a) Renormalized P.7
$$\phi = \sqrt{z} \phi_r$$

$$L = \frac{z}{z} (\partial_{\mu} \phi_r)^2 - \frac{z^2 m^2}{z^2} \phi_r^2 - \frac{z^2 \lambda_0}{4!} \phi_r^4$$

$$= \frac{1}{z} (\partial_{\mu} \phi_r)^2 - \frac{m^2}{z} \phi_r^2 - \frac{\lambda}{4!} \phi_r^4 + \frac{S^2}{z} (\partial_{\mu} \phi_r)^2 - \frac{Sm}{z} \phi_r^2 - \frac{S\lambda}{4!} \phi_r^4$$

$$\begin{cases} St = 2-1 \\ Sm = 2mo^2 - m^2 \\ S\lambda = \lambda_0 t^2 - \lambda \end{cases}$$

$$\frac{P}{P^{2}-m^{2}+i\varepsilon} = -i\lambda \qquad = -i\lambda$$

I -> internal lines

1 vertex
$$\longrightarrow$$
 4 lines
$$D = 4L - 2I \qquad \qquad \int \frac{d^4 p}{p^2 - m^2}$$

$$= 4(1 - V + 1) - 2I$$

$$= 4 - E$$

d) $\phi \rightarrow -\phi$, amplitudes with odd ff of external lines vanish

e) [L] = d, $[\partial_n \phi] (\partial^n \phi) = 1$ $d = [(\partial_n \phi)(\partial^n \phi)] = 2(1+[\phi]) (= 1) (\phi) = \frac{d}{2} - 1$

$$d = [\lambda_0 \phi^4] = 4[\phi] + [\lambda_0] = 2d - \varphi + [\lambda_0]$$

à is dimensionless

f) divergences => poles in {\frac{1}{\xi}}

MS scheme; only absorb poles

$$iM = \sum_{i} \sum_{j} + \sum_{i} + \sum_{j} + \sum_{i} \sum_{j} + \sum_{i} \sum_{j} + \sum_{i} \sum_{j} + \sum_{i} \sum_{j} \sum_{j} \sum_{j} \sum_{i} \sum_{j} \sum_{j} \sum_{j} \sum_{j} \sum_{i} \sum_{j} \sum_{j}$$

+

(must be finite)

S-channel diagram with incoming momenta Pr, Pr

$$= (-i\lambda)^{2} \frac{1}{2} \int \frac{d^{9}k}{(2\pi)^{9}} \frac{i}{k^{2}-m^{2}+i\xi} \frac{i}{(k+\beta_{1}+\beta_{2})^{2}-m^{2}+i\xi} =: A(S)$$
Symm. factor

iM = -i2 + A(s) + A(t) + A(u) - i8x

expand A(s) around A(0)

$$A(S) = A(0) + \frac{\partial}{\partial l^{2}} A(l^{2}) \frac{\partial}{\partial l^{2}} P_{n}^{2}$$

$$divergent$$

$$l$$

$$A(S) \sim A(0) = \lambda^{2} \ln^{8-2} d \frac{1}{2} \int \frac{d^{2}k}{(2\pi)^{2}} \frac{1}{(k^{2}-m^{2}+i\xi)^{2}}$$

$$= \lambda^{2} \mu^{8-2d} \frac{1}{2} \frac{i}{(4\pi)^{d/2}} \frac{P(\frac{4-d}{2})}{P(2)} m^{d-4}$$

$$d=4-\epsilon \sum_{i=1}^{2} \lambda^{2} \frac{1}{2} \frac{i}{(4\pi)^{2-\frac{2}{2}i}} P(\frac{\epsilon}{2}) m^{-\epsilon}$$

$$A(s) \sim \lambda^2 \frac{i}{(4\pi)^2} \frac{1}{\xi}$$

$$M = \frac{\lambda^2}{(4\pi)^2} = \frac{1}{\xi} \cdot 3 - \delta \lambda$$
 = ignore tree level contribution

in order to keep \mathcal{U} finite $\rightarrow S\lambda = \lambda^2 \frac{3}{76\lambda^2} \frac{1}{\varepsilon}$