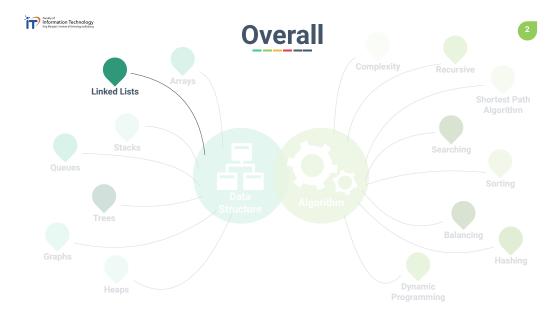


Chapter 5: Linked Lists

Dr. Sirasit Lochanachit







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Linked lists



To avoid these limitations, an alternative to array is linked list.

Array 2 7 8 4 Value 0 1 2 3 Index



- Length of array has to be pre-allocated, empty space wasted.
- Adding or removing elements between values in the array is expensive O(n)



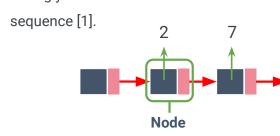
Linked Lists

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Singly Linked Lists

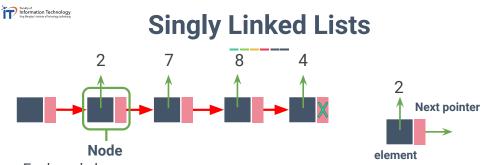
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A singly **linked list** is a collection of nodes that form a linear order of a



[1] Michael T. Goodrich et al., Data Structures and Algorithms in Python, 2013

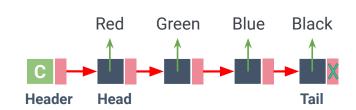




- Each node keeps:
- A reference to an object/value which is its element.
- Link/Pointer: One or more references to adjacent nodes or subsequent nodes.
 - Reference to None if there is no further node.



Singly Linked Lists



- Head and tail identify the first and last node, respectively.
- **Header** node can contain a counter to keep track the number of nodes that form a list.

Linked Lists



Singly Linked Lists

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Real-life examples of Linked Lists:







Retrieved from https://live.staticflickr.com/5610/15429943089_edc7011843_o_d.jpq CC BY 2.0 https://live.staticflickr.com/23/26472155_8cc5066b66_o_d.jpq CC BY-SA 2.0



For simplicity, the linked list illustration will embed element within the node.

Note that each node still contains a reference to the element, not the element itself directly.



Singly Linked Lists



- Traversing or link hopping is the process of moving from one node to another according to each node's subsequent pointer.
- Linked Lists provides sequential access only.
 - \circ Locating the element in a linked list requires O(n) time to traverse the list from the beginning.



Singly Linked Lists

Suppose that it takes 1 byte to store an integer.

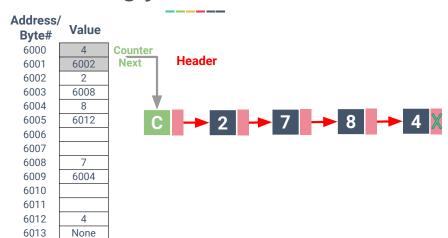


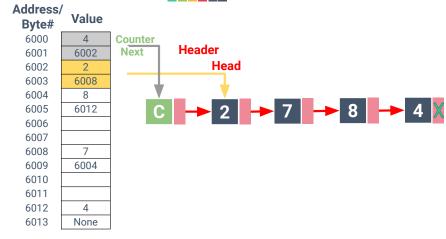




Singly Linked Lists





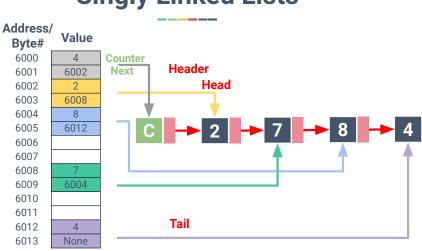


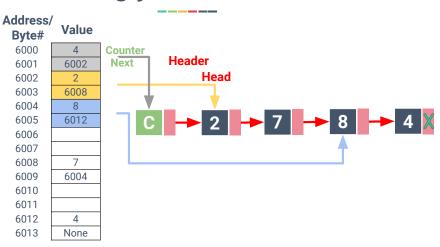
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Singly Linked Lists



Singly Linked Lists





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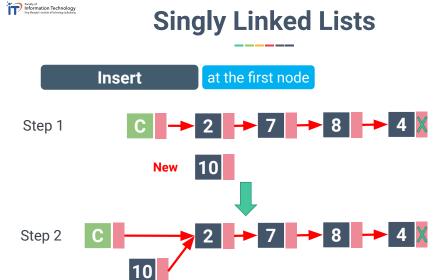
Singly Linked Lists

Step 1: Create a new node storing reference to an element.

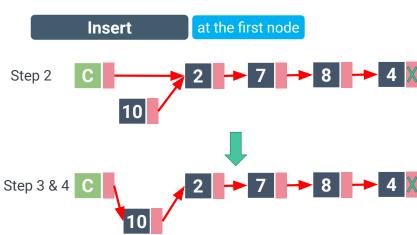
Step 2: Set new node's next pointer to the current/old head.

Step 3: Set the list's head to reference the new node.

Step 4: Increment the node count.



Singly Linked Lists





Address/

Byte#

6000

6001

6002

6003 6004

6005 6006

6007

6008

6009

6010

6011

6012

6013

Value

4

6002

6008

8

6012

6004

4

None

Step 1

Create a

new node

Singly Linked Lists

Value

6002

6008

8

6012

10

6004

4

None

Step 2, 3 & 4

Set

Pointers

Address/

Byte#

6000

6001

6002

6003

6004

6005

6006

6007

6008

6009

6010

6011

6012

6013

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Address/

Byte#

6000

6001

6002

6003

6004

6005

6006

6007

6008

6009

6010

6011

6012

6013

Value

6006

2

6008

8

6012

10

6002

4

None

Singly Linked Lists

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Insert

at the first node

Algorithm add_front(L, e):

new_node = Node(e)

new node.next = L.head

L.head = new node

L.size = L.size + 1

if L.tail == None:

L.tail = L.head

Create new node instance

Set new node's next pointer to the old head

Update the list's head to reference the new node

Increment the node count

List was empty O(1)

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Singly Linked Lists

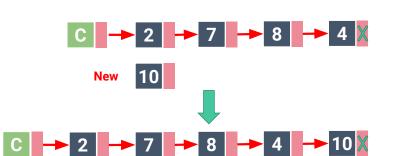
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Singly Linked Lists

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Insert

at the last node



Insert

at the last node



Step 1: Create a new node storing reference to an element.

Step 2: Set new node's next pointer to None.

O(1)

Step 3: Update the list's tail to reference the new node.

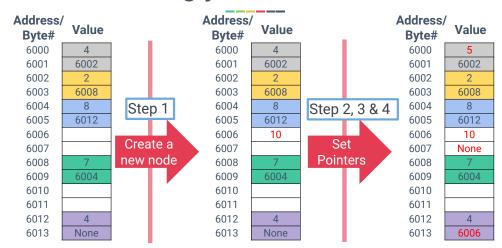
Step 4: Increment the node count.



Insert at the last node New C → 2 → 7 → 8 → 4 X Step 1 C → 2 → 7 → 8 → 4 X Step 3 & 4 C \longrightarrow 2 \longrightarrow 7 \longrightarrow 8 \longrightarrow 4 \longrightarrow 10 \times



Singly Linked Lists





Singly Linked Lists

0(1)



Singly Linked Lists

Insert

at the last node

Algorithm add_last(L, e):

else:

new_node = Node(e) # Create new node instance

new node.next = None # Set new node's next pointer to None

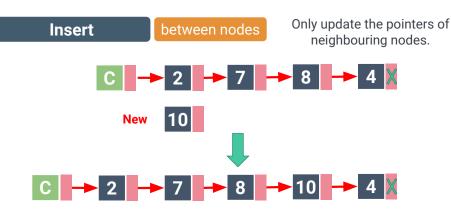
if I tail == None: # List was empty

L.head & L.tail = new node

L.tail.next = new_node # Make old tail point to new node

L.tail = new_node # Update the list's tail to reference the new node

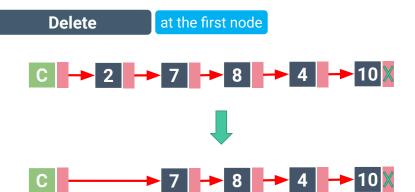
L.size = L.size + 1 # Increment the node count



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Singly Linked Lists





Step 1: Set head node's next pointer to the subsequent node.

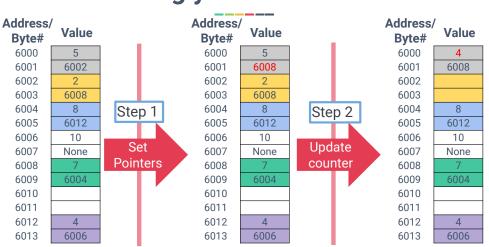
• If head is **None**, then the list is empty, return error.

Step 2: Decrement the node count.

0(1)



Singly Linked Lists



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Singly Linked Lists

Delete

at the first node

Algorithm remove_first(L):

if L.head == None: # List is empty

return Error

L.head = L.head.next # Make head point to next node or None if empty

L.size = L.size - 1 # Decrement the node count

if L.head == None: # List is empty after first node is removed

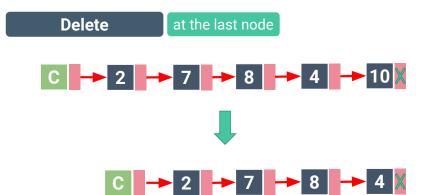
L.tail = None

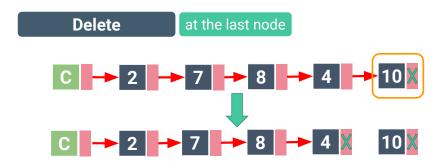
O(1)





Singly Linked Lists





Step 1: Find the next to last node, then update the next pointer to None.

Step 2: Decrement the node count.

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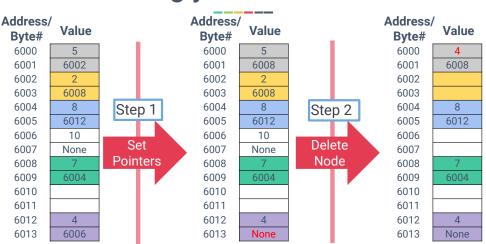
Singly Linked Lists

Deletion of the last node in Singly Linked Lists:

- No direct link from the tail node to the node before the tail.
 - There is only a link from the node before the tail to the tail node.
- To access the node before the tail, need to start from the head node and search through the list - O(n).
- To address this problem, **doubly linked list** is proposed as an alternative to singly linked list. also keeps links in backward direction.

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Singly Linked Lists





O(n) - why?





Singly Linked Lists: Stacks

Delete

at the last node

Algorithm remove_last(L):

if L.head == L.tail:

if L.head == None: return Error # List is empty

L.head & L.tail = None

else:

p = L.head # Initialise pointer to traverse the list

while p.next.next != None: # Traverse until next to last node is found

List has one node

p = p.next

p.next = None, L.tail = p # Update tail pointer

L.size = L.size - 1 # Decrement the node count O(n)



How to Implement a Stack?

Array!!

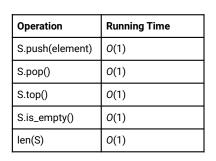
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Linked Lists!!

• Singly Linked Lists

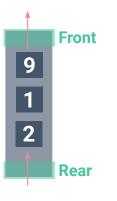


Asymptotic Performance





Singly Linked Lists: Queues



How to Implement a Queue?

Array!!

and

Linked Lists!!

• Singly Linked Lists





Asymptotic Performance

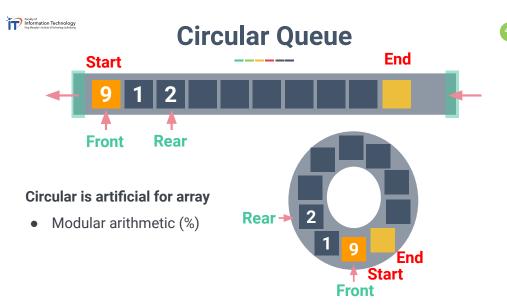
Operation	Running Time
Q.enqueue(e)	0(1)
Q.dequeue()	0(1)
Q.first()	0(1)
Q.is_empty()	0(1)
len(Q)	0(1)





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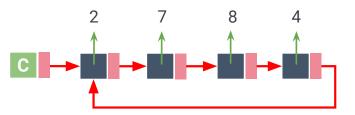


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Circularly Linked Lists

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A **circularly linked list** adds the notion of having the tail of the list to point back to the head of the list as the next node.



Circularly Linked Lists



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Circularly Linked Lists

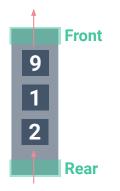
Address/	
Byte#	Value
6000	4
6001	6002
6002	2
6003	6008
6004	8
6005	6012
6006	
6007	
6008	7
6009	6004
6010	
6011	
6012	4
6013	6002

Suppose that it takes 1 byte to store an integer.





Circularly Linked Lists: Queues



How to Implement a Queue?

Array!!

and

Linked Lists!!

- Singly Linked Lists
- Circularly Linked Lists

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Asymptotic Performance

Operation	Running Time
Q.enqueue(e)	0(1)
Q.dequeue()	0(1)
Q.first()	0(1)
Q.is_empty()	0(1)
len(Q)	0(1)

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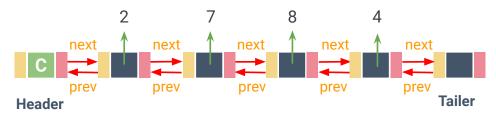
Singly Linked List

Circularly Linked List

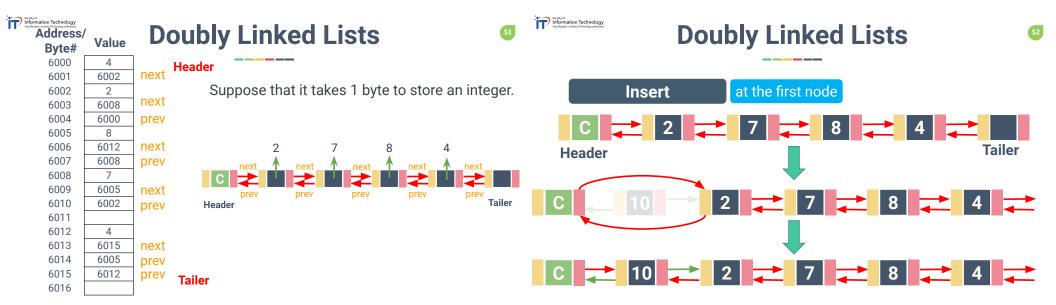
Doubly Linked List

Doubly Circularly Linked List

To add more symmetry to the list, **doubly linked lists** allow each node to keep a reference to the node <u>before</u> it and a pointer to the node <u>after</u> it.



[1] Michael T. Goodrich et al., Data Structures and Algorithms in Python, 2013



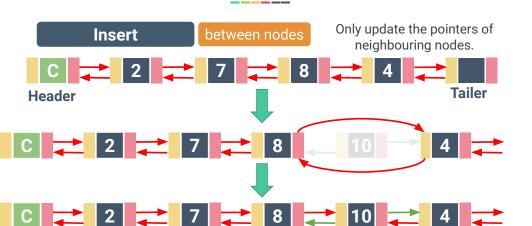


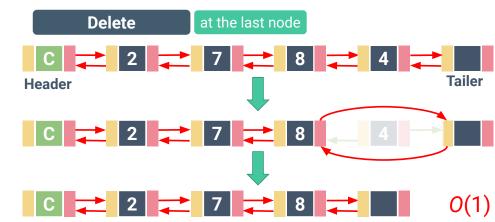
Doubly Linked Lists

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Doubly Linked Lists

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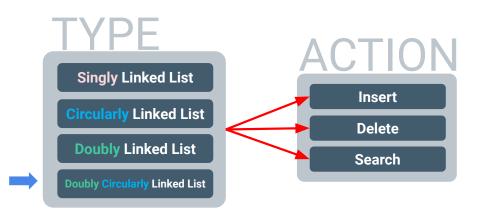


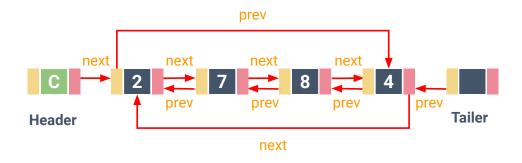
Linked Lists

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Doubly Circularly Linked Lists

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Linked Lists







Linked list properties:

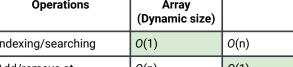
- Each node contains an element and a pointer(s) to the next node (and previous node).
- Sequential access only: nodes are read from the beginning.
 - Not convenient to have an index, unlike array-based sequences.
- No pre-allocated fixed size of memory, resizeable.
- Insertion and deletion operations are more efficient compared to array.
 - Take O(1) constant time to add and remove elements at any part in linked lists.

Linked list's limitations:

- Accessing the data/node in lists takes linear time O(n)
 - To find the item or node at certain location, linked list has to start from the first node and traversing until the target is found.
 - For example, find the 10th node, has to traversing 10 times.
 - Unable to perform binary search.
- Use extra storage than the array to keep next pointers/references.
 - Impractical for storing small data such as characters.



Linked Lists vs Arrays



Operations	(Dynamic size)	LINKEG LIST
Indexing/searching	0(1)	O(n)
Add/remove at beginning	O(n)	0(1)
Add/remove at end	0(1)	O(1) when last element is known $O(n)$ when last element is unknown
Add/remove in between	O(n)	0(1)
Wasted memory space (average)	O(2n)	O(2n) - Singly linked list or O(3n) - Doubly linked list



Individual Assignment



- Assignment#3: Queues
- Due 09.00 am, Tuesday 01/09/2020.
- Submission
 - Email: sirasit@it.kmitl.ac.th
 - Paper: in classroom next week
- Can be either written by hand or typing.