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"""5. a. Determine the greatest common divisors of elements from a list.
(recursive)
b. Insert an element on the n-position in a list. (recursive)"""

class Node:
    def __init__(self, value):
        self.value = value
        self.next = None

class List:
    def __init__(self):
        self.head = None

def createList():
    list = List()
    list.head = createList_rec()
    return list

def createList_rec():
    x = int(input("x = "))
    if x == 0:
        return None
    else:
        node = Node(x)
        node.next = createList_rec()
        return node

def gcd(a, b):
    if b == 0:
        return a
    else:
        return gcd(b, a % b)

def lcm(a, b):
    x = gcd(a, b)
    p = a * b
    return p/x

def lcmList_rec(node):
    if node is None:
        return 0
    elif node.next is None:
        return node.value
    else:

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        return lcm(node.value, lcmList_rec(node.next))

def gcdList_rec(node):
    if node is None:
        return 0
    elif node.next is None:
        return node.value
    else:
        return gcd(node.value, gcdList_rec(node.next))

def insert_pos_rec(node, value, pos):
    if pos == 0:
        new_node = Node(value)
        new_node.next = node
        return new_node
    elif node is None:
        return None
    else:
        node.next = insert_pos_rec(node.next, value, pos - 1)
        return node

def insert_pos(list, value, pos):
    list.head = insert_pos_rec(list.head, value, pos)

def printList(list):
    node = list.head
    while node is not None:
        print(node.value)
        node = node.next

def menu():
    print("1. Create list")
    print("2. Determine GCD of list elements")
    print("3. Insert element at n-position")
    print ("4. Print list")
    print("5. LCM")
    print("6. Exit")
    list = None
    while True:
        choice = int(input("Choice: "))
        if choice == 1:
            list = createList()
        elif choice == 2:
            if list is None:
                print("List is empty")
            else:

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        print("GCD:", gcdList_rec(list.head))
    elif choice == 3:
        if list is None:
            print("List is empty")
        else:
            value = int(input("Value to insert: "))
            pos = int(input("Position: "))
            insert_pos(list, value, pos)
            printList(list)
    elif choice == 4:
        printList(list)
    elif choice == 5:
        print("LCM:", int(lcmList_rec(list.head)))
    elif choice == 6:
        break
    else:
        print("Invalid choice")

if __name__ == "__main__":
    menu()

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- a) Let $L=[l_1, l_2, \dots, l_n]$ be a single linked list

$$\begin{aligned} \text{gcd}(a,b) = & \begin{cases} a, & \text{if } b = 0 \\ \{\text{gcd}(b, a \bmod b), & \text{if } b \neq 0 \end{cases} \end{aligned}$$

$$\begin{aligned} \text{gcdList_rec}([]) &= 0 \text{ (empty list)} \\ \text{gcdList_rec}([l_1]) &= l_1 \text{ (single element)} \\ \text{gcdList_rec}([l_1, l_2, l_3, \dots, l_n]) &= \text{gcd}(l_1, \text{gcdList_rec}[l_2, l_3, \dots, l_n]) \end{aligned}$$

- b) Let $L=[l_1, l_2, \dots, l_n]$ be a single linked list, pos the position where we insert the element and value the value we insert
- $$\begin{aligned} \text{insert_pos_rec}([l_1, l_2, l_3, \dots, l_n], \text{value}, \text{pos}) &= [l_1] \cup \text{insert_pos_rec}([l_2, \dots, l_n], \text{value}, \text{pos} - 1) \\ L([]) &= \text{None} \\ L([l_1, l_2, \dots, l_n], \text{value}, 0) &= L[\text{value}, l_1, \dots, l_n] \end{aligned}$$

Examples:

E:\PLF-Lab1\venv\Scripts\python.exe E:\PLF-Lab1\main.py

1. Create list
2. Determine GCD of list elements

3. Insert element at n-position

4. Print list

5. LCM

6. Exit

Choice: 1

x = 4

x = 6

x = 8

x = 2

x = 0

Choice: 2

GCD: 2

Choice: 3

Value to insert: 5

Position: 0

5

4

6

8

2

Choice:

E:\PLF-Lab1\.venv\Scripts\python.exe E:\PLF-Lab1\main.py

1. Create list

2. Determine GCD of list elements

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6. Exit

Choice: 1

x = 3

x = 4

x = 5

x = 6

x = 0

Choice: 2

GCD: 1

Choice: 3

Value to insert: 7

Position: 5

3

4

5

6

Choice: 3

Value to insert: 7

Position: 4

3

4

5

6

7