a)
$$L = \frac{1}{2} (\partial_{m} \Phi)^{2} - \frac{1}{2} M^{2} \Phi^{2} + \frac{1}{2} (\partial_{m} \Phi)^{2} - \frac{1}{2} m^{2} \Phi^{2} - \frac{M}{2} \Phi \Phi^{2}$$

$$H_{int}(X) = \frac{M}{2} \Phi(X) \Phi(X)$$

$$\Phi(X) = \int \frac{d^{3}k}{(2\lambda)^{3} \int_{2kk}} (e^{-ik\cdot X} a_{k} + e^{+ik\cdot X} a_{k}^{+}), \quad k^{\circ} = W_{k} = \sqrt{k^{2} + m^{2}}$$

$$\Phi(X) = \int \frac{d^{3}k}{(2\lambda)^{3} \int_{2kk}} (e^{-ik\cdot X} b_{k} + e^{+ik\cdot X} b_{k}^{+}), \quad k^{\circ} = E_{k} = \sqrt{k^{2} + m^{2}}$$

$$= \Phi(X) \Phi(Y) = D_{T}^{m} (X - Y) = \int \frac{d^{4}q}{(2\lambda)^{4}} \frac{i}{p^{2} - m^{2} + iE} e^{-iq(X - Y)}$$

$$= \Phi(X) \Phi(Y) = D_{T}^{m} (X - Y)$$

$$= (-i M) \int d^{4}X$$

$$= interaction can happen at any space-time $\frac{1}{2}$ takes into account permutations of 2π fields.$$

at the constraction with the incoming particle.

(0| 0(x) | Pa) = (0| 0(x) | Pa) = e-ip.x

b)
$$S = \langle \vec{p}_{1} \vec{p}_{2} | T \exp(-i \int d^{4}x \operatorname{Hint}(x)) | \vec{p}_{A} \rangle$$

$$S = 1 + i T, \quad T = (2Z)^{4} S^{4} (p_{1} + p_{2} - p_{A}) M$$

$$S^{(4)} = \langle \vec{P}_{A} \vec{P}_{1} | \vec{P}_{A} \rangle = \int 8 \omega_{P}, \omega_{P}, \vec{P}_{P}, \vec{P}_{A} \langle 0 | a\vec{P}_{A} a\vec{P}_{A}, b\vec{P}_{A} | 10 \rangle$$

$$\propto \langle 0 | b\vec{P}_{A} a\vec{P}_{A} a\vec{P}_{A} | 10 \rangle$$

$$= \frac{1}{2} \int d^{4}x \langle \vec{P}_{1} \vec{P}_{2} | T C - i \frac{2}{3} \phi \omega_{P} \phi \omega_{P} \vec{P}_{A} \rangle | \vec{P}_{A} \rangle$$

$$= \frac{-iM}{2} \int d^{4}x \langle \vec{P}_{1} \vec{P}_{1} | \phi (x) \phi (x) \vec{P}_{1} (x) | \vec{P}_{A} \rangle$$

$$+ \frac{-iM}{2} \int d^{4}x \langle \vec{P}_{1} \vec{P}_{1} | \phi (x) \phi (x) \vec{P}_{1} (x) | \vec{P}_{A} \rangle$$

$$= -iM \int d^{4}x e^{ix \langle \vec{P}_{1} \vec{P}_{1} | \phi (x) \phi (x) \vec{P}_{1} (x) | \vec{P}_{A} \rangle}$$

$$= -iM \int d^{4}x e^{ix \langle \vec{P}_{1} \vec{P}_{1} | \phi (x) \phi (x) \vec{P}_{1} (x) | \vec{P}_{A} \rangle}$$

$$= -iM \int d^{4}x e^{ix \langle \vec{P}_{1} \vec{P}_{1} | \phi (x) \phi (x) \vec{P}_{1} (x) | \vec{P}_{A} \rangle}$$

$$= -iM \int d^{4}x e^{ix \langle \vec{P}_{1} \vec{P}_{1} | \phi (x) \phi (x) \vec{P}_{1} (x) | \vec{P}_{1} \rangle}$$

$$= -iM \int d^{4}x e^{ix \langle \vec{P}_{1} \vec{P}_{1} | \phi (x) \phi (x) \vec{P}_{1} (x) | \vec{P}_{1} \rangle}$$

$$= -iM \int d^{4}x e^{ix \langle \vec{P}_{1} \vec{P}_{1} | \phi (x) \phi (x) \vec{P}_{1} (x) | \vec{P}_{1} \rangle}$$

$$= -iM \int d^{4}x e^{ix \langle \vec{P}_{1} \vec{P}_{1} | \phi (x) \phi (x) \phi (x) \vec{P}_{1} | \vec{P}_{1} \rangle}$$

$$= -iM \int d^{4}x e^{ix \langle \vec{P}_{1} \vec{P}_{1} | \phi (x) \phi (x) \vec{P}_{1} | \vec{P}_{1} \rangle}$$

$$= -iM \int d^{4}x e^{ix \langle \vec{P}_{1} \vec{P}_{1} | \phi (x) \phi (x) \vec{P}_{1} | \vec{P}_{1} \rangle}$$

$$= -iM \int d^{4}x e^{ix \langle \vec{P}_{1} \vec{P}_{1} | \phi (x) \phi (x) \vec{P}_{1} | \vec{P}_{1} \rangle}$$

$$= -iM \int d^{4}x e^{ix \langle \vec{P}_{1} \vec{P}_{1} | \phi (x) \phi (x) \vec{P}_{1} | \vec{P}_{1} \rangle}$$

$$= -iM \int d^{4}x e^{ix \langle \vec{P}_{1} \vec{P}_{1} | \phi (x) \phi (x) \vec{P}_{1} | \vec{P}_{1} \rangle}$$

$$= -iM \int d^{4}x e^{ix \langle \vec{P}_{1} \vec{P}_{1} | \phi (x) \phi (x) \vec{P}_{1} | \vec{P}_{1} \rangle}$$

$$= -iM \int d^{4}x e^{ix \langle \vec{P}_{1} \vec{P}_{1} | \phi (x) \phi (x) \vec{P}_{1} | \vec{P}_{1} \rangle}$$

$$= -iM \int d^{4}x e^{ix \langle \vec{P}_{1} \vec{P}_{1} | \phi (x) \phi (x) \vec{P}_{1} | \vec{P}_{1} \rangle}$$

$$= -iM \int d^{4}x e^{ix \langle \vec{P}_{1} \vec{P}_{1} | \phi (x) \phi (x) \vec{P}_{1} | \vec{P}_{1} \rangle}$$

$$= -iM \int d^{4}x e^{ix \langle \vec{P}_{1} \vec{P}_{1} | \phi (x) \phi (x) \vec{P}_{1} | \phi (x) \phi (x)$$

$$=\frac{1}{32\pi}\frac{h}{M}\sqrt{1-\frac{4m^2}{M^2}}$$

e) $S^{(3)} = \frac{1}{3!} \left(\frac{-i\mu}{2}\right)^3 \int d^4x d^4y d^4z$ be aware of φ and φ $\langle P_1 P_2 | T [\underline{\partial}(x) \phi(x) \phi(x) \underline{\Phi}(y) \phi(y) \underline{\Phi}(y) \underline{\Phi}(x) \phi(x) \varphi(x) | P_A \rangle$

$$e^{-il_{A}\frac{\pi}{2}}$$

$$\int \frac{d^{4}Q}{(2\pi)^{4}} \frac{ie^{-iQ(x-y)}}{Q^{2}-m^{2}+i\xi} = (-i\mu)^{3} \int d^{4}x d^{4}y d^{4}x \frac{d^{4}f_{1}}{(2\pi)^{4}} \frac{d^{4}f_{2}}{(2\pi)^{4}} \times \frac{d^{4}Q}{(2\pi)^{4}} e^{-i\xi(P_{1}-P_{1}-P_{2})} e^{+ix(P_{1}-f_{1}-Q)} e^{+iy(P_{2}-f_{2}+Q)} \times \frac{i}{P_{1}+m^{2}+i\xi} = \frac{i}{P_{2}-m^{2}+i\xi} \frac{i}{Q^{2}-m^{2}+i\xi} = \frac{i}{Q^{2}-m^{2}+i\xi} \frac{i}{Q^{2}-m^{2}+i\xi} = \frac{i}{Q^{2}-m^{2}+i\xi} \frac{i}{Q^{2}-m^{2}+i\xi} = \frac{i}{Q^{2}-m^{2}+i\xi} \frac{i}{Q^{2}-m^{2}+i\xi} = \frac{$$