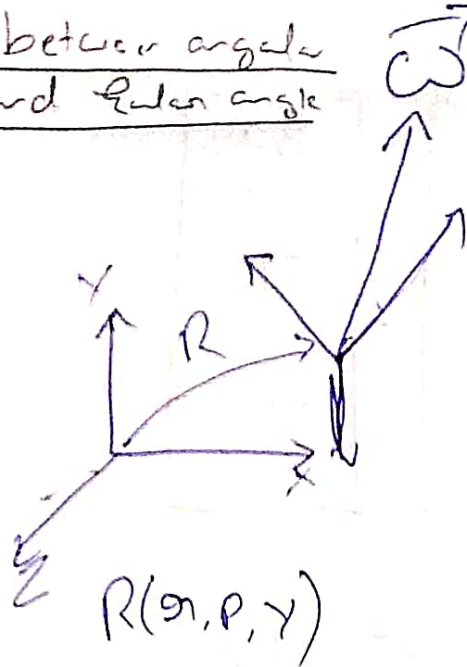


Relation between angular velocity and Euler angle rate



$$E = \begin{bmatrix} \frac{\delta \alpha}{\delta t} \\ \frac{\delta \beta}{\delta t} \\ \frac{\delta \gamma}{\delta t} \end{bmatrix} \rightarrow \omega$$

$$\begin{bmatrix} \frac{\delta \alpha}{\delta t} \\ 0 \\ 0 \end{bmatrix} + R^T(\alpha) \begin{bmatrix} 0 \\ \frac{\delta \beta}{\delta t} \\ 0 \end{bmatrix} + R^T(\alpha) R^T(\beta) \begin{bmatrix} 0 \\ 0 \\ \frac{\delta \gamma}{\delta t} \end{bmatrix}$$

$$\begin{bmatrix} \frac{\delta \alpha}{\delta t} \\ 0 \\ 0 \end{bmatrix} + \begin{bmatrix} 1 & 0 & 0 \\ 0 & C_\alpha & S_\alpha \\ 0 & -S_\alpha & C_\alpha \end{bmatrix} \begin{bmatrix} 0 \\ \frac{\delta \beta}{\delta t} \\ 0 \end{bmatrix} + \begin{bmatrix} 1 & 0 & 0 \\ 0 & C_\alpha & S_\alpha \\ 0 & -S_\alpha & C_\alpha \end{bmatrix} \begin{bmatrix} C_\beta & 0 & -S_\beta \\ 0 & 1 & 0 \\ S_\beta & 0 & C_\beta \end{bmatrix} \begin{bmatrix} 0 \\ 0 \\ \frac{\delta \gamma}{\delta t} \end{bmatrix}$$

$$\begin{bmatrix} 0 \\ C_\alpha \frac{\delta \beta}{\delta t} \\ -S_\alpha \frac{\delta \beta}{\delta t} \end{bmatrix} \quad \begin{bmatrix} -S_\beta \frac{\delta \gamma}{\delta t} \\ 0 \\ C_\beta \frac{\delta \gamma}{\delta t} \end{bmatrix}$$

$$\begin{bmatrix} -S_\beta \frac{\delta \gamma}{\delta t} \\ S_\alpha C_\beta \frac{\delta \gamma}{\delta t} \\ C_\alpha C_\beta \frac{\delta \gamma}{\delta t} \end{bmatrix}$$

$$\omega = \begin{bmatrix} 1 & 0 & -S_p \\ 0 & C_{\alpha} & S_{\alpha} C_p \\ 0 & -S_{\alpha} & C_{\alpha} C_p \end{bmatrix} \begin{bmatrix} \frac{\delta \eta}{\delta t} \\ \frac{\delta p}{\delta t} \\ \frac{\delta y}{\delta t} \end{bmatrix}$$

$$\begin{bmatrix} \frac{\delta \eta}{\delta t} \\ \frac{\delta p}{\delta t} \\ \frac{\delta y}{\delta t} \end{bmatrix} = \begin{bmatrix} 1 & S_{\alpha} t_p & C_{\alpha} t_p \\ 0 & C_{\alpha} & -S_{\alpha} \\ 0 & \frac{S_{\alpha}}{C_p} & \frac{C_{\alpha}}{C_p} \end{bmatrix} \omega$$