# **Quantum Field Theory**

July 16, 2019

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## 1 Classical field theory

## 1.1 Field theory in continuum

### **Euler-Lagrange-equation**

$$\partial_{\mu} \left( \frac{\partial \mathcal{L}}{\partial (\partial_{\mu} \phi)} \right) - \frac{\partial \mathcal{L}}{\partial \phi} = 0 \tag{1.1.1}$$

momentum density

$$\pi(x) = \frac{\partial \mathcal{L}}{\partial \dot{\phi}(\mathbf{x})} \tag{1.1.2}$$

Hamiltonian density

$$\mathcal{H}(\phi(\mathbf{x}), \pi(\mathbf{x})) = \pi(\mathbf{x})\dot{\phi}(\mathbf{x}) - \mathcal{L}(\phi, \partial_{\mu}\phi)$$
(1.1.3)

### 1.2 Noether Theorem

If a Lagrangian field theory has an infinitisimal symmetry, then there is an associated current  $j^{\mu}$ , which is conserved.

$$\partial_{\mu}j^{\mu} = 0 \tag{1.2.1}$$

$$j^{\mu} = \frac{\partial \mathcal{L}}{\partial(\partial_{\mu}\phi)} \Delta \phi - X^{\mu} \tag{1.2.2}$$

### **Energy-momentum tensor (stress-energy tensor)**

Asymmetric version

$$\Theta_{\nu}^{\mu} = \frac{\partial \mathcal{L}}{\partial(\partial_{\mu}\phi)} \partial_{\nu}\phi - \delta_{\nu}^{\mu}\mathcal{L}$$
 (1.2.3)

General version

$$T^{\mu\nu} = \Theta^{\mu\nu} + \partial_{\lambda} f^{\mu\nu\lambda} \tag{1.2.4}$$

with  $f^{\lambda\mu\nu} = -f^{\mu\lambda\nu}$  or  $\partial_{\mu}\partial\nu f^{\lambda\mu\nu} = 0$