

Lecture - 18 (Determinants)

defined for
square matrix

$$\det A \quad / \quad |A|$$

Invertible $\longrightarrow |A| \neq 0$
Non-Invertible $\longrightarrow |A| = 0$

① $\det I = 1$

② Exchange rows: reverse sign of determinant

③ → ① If we multiply t with one of the row then determinant become t times.

$$\begin{vmatrix} ta & tb \\ c & d \end{vmatrix} = t \begin{vmatrix} a & b \\ c & d \end{vmatrix}$$

→ ② $\begin{vmatrix} a+ta' & b+tb' \\ c & d \end{vmatrix} = \begin{vmatrix} a & b \\ c & d \end{vmatrix} + \begin{vmatrix} ta' & tb' \\ c & d \end{vmatrix}$

Linear for each row.

④ ~~Two~~ Two equal result in Zero determinant.

⑤ Subtract $k \times \text{row } I$ from row K .
 \longrightarrow determinant doesn't change.

⑥ Row of Zeros $\rightarrow \det A = 0$

⑦
$$\begin{vmatrix} d_1 & - & + & + \\ 0 & d_2 & - & + \\ 0 & 0 & d_3 & + \\ 0 & 0 & 0 & d_n \\ 0 & 0 & 0 & 0 \end{vmatrix} = d_1 d_2 d_3 \dots d_n$$

⑧ $|A| = 0$ when A is Singular.

⑨ $\det AB = (\det A)(\det B)$

$\| \det A^{-1} = \frac{1}{\det A} \|$

$\det A^n = (\det A)^n$

~~$\det mA$~~

$\det mA = \det A \times m^n$

$\rightarrow \{ \text{If } n = \text{dim of } A \}$

⑩ $\det A^T = \det A$

