

# Data Structures 1.1

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## What is a Data Structure?

A data structure (DS) is a way of organizing data so that it can be used effectively.

## Why Data Structures?

They are essential ingredients in creating fast and powerful algorithms.

They help to manage and organize data.

They make code cleaner and easier to understand.

## Abstract Data Types vs. Data Structures.

### Abstract Data Type

An abstract data type (ADT) is an abstraction of a data structure which provides only the interface to which a data structure must adhere to.

The interface does not give any specific details about how something should be implemented or in what programming language.

Table 1: Examples

<b>Abstraction (ADT)</b>	<b>Implementation (DS)</b>
List	Dynamic Array Linked List
Queue	Linked List based, Array Based Queue, Stack based Queue
Map	Tree Map, Hash Map / Hash Table
Vehicle	Golf Cart, Bicycle, Smart Car

## Computational Complexity Analysis

### Complexity Analysis

As programmers, we often find ourselves asking the same two questions over and over again:

How much time does this algorithm need to finish?

How much space does this algorithm need for its computation?

## Big-O Notation

Big-O Notation gives an upper bound of the complexity in the worst case, helping to quantify performance as the input size becomes arbitrarily large.

$n$  - The size of the input

Table 2: Complexities ordered in from smallest to largest.

Term	Notation
Constant Time	$O(1)$
Logarithmic Time	$O(\log(n))$
Linear Time	$O(n)$
Linearithmic Time	$O(n \log(n))$
Quadratic Time	$O(n^2)$
Cubic Time	$O(n^3)$
Exponential Time	$O(b^n), b > 1$
Factorial Time	$O(n!)$

## Big-O Properties

$$O(n + c) = O(n)$$

$$O(cn) = O(n), c > 0$$

Let  $f$  be a function that describes the running times of a particular algorithm for an input size of  $n$ :

$$f(n) = 7\log(n)^3 + 15n^2 + 2n^3 + 8$$

$$O(f(n)) = O(n^3)$$

## Big-O Examples