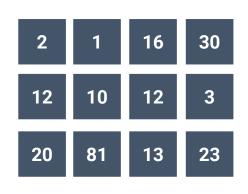


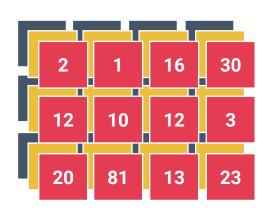
- Python's list instance maintains an underlying array that often has greater capacity than the current length of the list.
- If a capacity is exhausted, the list class requests a new, larger array.



Arrays







(a) One dimension

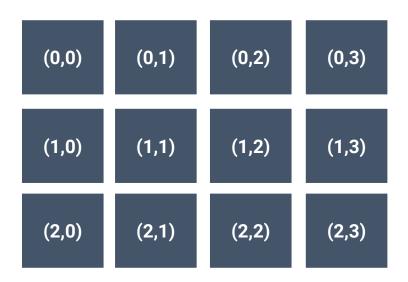
(b) Two dimensions

(c) Three dimensions

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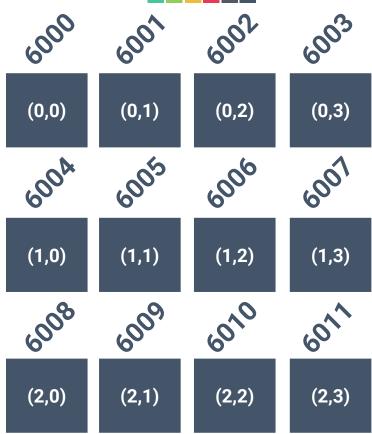


2-Dimensional Arrays



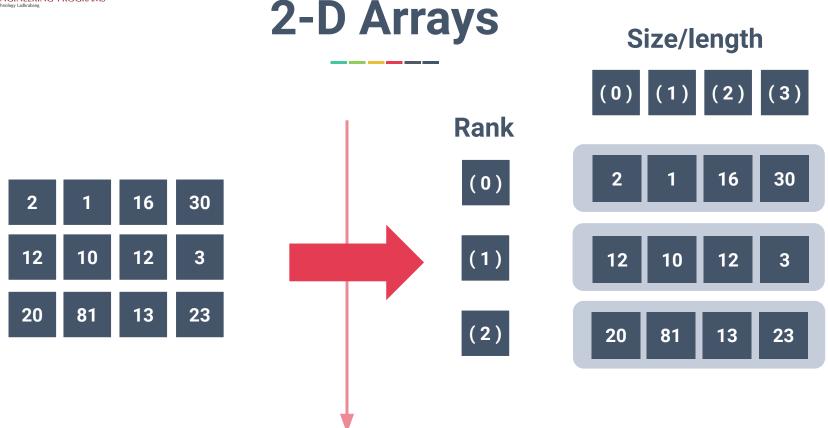


2-Dimensional Arrays



02 Data Structures and Algorithms





(a) Two dimensions

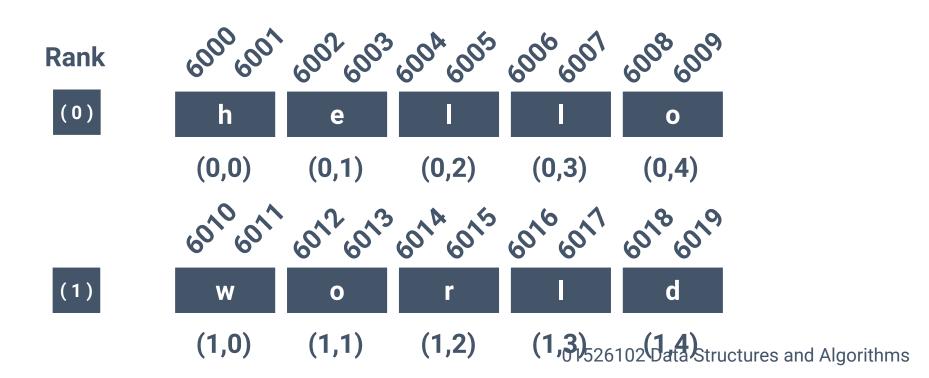
(b) Nested-one dimension



Example

Python Code: 2-D Arrays

c = np.array([['h','e','l','l','o'],['w','o','r','l','d']])





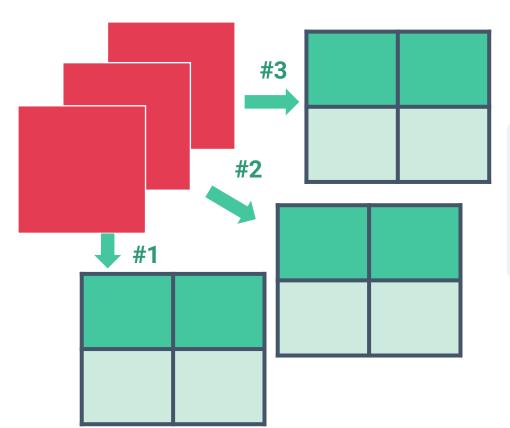
Exercise

Based on previous slide, suppose start address is 6000, find the address of index (1,4)

- start_address + cell_size * index
- Where index = (target_rank * array_length) + target_index



3D Arrays

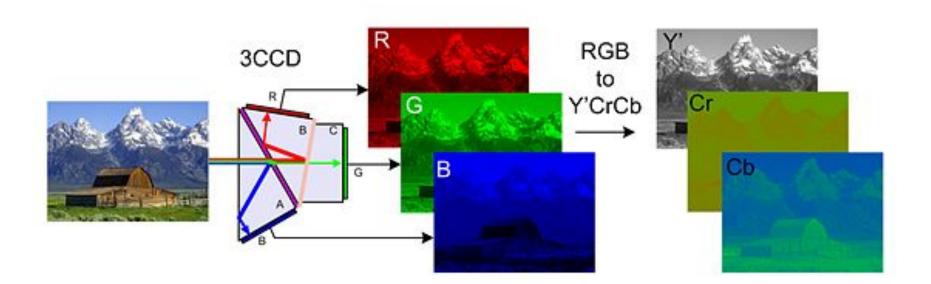


Python Code: 3D Arrays

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3D Arrays



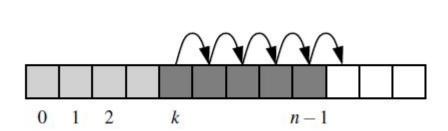


List Operations

Operation	Running Time
len(data)	O(1)
data[i]	O(1)
data[i] = val	O(1)
c * data	<i>O</i> (n)
data.reverse()	O(n)
data.sort()	O(n log n)



Adding Elements to a List



- Operation insert(k, value) requires creating a room to insert a new element at index k of a dynamic array
 - Make room by shifting forward the (n 1) k elements data[k], ..., data[n-1]
 - O(n k + 1) for inserting at index k



Lab 3-1

Record the <u>average</u> running time of insert(k, 20) in seconds with three different inserting patterns for each of the *N* calls:

- 1. Repeatedly insert at the beginning of a list
- 2. Repeatedly insert near the middle of a list
- 3. Repeatedly insert at the end of the list
 - Each pattern starts from an empty list[] -> data = []

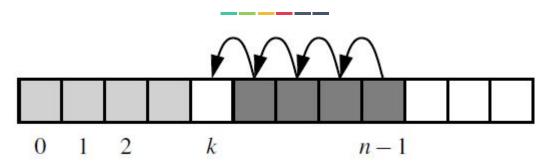


Lab 3-1

	N								
Patterns	10	20	50	100	200				
First Case									
Second Case									
Third Case									



Removing Elements from a List



- Operation pop(k) removes the element that is at index k < n of a list
 - Then shifting backward the (n-1)-(k+1) elements data[k+1], ..., data[n-1]
 - o O(n k) for removing element at index k



	Add Operation	Running Time	Remove Operation	Running Time
Beginning				
End				
Between				

10	5	8	7	1			
----	---	---	---	---	--	--	--



	Add Operation	Running Time	Remove Operation	Running Time
Beginning				
End	data.append(val)	O(1)		
Between				

10	5	8	7	1	20		
----	---	---	---	---	----	--	--



	Add Operation	Running Time	Remove Operation	Running Time
Beginning				
End	data.append(val)	O(1)	data.pop()	O(1)
Between				

10	5	8	7	1			
----	---	---	---	---	--	--	--



	Add Operation	Running Time	Remove Operation	Running Time
Beginning			data.pop(0) Del data[0]	<i>O</i> (n)
End	data.append(val)	0(1)	data.pop()	0(1)
Between				

5	8	7	1			
---	---	---	---	--	--	--



	Add Operation	Running Time	Remove Operation	Running Time
Beginning			data.pop(0) Del data[0]	<i>O</i> (n)
End	data.append(val)	0(1)	data.pop()	0(1)
Between				

5	8	7	1				
---	---	---	---	--	--	--	--



	Add Operation	Running Time	Remove Operation	Running Time
Beginning	data.insert(0, val)	<i>O</i> (n)	data.pop(0) Del data[0]	<i>O</i> (n)
End	data.append(val)	0(1)	data.pop()	0(1)
Between				

9	5	8	7	1			
---	---	---	---	---	--	--	--



	Add Operation	Running Time	Remove Operation	Running Time	
Beginning	data.insert(0, val)	<i>O</i> (n)	data.pop(0) Del data[0]	<i>O</i> (n)	
End	data.append(val) O(1)		data.pop()	0(1)	
Between			data.remove(val)	O(n)	

9 5 7 1 1



	Add Operation	d Operation Running Time		Running Time	
Beginning	data.insert(0, val)	<i>O</i> (n)	data.pop(0) Del data[0]	<i>O</i> (n)	
End	data.append(val) O(1)		data.pop()	0(1)	
Between			data.remove(val)	<i>O</i> (n)	

9	5	7	1				
---	---	---	---	--	--	--	--

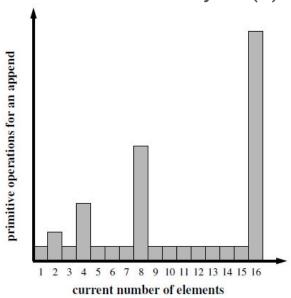


	Add Oper	ation	.			Rem Ope	nove ration		Running Time		
Beginning	data.inse	rt(0, val)	<i>O</i> (n)			data.pop(0) Del data[0]			O(n)		
End	data.appe	end(val)	O(1)		data.pop()			O(1)			
Between	data.inse val)	rt(index,	<i>O</i> (n)			data.remove(val)			<i>O</i> (n)		
9	0	5		7	1						



Amortization (Distribution) Analysis

- Operation append(value)
 - If an array is not full, copy the value into the array O(1)
 - \circ Otherwise, growing a dynamic array by copy old values to a new array O(n)
 - Does this means **append**() has O(n)?





Amortization (Distribution) Analysis

- Let S be a dynamic array with initial capacity of size 1 and double the array when it hits a capacity (full)
 - \circ An array is full when S has 2^i elements, for some integer $i \ge 0$
 - The size of the array S is 2^i
 - The cost for doubling the size is 2ⁱ coins.
- For each append operation, 3 coins are charged as a cost.
 - One is for executing append operation
 - Two is for moving elements to a new array
- If an array is not full when append, save 2 coins





