

Pattern Recognition

Lecture 19. Clustering

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PR/ML algorithms category

Supervised Learning

labeled data, task-driven

- **Classification**
- **Regression**
 - *e.g., Population growth prediction, Market prediction, etc.*

Unsupervised Learning

unlabeled data, data-driven

- **Dimensionality Reduction**
- **Clustering**

Reinforcement Learning

learn from error

- *e.g., Real-time Decision, Game AI*

- Unsupervised learning , Requires data, but no labels
- Detect patterns, e.g.
 - Group emails or search results
 - Regions of images
- Useful when don't know what you're looking for



Applications

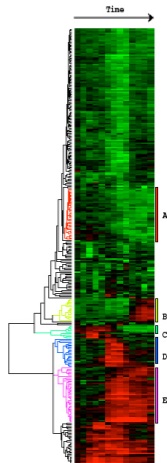
Image Segmentation



[Slide from James Hayes]

Applications

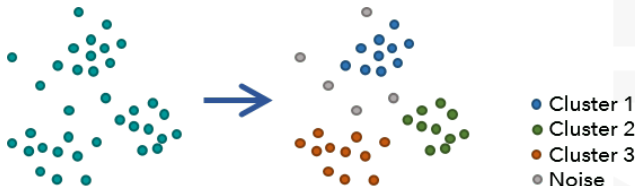
Clustering gene expression data



Eisen et al, PNAS 1998

Clustering

- The organization of **unlabeled data** into similarity groups called **clusters**.
- A **cluster** is a collection of data items which are “similar” between them, and “dissimilar” to data items in other clusters.



Similarities?



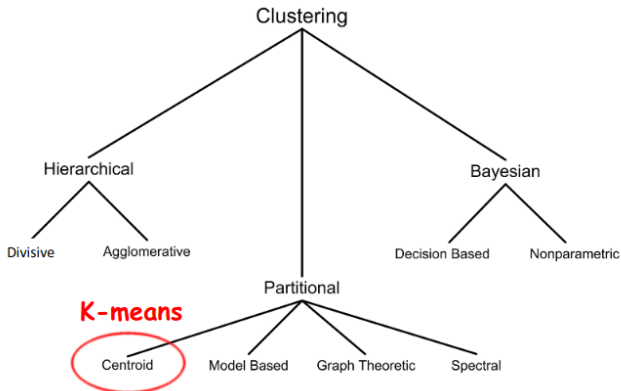
Defining Distance Measures

Definition: Let $O1$ and $O2$ be two objects from the universe of possible objects. The distance (dissimilarity) between $O1$ and $O2$ is a real number denoted by $D(O1, O2)$.

e.g.

- Euclidean distance
- Correlation coefficient
- etc.

Clustering



Clustering

- **Hierarchical** algorithms find successive clusters using previously established clusters. These algorithms can either **agglomerative** (*bottom-up*) or **divisive** (*top-down*):
 - **Agglomerative algorithms** begin with each element as a separate cluster and merge them into successive larger clusters;
 - **Divisive algorithms** begin with the whole set and proceed to divide it into successively smaller clusters.
- **Partitional** algorithms typically determine all clusters at once, but can also be used as divisive algorithms in the hierarchical clustering.
- **Bayesian** algorithms try to generate a *posteriori distribution* over the collection of all partitions of the data.

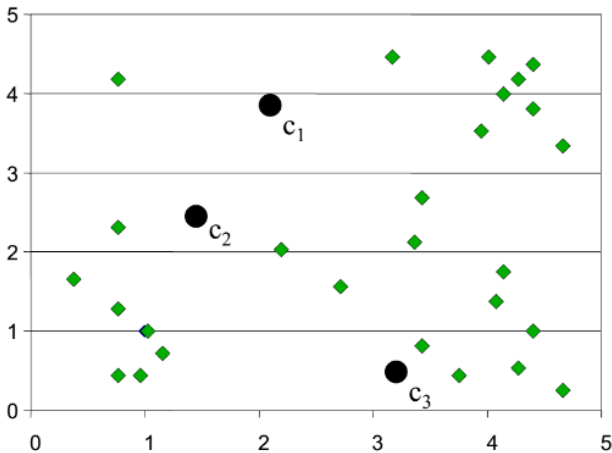
K-means

An iterative clustering algorithm

- **Initialize:** Pick K random points as cluster centers
- **Alternate:**
 - 1. Assign data points to closest cluster center
 - 2. Change the cluster center to the average of its assigned points
- Stop when no points' assignments change

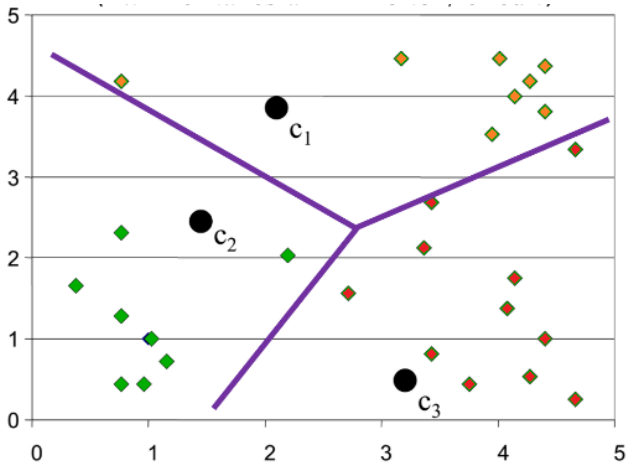
K-Means

Step 1. Randomly initialize cluster centers



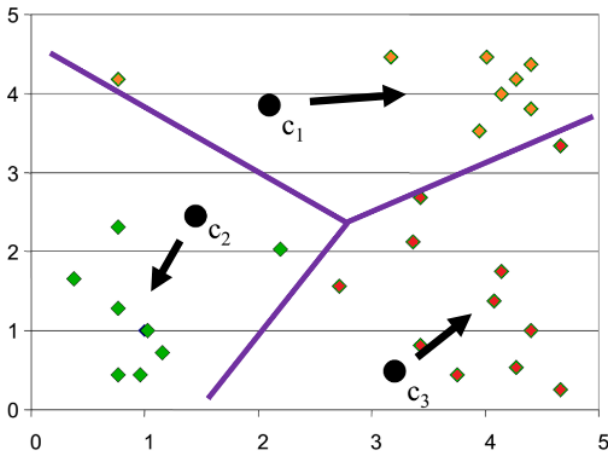
K-Means

Step 2. Determine cluster membership for each input



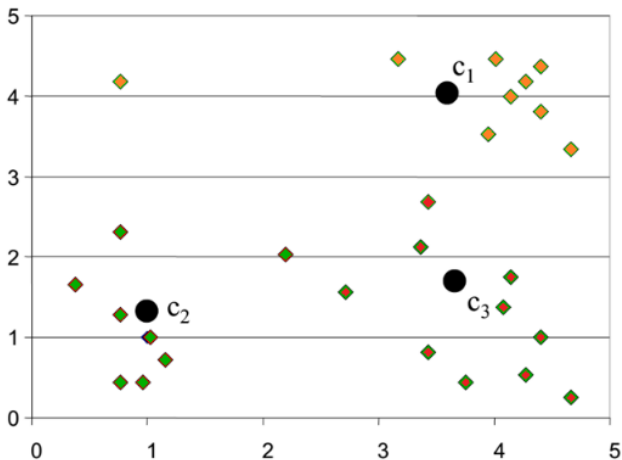
K-Means

Step 3. Re-estimate cluster centers



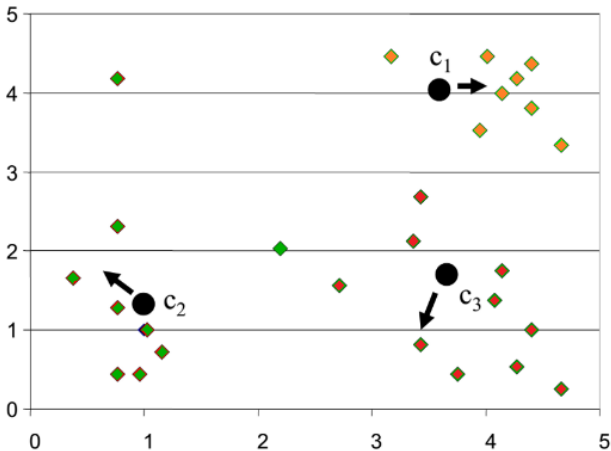
K-Means

Result of the first iteration



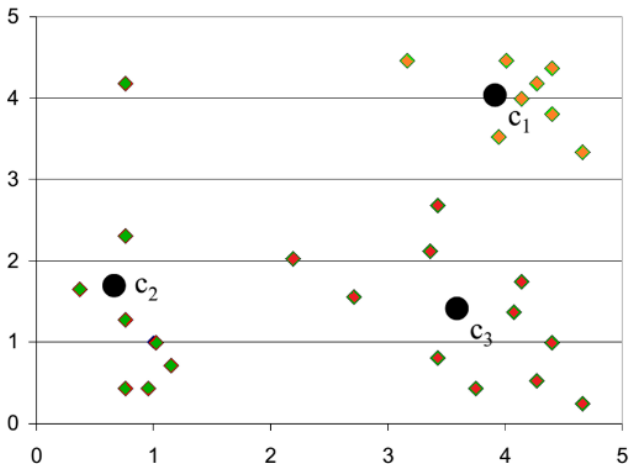
K-Means

Second Iteration



K-Means

Result of the second iteration



K-means convergence (stopping) criterion

- no (or minimum) re-assignments of data points to different clusters
- no (or minimum) change of centroids
- minimum decrease in the sum of squared error (SSE)

$$SSE = \sum_{j=1}^k \sum_{\mathbf{x} \in C_j} d(\mathbf{x}, \mathbf{m}_j)^2$$

- C_j is the j th cluster,
- \mathbf{m}_j is the centroid of cluster C_j (the mean vector of all the data points in C_j),
- $d(\mathbf{x}, \mathbf{m}_j)$ is the (Euclidean) distance between data point \mathbf{x} and centroid \mathbf{m}_j .

Summary: K-Means

Strength

- Simple, easy to implement and debug
- Intuitive objective function: optimizes intra-cluster similarity
- Relatively efficient.

Weakness

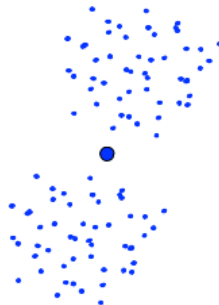
- Applicable only when mean is defined, what about categorical data?
- Often terminates at a local optimum. Initialization is important.
- Need to specify K, the number of clusters, in advance.
- Unable to handle noisy data and outliers.
- Not suitable to discover clusters with non-convex shapes

Appendix

A local optimum:



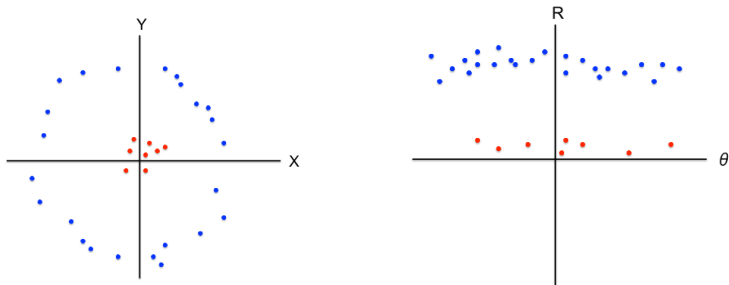
Would be better to have
one cluster here



... and two clusters here

Figure: K-Means Getting Stuck

Appendix



(a) K-means not able to properly cluster (b) Changing the features (distance function) can help

Reference I



Thank You !
Q & A