# **MEC E 403**

# Lab 1: Centrifugal Pumps

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#### Abstract

This will be a summary of the lab. It will include the purpose of the lab, the methods used, and the results obtained. This will be completed after the lab is finished.

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#### 1 Nomenclature

will do this after the lab is done because I don't know what all the variables used will be yet. asd

#### 2 Introduction

#### 2.1 Background

**TO DO: Reword and find sources for information.** Pumps, turbines, and fans are turbo machines whose function is to change the energy level of a fluid. A pump or compressor increases the total head or pressure of the fluid while a turbine decreases it and extracts energy from the flow. Analysis of turbo machines is an important piece of technology, and a knowledge of their general characteristics is essential for many branches of engineering.

The geometry of turbo machines varies appreciably for the differing types that have been developed. Broadly there are two classes. In the first class there is a pronounced change in radius from the inlet to the discharge; these may be said to be centrifugal turbo machines. This is an important type of turbo machine as there are a great number of pumps, turbines and compressors that fall into this category. The other class consists of axial machines in which the flow is largely parallel to the axis of rotation. Between these extremes are examples in which the flow may proceed along conical surfaces of revolution, and these are sometimes called mixed-flow turbo machines. In all these varying types, however, there must be a rotating member, usually called a rotor, or impeller, to do work on the fluid.

# 2.2 Objectives

- 1. To measure the performance of a centrifugal pump and compare the results with the manufacturer's specification and theoretical predictions.
- 2. To compare the performance of parallel and series pump system configurations.

# 3 Procedure

# 3.1 Equipment

- Pump system that can be configured as a single pump or as two pumps in series or parallel operation. This is the system being studied.
- Stopwatch to measure time to fill a container
- Strobotach to verify pump rotational speed

- Mass scale to measure 200 lbs of water
- 1.401 kg mass to measure moment arm (torque) of motor
- Pressure transducers to measure pump pressure differential

#### 3.2 Procedure

- 1. The pump system will be tested individually at 1800, 2700, and 3600 RPM. The speed of the pump will be verified using the strobotach.
- 2. At each pump speed, the flow rates at 4 different pressures will be recorded (shutoff, full open, and two other equally spaced intermediate settings). The speed of the pump will be set to the correct value when changing the pressures before taking any other readings.
- 3. At each operating condition, the pump speed, pressure transducer output, the moment arm and dyno mass (to determine the torque produced by the motor), and time required to collect a known quantity of water will be recorded.
- 4. Items (2)-(4) will be repeated for parallel and series system configurations with both pumps set at 2700 RPM.

# 4 Theory

# 4.1 Euler's Turbomachinery Equations

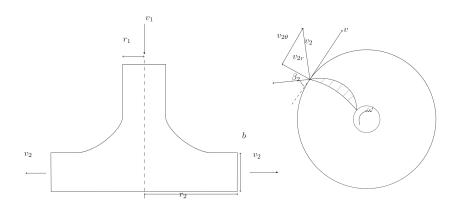


Figure 1: Impeller Diagram

Using the following assumptions:

1. Viscous effects are negligible

- 2. Velocity profile is uniform at the exit
- 3. All work done by the pump is transferred to the fluid

Then by conservation of angular momentum,

$$T = \dot{m}r_2 v_{2\theta} \tag{1}$$

where T is the torque,  $\dot{m}$  is the mass flow rate,  $r_2$  is the radius of the impeller, and  $v_{2\theta}$  is the tangential velocity at the exit. From Figure 1, we can see that

$$v_{2\theta} = U - v_{2r} \cot \beta_2 \tag{2}$$

where U is the tip speed,  $v_{2r}$  is the radial velocity at the exit, and  $\beta_2$  is the blade angle. Combining (1) and (2), we get

$$T = \dot{m}r_2(U - v_{2r}\cot\beta_2) \tag{3}$$

By Assumption 3, we can say that

$$T\Omega = \dot{m}gH \tag{4}$$

where  $\Omega$  is the impeller angular velocity, g is the acceleration due to gravity, and H is the total head rise across the pump. By combining (3), (4), and the kinematic relationship  $U = r_2\Omega$ , we get

$$\frac{Hg}{U^2} = 1 - \frac{v_{2r}}{U}\cot\beta_2\tag{5}$$

Defining the head coefficient  $\Psi$  and the flow coefficient  $\Phi$  as

$$\Psi = \frac{Hg}{U^2} \quad \Phi = \frac{v_{2r}}{U} \tag{6}$$

then (5) becomes

$$\Psi = 1 - \Phi \cot \beta_2 \tag{7}$$

also,  $v_{2r}$  can be expressed by the continuity equation as

$$v_{2r} = \frac{Q}{A_2} = \frac{Q}{b(2\pi r_2 - Nw)} \tag{8}$$

where Q is the flow rate,  $A_2$  is the area of the exit, b is the blade height at the exit, N is the number of blades, and w is the width of the blade.

#### 4.2 Shutoff Head

The ideal shutoff head can be obtained as

$$H'_{\text{ideal}} = \frac{U^2}{q}$$

by setting  $\Phi=0$  in (7). If it is assumed that all kinetic energy is lost due to friction, then

$$\frac{KE}{\text{unit weight}} = \frac{U^2}{2g}$$

where KE is the kinetic energy. Therefore, the rule of thumb for the shutoff head is

$$H'_{\text{thumb}} = \frac{U^2}{g} - \frac{U^2}{2g}$$

$$H'_{\text{thumb}} = \frac{U^2}{2g} = \frac{1}{2}H'_{\text{ideal}}$$

$$(9)$$

### 4.3 Affinity Laws

For large Reynolds numbers, the flow is dynamically similar in geometrically similar machines when the flow and head coefficients are the same. For geometrically similar machines operating at different conditions (i) and (ii) such that the head and flow coefficients are the same, the following relationships hold:

$$\Psi_i = \Psi_{ii}$$

$$\frac{H_i}{U_i^2} = \frac{H_{ii}}{U_{ii}^2}$$

so,

$$\frac{H_i}{H_{ii}} = \left(\frac{U_i}{U_{ii}}\right)^2 \approx \left(\frac{D_i \Omega_i}{D_{ii} \Omega_{ii}}\right)^2 \tag{10}$$

where D is the diameter of the impeller. Also,

$$\Phi_i = \Phi_{ii} 
\frac{v_{2ri}}{U_i} = \frac{v_{2rii}}{U_{ii}}$$
(11)

Assuming the blade width is negligible, from (8), we get

$$v_{2r} = \frac{Q}{\pi Db} \tag{12}$$

so (11) becomes

$$\frac{Q_i D_{ii} b_{ii}}{Q_{ii} D_i b_i} = \frac{U_i}{U_{ii}}$$

$$\frac{Q_i}{Q_{ii}} = \frac{\Omega_i b_i}{\Omega_{ii} b_{ii}} \left(\frac{D_i}{D_{ii}}\right)^2$$
(13)

For geometrically similar machines, the ratios of b/D are the same, so (13) becomes

$$\frac{Q_i}{Q_{ii}} = \frac{\Omega_i}{\Omega_{ii}} \left(\frac{D_i}{D_{ii}}\right)^3 \tag{14}$$

#### 4.4 Transducer Head Adjustment

In this experiment, since the inlet and outlet pipe diameters are different, the transducer head,  $H_t$ , must be corrected for flow kinetic energy to give the pump stagnation head, H, as

$$H = H_t + \frac{v_2^2}{2g} - \frac{v_1^2}{2g}$$

$$H = H_t + \frac{v_2^2}{2g} \left( 1 - \left( \frac{v_1}{v_2} \right)^2 \right)$$
(15)

where  $H_t$  is the transducer head,  $v_1$  is the velocity at the inlet, and  $v_2$  is the velocity at the outlet. The volume flowrate through the system can be written as

$$Q = \frac{v_2 \pi D_2^2}{4} \tag{16}$$

and with the pipe diameters  $D_1$  at the inlet and  $D_2$  at the outlet, mass conservation requires that

$$v_2 \pi D_2^2 = v_1 \pi D_1^2 \tag{17}$$

With (16) and (17), (15) becomes

$$H = H_t + \frac{8Q^2}{\pi^2 D_2^4 g} \left( 1 - \left( \frac{D_2}{D_1} \right)^4 \right)$$
 (18)

#### 4.5 Pumps in Series and Parallel

When pumps are connected in series, the total head is the sum of the individual heads, and the flow rate is the same as the individual flow rates. **CITE A FIGURE** 

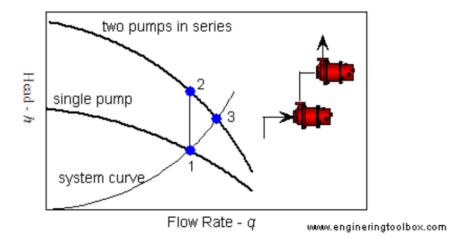


Figure 2: Pumps in Series

$$H_{\text{series},t} = H_{1,t} + H_{2,t}$$
 (19)

$$Q_{\text{series}} = Q_1 = Q_2 \tag{20}$$

When pumps are connected in parallel, the total head is the average of the individual heads, and the total flow rate is the sum of the individual flow rates.

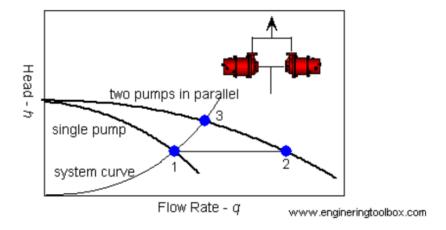


Figure 3: Pumps in Parallel

$$H_{\text{parallel},t} = \frac{H_{1,t} + H_{2,t}}{2} \tag{21}$$

$$Q_{\text{parallel}} = Q_1 + Q_2 \tag{22}$$

#### 5 Results and Discussion

#### 5.1 Single Pump Performance

- analyze data prolly put in appendix
- make plots
- do error analysis and propogation

#### 5.2 Parallel Pump Performance

- analyze data prolly put in appendix
- make plots
- do error analysis and propogation

#### **5.3** Series Pump Performance

- analyze data prolly put in appendix
- make plots
- do error analysis and propogation

# **5.4** Comparison of Pump Configurations

### 5.5 Manufacturer's Specifications

### 6 Conclusion

- Summarize the results of the lab
- Discuss the significance of the results
- Discuss the sources of error
- Discuss the limitations of the experiment
- Discuss the implications of the results
- Discuss the future work

# **6.1** Technical Recommendations

# 7 References

The references section will be auto populated with Bibtex.

# A Appendix: Single Pump Head-Discharge Analysis

### A.1 Single Pump Discharge and Heads

Table A.1: Single pump experimental discharge and heads for 1800 RPM, 2700 RPM, and 3600 RPM

Configuration	Pump Speed	Transducer Output	Time to collect water (s)		Nominal Time, t	Volumetric Flow, $Q$	Transducer Head, $H_t$	Corrected Head, H	
	(RPM)	(V)	Trial 1	Trial 2	Trial 3	(s)	$({ m m}^3{ m s}^{-1})$	(m)	(m)
Fully open	1800	0.75	28.55	28.99	28.79	28.78	0.003159	2.64	2.91
Partial 1	1800	0.83	30.14	30.51	30.16	30.27	0.003003	2.92	3.16
Partial 2	1800	1.43	61.12	60.80	60.86	60.93	0.001492	5.04	5.09
Closed	1800	1.56	-	-	-	-	-	5.49	5.49
Fully open	2700	1.50	18.66	18.93	18.55	18.71	0.004858	5.28	5.91
Partial 1	2700	1.62	19.23	19.23	18.96	19.14	0.004749	5.70	6.31
Partial 2	2700	2.94	31.15	31.30	31.22	31.22	0.002911	10.4	10.6
Closed	2700	3.52	-	-	-	-	-	12.4	12.4
Fully open	3600	2.44	14.13	13.93	14.06	14.04	0.006474	8.59	9.72
Partial 1	3600	2.89	15.04	14.35	14.31	14.57	0.006240	10.2	11.2
Partial 2	3600	5.85	37.01	37.04	37.07	37.04	0.002454	20.6	20.8
Closed	3600	6.18	-	-	-	-	-	21.8	21.8

Sample calculations are evaluated for the fully open configuration at 1800 RPM. Starting with time,

$$t = \frac{\sum t_i}{n} = \frac{28.55 \,\mathrm{s} + 28.99 \,\mathrm{s} + 28.79 \,\mathrm{s}}{3} = 28.78 \,\mathrm{s}$$

The volumetric flow rate was calculated using water which had a mass of  $m=200\,\mathrm{lb}=90.7\,\mathrm{kg}$  and a density of  $\rho=998\,\mathrm{kg}\,\mathrm{m}^{-3}$ . Then,

$$Q = \frac{m}{\rho t} = \frac{90.7 \,\mathrm{kg}}{998 \,\mathrm{kg} \,\mathrm{m}^{-3} \times 28.78 \,\mathrm{s}} = 0.003159 \,\mathrm{m}^3 \,\mathrm{s}^{-1}$$

The transducer head was found by

$$H_t = \frac{\Delta P}{\rho q} = \frac{0.75 \,\text{V} \times 5 \,\text{psi} \,\text{V}^{-1} \times 6894.76 \,\text{Pa} \,\text{psi}^{-1}}{998 \,\text{kg} \,\text{m}^{-3} \times 9.81 \,\text{m} \,\text{s}^{-2}} = 2.64 \,\text{m}$$

The corrected head was found using inlet diameter,  $D_1=0.0508\,\mathrm{m}$ , and outlet diameter,  $D_2=0.0508\,\mathrm{m}$ 

 $0.0381\,\mathrm{m},\,\mathrm{by}$ 

$$H = H_t + \frac{8Q^2}{\pi^2 D_2^4 g} \left[ 1 - \left( \frac{D_2}{D_1} \right)^4 \right]$$

$$= 2.64 \,\mathrm{m} + \frac{8 \times (0.003159 \,\mathrm{m}^3 \,\mathrm{s}^{-1})^2}{\pi^2 \times (0.0381 \,\mathrm{m})^4 \times 9.81 \,\mathrm{m} \,\mathrm{s}^{-2}} \left[ 1 - \left( \frac{0.0381 \,\mathrm{m}}{0.0508 \,\mathrm{m}} \right)^4 \right]$$

$$= 2.91 \,\mathrm{m}$$

#### A.2 Single Pump Head and Flow Coefficients

Table A.2: Single pump experimental head and flow coefficients for 1800 RPM, 2700 RPM, and 3600 RPM

Configuration	Pump Speed	Volumetric Flow, $Q$	Corrected Head, $H$	Tip Speed, ${\cal U}$	Radial Exit Velocity, $v_{2r}$	Head Coefficient, $\Psi$	Flow Coefficient, $\Phi$
	(RPM)	$({ m m}^3{ m s}^{-1})$	(m)	$(\mathrm{m}\mathrm{s}^{-1})$	$(\mathrm{ms^{-1}})$		
Fully open	1800	0.003159	2.91	10.2	1.2	0.275	0.12
Partial 1	1800	0.003003	3.16	10.2	1.1	0.300	0.11
Partial 2	1800	0.001492	5.09	10.2	0.6	0.482	0.05
Closed	1800	-	5.49	10.2	0.0	0.520	0.00
Fully open	2700	0.004858	5.91	15.3	1.8	0.249	0.12
Partial 1	2700	0.004749	6.31	15.3	1.8	0.265	0.12
Partial 2	2700	0.002911	10.6	15.3	1.1	0.445	0.07
Closed	2700	-	12.4	15.3	0.0	0.522	0.00
Fully open	3600	0.006474	9.72	20.4	2.4	0.230	0.12
Partial 1	3600	0.006240	11.2	20.4	2.3	0.266	0.11
Partial 2	3600	0.002454	20.8	20.4	0.9	0.491	0.05
Closed	3600	-	21.8	20.4	0.0	0.515	0.00

Sample calculations are evaluated for the fully open configuration at 1800 RPM. The tip speed was calculated using the impeller radius,  $r_2 = 0.108/2 = 0.054$  m, by

$$U = r_2 \Omega$$
  
= 0.054 m × 1800 RPM ×  $\left(\frac{2\pi}{60} \text{ RPM}^{-1}\right)$   
= 10.2 m s<sup>-1</sup>

The radial exit velocity was calculated using the impeller diameter, the blade height at exit, b =

 $0.009\,\mathrm{m}$ , blade width at exit,  $w=0.0085\,\mathrm{m}$ , and the number of blades N=5, by

$$v_{2r} = \frac{Q}{b(2\pi r_2 - Nw)}$$

$$= \frac{0.003159 \,\mathrm{m}^3 \,\mathrm{s}^{-1}}{0.009 \,\mathrm{m} \times (2\pi \times 0.054 \,\mathrm{m} - 5 \times 0.0085 \,\mathrm{m})}$$

$$= 1.2 \,\mathrm{m} \,\mathrm{s}^{-1}$$

The head coefficient was found by

$$\Psi = \frac{Hg}{U^2}$$

$$= \frac{2.91 \,\mathrm{m} \times 9.81 \,\mathrm{m} \,\mathrm{s}^{-2}}{(10.2 \,\mathrm{m} \,\mathrm{s}^{-1})^2}$$

$$= 0.275$$

The flow coefficient was found by

$$\Phi = \frac{v_{2r}}{U}$$

$$= \frac{1.2 \,\mathrm{m \, s^{-1}}}{10.2 \,\mathrm{m \, s^{-1}}}$$

$$= 0.12$$

# A.3 Single Pump Manufaturer's Data

Sample calculations are evaluated 1800 RPM with a volumetric flow rate of  $Q=0.0040\,\mathrm{m^3\,s^{-1}}$ . The tip speed was calculated using the impeller radius,  $r_2=0.108/2=0.054\,\mathrm{m}$ , by

$$U = r_2 \Omega$$
  
= 0.054 m × 1800 RPM ×  $\left(\frac{2\pi}{60} \text{ RPM}^{-1}\right)$   
= 10.2 m s<sup>-1</sup>

	Table A.3: Single p	oump manufacturer	's data for	1800 RPM.	2700 RPM.	and 3600 RPM
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Pump Speed	Volumetric Flow, $Q$	Head, $H$	Tip Speed, ${\cal U}$	Radial Exit Velocity, $v_{2r}$	Head Coefficient, $\Psi$	Flow Coefficient, $\Phi$
(RPM)	$(m^3 s^{-1})$	(m)	$(\mathrm{ms^{-1}})$	$(\mathrm{ms^{-1}})$		
1800	0.0040	2.58	10.2	1.5	0.244	0.15
1800	0.0033	4.14	10.2	1.2	0.392	0.12
1800	0.0026	4.96	10.2	1.0	0.470	0.10
1800	0.0020	5.40	10.2	0.75	0.511	0.07
2700	0.0060	5.77	15.3	2.2	0.243	0.15
2700	0.0050	9.12	15.3	1.9	0.384	0.12
2700	0.0040	11.0	15.3	1.5	0.463	0.10
2700	0.0030	12.1	15.3	1.1	0.509	0.07
2700	0.0020	12.8	15.3	0.75	0.539	0.05
3600	0.0080	10.3	20.4	3.0	0.244	0.15
3600	0.0067	16.1	20.4	2.5	0.381	0.12
3600	0.0054	19.2	20.4	2.0	0.454	0.10
3600	0.0040	21.6	20.4	1.5	0.511	0.07
3600	0.0027	22.8	20.4	1.0	0.540	0.05

The radial exit velocity was calculated using the impeller diameter, the blade height at exit,  $b=0.009\,\mathrm{m}$ , blade width at exit,  $w=0.0085\,\mathrm{m}$ , and the number of blades N=5, by

$$v_{2r} = \frac{Q}{b(2\pi r_2 - Nw)}$$

$$= \frac{0.0040 \,\mathrm{m}^3 \,\mathrm{s}^{-1}}{0.009 \,\mathrm{m} \times (2\pi \times 0.054 \,\mathrm{m} - 5 \times 0.0085 \,\mathrm{m})}$$

$$= 1.5 \,\mathrm{m} \,\mathrm{s}^{-1}$$

The head coefficient was found by

$$\Psi = \frac{Hg}{U^2}$$

$$= \frac{2.58 \,\mathrm{m} \times 9.81 \,\mathrm{m} \,\mathrm{s}^{-2}}{(10.2 \,\mathrm{m} \,\mathrm{s}^{-1})^2}$$

$$= 0.244$$

The flow coefficient was found by

$$\Phi = \frac{v_{2r}}{U}$$

$$= \frac{1.5 \,\mathrm{m \, s^{-1}}}{10.2 \,\mathrm{m \, s^{-1}}}$$

$$= 0.15$$