

$$H.9 \quad a) \quad \Delta_2^\mu(p', p) = \alpha (\gamma^\mu + \beta (p+p')^\mu)$$

$$\alpha = \frac{2m^2}{(d-2)q^2(q^2-4m^2)} \quad , \quad \beta = \frac{(d-2)q^2+4m^2}{2m(q^2-4m^2)}$$

$$\begin{aligned} & \text{Tr} [\not{p}' \Delta_2^\mu(p', p) \not{p}] \\ &= \text{Tr} \left\{ (\not{p} + m) \alpha (\gamma^\mu + \beta (p+p')^\mu) (\not{p}' + m) \left[\gamma_\mu F_1 + \frac{i\sigma_{\mu\nu}}{2m} (p'-p)^\nu F_2 \right] \right\} \\ &= \alpha \text{Tr} \left[(\not{p} + m) (\gamma^\mu + \beta (p+p')^\mu) (\not{p}' + m) \frac{i\sigma_{\mu\nu}}{2m} (p'-p)^\nu F_2 \right] \quad \begin{matrix} \text{odd \# of } \gamma \\ \rightarrow \end{matrix} \quad (?) \\ & \quad \underbrace{\gamma^\mu (\not{p} + m) (\not{p}' + m)}_{\gamma^\mu (\not{p} + m) (\not{p}' + m) \stackrel{tr}{=} \gamma^\mu \not{p} m + \gamma^\mu \not{p}' m} \\ &= \alpha \text{Tr} \left\{ [m \gamma^\mu (\not{p} + \not{p}') + \beta (p+p')^\mu (\not{p} \not{p}' + m^2)] \frac{i\sigma_{\mu\nu}}{2m} (p'-p)^\nu F_2 \right\} \\ &= \frac{-\alpha}{4m} (p'-p)^\nu F_2 \cdot \text{Tr} \left\{ [m \gamma^\mu (\not{p} + \not{p}') + \beta (p+p')^\mu (\not{p} \not{p}' + m^2)] \cdot (\gamma_\mu \delta_\nu - \gamma_\nu \gamma_\mu) \right\} \end{aligned}$$

$$\begin{aligned} \text{Tr} &= m(p+p')_\alpha \text{Tr} [\gamma^\mu \gamma^\alpha (\gamma_\mu \gamma_\nu - \gamma_\nu \gamma_\mu)] \\ & \quad + \beta (p'+p)^\mu \left\{ p_\alpha p'_\beta \text{Tr} [\gamma^\alpha \gamma^\beta (\gamma_\mu \gamma_\nu - \gamma_\nu \gamma_\mu)] + m^2 \text{Tr} [\gamma_\mu \gamma_\nu - \gamma_\nu \gamma_\mu] \right\} \\ &= m(p+p')_\alpha [-4(d-2)g_\nu^\alpha - 4d g_\nu^\alpha] + \beta (p'+p)^\mu \{ 4p_\alpha p'_\beta (g^{\alpha\beta} g_{\mu\nu} - g_\mu^\alpha g_\nu^\beta \\ & \quad + g_\nu^\alpha g_\mu^\beta) - 4p_\alpha p'_\beta (g^{\alpha\beta} g_{\nu\mu} - g_\nu^\alpha g_\mu^\beta + g_\mu^\alpha g_\nu^\beta) \} \\ &= m(p+p')_\alpha \cdot (-8)(d+1) g_\nu^\alpha + 8\beta (p'+p)^\mu [p_\alpha p'_\beta (g_\nu^\alpha g_\mu^\beta - g_\mu^\alpha g_\nu^\beta)] \\ &= -8(d+1)m(p+p')_\nu + 8\beta (p'+p)^\mu (p_\nu p'_\mu - p_\mu p'_\nu) \\ & \quad = \underline{p'^\mu p_\nu} + \underline{p^\mu p'_\nu} - \underline{p'^\mu p_\mu p'_\nu} - \underline{p^\mu p_\mu p'_\nu} \\ &= m^2(p-p')_\nu + p^\mu p'_\mu (p-p')_\nu \\ &= (m^2 + p^\mu p'_\mu) (p-p')_\nu \end{aligned}$$

$$\begin{aligned}
 &= F_2 \frac{-\alpha}{4m} (p' - p)^\nu \left\{ -8(d+1)m (p + p')_\nu + 8\beta (m^2 + p^\mu p'_\mu) (p - p')_\nu \right\} \\
 &\quad \underbrace{\hspace{10em}}_{= q^2} \\
 &\quad = (p' - p) \cdot (p + p') \\
 &\quad = 2m^2
 \end{aligned}$$

$$\begin{aligned}
 &= F_2 \frac{-\alpha}{4m} \left[-8(d+1)m \cdot 2m^2 + 8\beta (m^2 + p \cdot p') q^2 \right] \\
 &\quad \underbrace{\hspace{10em}}_{= -\alpha \frac{1}{4m} \cdot \left[-16(d+1)m^3 + 8(m^2 + p \cdot p') q^2 \frac{(d-2)q^2 + 4m}{2m(q^2 - 4m^2)} \right]}
 \end{aligned}$$