3. a)
$$\int d^{4}x \, e^{ipx} \langle \Omega | T \, \phi(x) \, \phi(i) | \Omega \rangle$$

$$= - + - 0 - + - 0 - 0 - + - 0$$

$$= D_{F}^{(0)}(p^{2}) + D_{F}^{(0)}(p^{3}) \left(-i\sum(p^{2})\right) D_{F}^{(0)}(p^{2}) + \cdots$$

$$= D_{F}^{(0)}(p^{3}) \frac{1}{1 + i\sum(p^{2})D_{F}^{(0)}(p^{3})} = \frac{i}{p^{3} - m_{0}^{2}} \frac{1}{1 + i\sum(p^{3})\frac{i}{p^{2} - m_{0}^{2}}}$$

$$= \frac{i}{p^{3} - m_{0}^{3} - \sum(p^{3})}$$

Expand
$$\Sigma(p^2) = \Sigma(m^2) + (p^2 - m^2) \Sigma'(m^2) + (p^2 - m^2) \widetilde{\Sigma}(p^2)$$

with $m_0^2 + \Sigma(m^2) = m^2$, $\widetilde{\Sigma}(m^2) = 0$

$$= \sum_{j=1}^{\infty} m_0^2 + \Sigma(p^2) = m_0^2 + \Sigma(m^2) + \cdots$$

$$= m^2 + (p^2 - m^2) \Sigma'(m^2) + (p^2 - m^2) \widetilde{\Sigma}(p^2)$$

$$= \frac{i}{p^2 - m^2} \frac{1}{1 - \Sigma'(m^2) - \widetilde{\Sigma}(p^2)}$$

$$= \frac{i}{p^2 - m^2} \frac{1}{1 - \Sigma'(m^2) - \widetilde{\Sigma}(p^2)} = \frac{i}{p^2 - m^2} + Regular$$

b)
$$\int_{int} = -\frac{\lambda}{3!} \phi^{3}$$
 -> vertex: $-i\lambda$

$$-i\sum_{2} (\rho^{2}) = \frac{(-i\lambda)^{2}}{2} \int \frac{d^{3}k}{(2\pi)^{3}} \frac{i}{(\rho + k)^{2} - mo^{2} + i\sum_{k} \frac{i}{(-k)^{2} - m$$

$$= \frac{(\lambda^{2} - m_{o}^{2} + \chi)^{2} + \chi^{2} + \chi^{2}}{1 + m_{o}^{2} + \chi^{2}}$$

$$= (k + p \chi)^{2} - p^{2} \chi (\chi - 1) - m_{o}^{2}$$

$$= (k + p \chi)^{2} - p^{2} \chi (\chi - 1) - m_{o}^{2}$$

$$= \frac{\lambda^{2}}{2(2\pi)^{4}} \int_{0}^{4} d\chi \int d^{4}q \frac{1}{(q^{2} - \Delta)^{2}}$$
Which protein: $q_{1} \rightarrow i q_{0} g_{0}$, $q_{1} = i + j = 1$ and $q_{2} = i + j = 1$ and $q_{3} = i + j = 1$ and $q_{4} = i + j = 1$ and $q_{5} = i + j$

$$= \frac{i\lambda^{2}}{2(2\pi)^{d}} \int_{0}^{1} dx \int d^{d} f = -2 \frac{1}{(2\epsilon^{2} - \delta)^{3}} \cdot \chi(\chi - 1)$$

$$= \frac{-i\lambda^{2}}{(2\pi)^{d}} \int_{0}^{1} dx \quad \chi(\chi - 1) \cdot \frac{1}{(4\pi)^{d/2}} \frac{\Gamma(3 - \frac{d}{2})}{\Gamma(3)} \Delta^{\frac{d}{2} - 3}$$

$$= \frac{-i\lambda^{2}}{(2\pi)^{d}} \frac{1}{2(4\pi)^{\frac{d}{2}}} \int_{0}^{1} dx \quad \chi(\chi - 1) \cdot \left[\int_{0}^{2} \chi(\chi - 1) + m^{2} \right]^{\frac{d}{2} - 3}$$

$$A + \int_{0}^{2} -m^{2}, \quad m^{2} - m^{2} = O(\lambda^{2})$$

$$\chi \int_{0}^{1} d\chi \quad \frac{\chi(\chi - 1)}{\chi^{2} - \chi + 1} \frac{1}{m^{2}}$$

2.
$$\mathcal{L} = \overline{Y}(i\partial - m)Y + \overline{X}(i\partial - m)X + \frac{1}{2}(\partial^{n}\phi\partial_{n}\phi - M^{2}\phi^{2})$$

 $-g\overline{Y}i\partial^{5}Y\phi - g\overline{X}i\partial^{5}X\phi$

M> m

$$\begin{cases} \mathcal{A}^{(n)}(p) + \overline{\mathcal{A}^{(5)}}(\widehat{p}) \longrightarrow \mathcal{X}^{(1)}(k) + \overline{\mathcal{X}^{(F)}}(\overline{k}) \\ pp \longrightarrow nn \end{cases}$$

$$a) \qquad -ig \ i \, \gamma^s = g \, \gamma^s \qquad ; \qquad -ig \ i \, \gamma^r = \overline{g} \, \sigma^s$$

$$i\mathcal{M} = \overline{\mathcal{V}}_{p}^{(h)}(\overline{p}) (g \gamma^{s}) u_{p}^{(f)}(\overline{p}) \frac{i}{(P_{r+1}P_{r})^{2} - \mathcal{M}^{2} + i\varepsilon} \overline{\mathcal{U}}_{n}^{(s)}(k) (g \gamma^{s}) \mathcal{V}_{n}^{(s)}(\overline{k})$$

$$\leftarrow --(?)$$

c)
$$IMI^{2} = \frac{1}{4} \sum_{spin} (g \overline{g})^{2} \overline{v}_{p}^{(i)}(\overline{p}) \gamma^{5} u_{p}^{cd}(\overline{p}) \frac{1}{s-u^{2}} \overline{u}_{n}^{(s)}(k) \gamma^{5} v_{n}^{(s)}(\overline{k})$$

for be aware

$$\overline{v}_{n}^{(s)}(\overline{k}) \gamma^{o} \gamma^{5} \gamma^{o} u_{n}^{(s)}(k) \frac{1}{s-u^{2}} \overline{u}_{p}^{(i)}(\overline{p}) \gamma^{5} v_{p}^{(i)}(\overline{p})$$

$$= \frac{(g \overline{g})^{2}}{4(s-u^{2})^{2} r, r'} tr[(\overline{p}-m)(-p'+m)) tr[(\overline{k}-\mu)(+k'+\mu)]$$

$$= tr(\overline{p}+u^{2}) = tr(\overline{k}k+\mu^{2})$$

$$= 4(\overline{p}-p+u^{2}) = 4(\overline{k}\cdot k+\mu^{2})$$

$$=\frac{(\mathfrak{J}\widehat{\mathfrak{J}})^2}{(s-\mu^2)^2} S^2$$

with
$$S^2 = 2m^2 + p \cdot \vec{p} = 2m^2 + k \cdot \vec{k}$$

d)
$$\frac{d\sigma}{d\Omega} = \frac{1}{64\pi^2 S} \frac{1\overline{I}_{11}}{|\overline{I}_{11}|} \frac{1}{|\overline{M}_{1}|^2}$$

$$= \frac{1}{64\pi^2 S} \frac{JS'}{JS'} \left(\frac{9\overline{9}}{S-M^2}\right)^2 S^2$$

$$= \frac{1}{64\pi^2} \left(\frac{9\overline{9}}{S-M^2}\right)^2 S$$

$$S = \frac{1}{64\pi^2 S} \frac{1\overline{I}_{11}}{S-M^2} \frac{1}{S} \frac{1}{S}$$

S < 4 µ², not able so produce nã - pair.

e)
$$Y^{(i)}(p) + X^{(i)}(\bar{k}) \rightarrow Y^{(3)}(\bar{p}) + X^{(i)}(k)$$
 $\bar{S} = (p+\bar{k})^2$
 $\bar{t} = (p-\bar{p})^2$
 $\bar{u} = (p-\bar{k})^2$

$$iM = \overline{u_{n}}^{(s)}(k) \left(\overline{g} \, 8^{s}\right) u_{n}^{(s)}(\overline{k}) \frac{-ig_{n}}{(p+\overline{k})^{2}-M^{2}} \overline{u_{p}}^{(s)}(\overline{p}) \left(g \, 8^{s}\right) u_{p}^{(s)}(p)$$

$$= \overline{gg} \overline{u_{n}}^{(s)}(k) \, 8^{s} \, u_{n}^{(s)}(\overline{k}) \, \overline{u_{p}}^{(s)}(\overline{p}) \, 8^{s} \, u_{p}^{(s)}(p)$$

$$= \frac{1}{4} \left(\frac{99}{5-m^2} \right)^2 \sum_{k} \bar{u}_{k}^{(5)}(k) \gamma^{5} u_{k}^{(5)}(\bar{p}) \gamma^{5} u_{p}^{(5)}(\bar{p}) \gamma^{5} u_{p}^{(5)}(\bar{p}) \bar{u}_{k}^{(5)}(\bar{p}) \bar{u}_{k}^{(5)}(\bar{p}) \bar{u}_{k}^{(5)}(\bar{p}) \bar{u}_{k}^{(5)}(\bar{k}) \gamma^{5} u_{p}^{(5)}(\bar{p}) \bar{u}_{k}^{(5)}(\bar{k}) \gamma^{5} u_{p}^{(5)}(\bar{k}) \gamma^{5} u_{p}^{(5)}(\bar{p}) \bar{u}_{k}^{(5)}(\bar{k}) \gamma^{5} u_{p}^{(5)}(\bar{p}) \bar{u}_{k}^{(5)}(\bar{k}) \gamma^{5} u_{p}^{(5)}(\bar{k}) \gamma^{5} u_{p}^$$

$$= \frac{1}{4} \left(\frac{99}{3-m^2} \right)^2 tr \left[(k+\mu)(y^5)^2 (-k+\mu) \right] tr \left[(p+m)(-p+m) \right]$$

$$= \frac{1}{4} \left(\frac{99}{3-m^2} \right)^2 tr \left[-k + \mu^2 \right] tr \left[-p + m^2 \right]$$

$$= \frac{1}{4} \left(k \cdot k - \mu^2 \right) = 4 \cdot (p \cdot p - m^2)$$

$$= \frac{4|9\bar{9})^{2}}{(\hat{s}-m^{2})} (k \cdot \bar{k}-m^{2}) (P - \bar{P}-m^{2})$$

$$\left(\begin{array}{c} \widetilde{t} = (p - \overline{p})^2 = 2m^2 - 2p\overline{p} \\ = (k - \overline{k})^2 = 2m^2 - 2k\overline{k} \end{array}\right)$$

$$= \left(\frac{9\bar{g}}{\bar{s}-\bar{m}}\right)^2 \tilde{t}^2$$