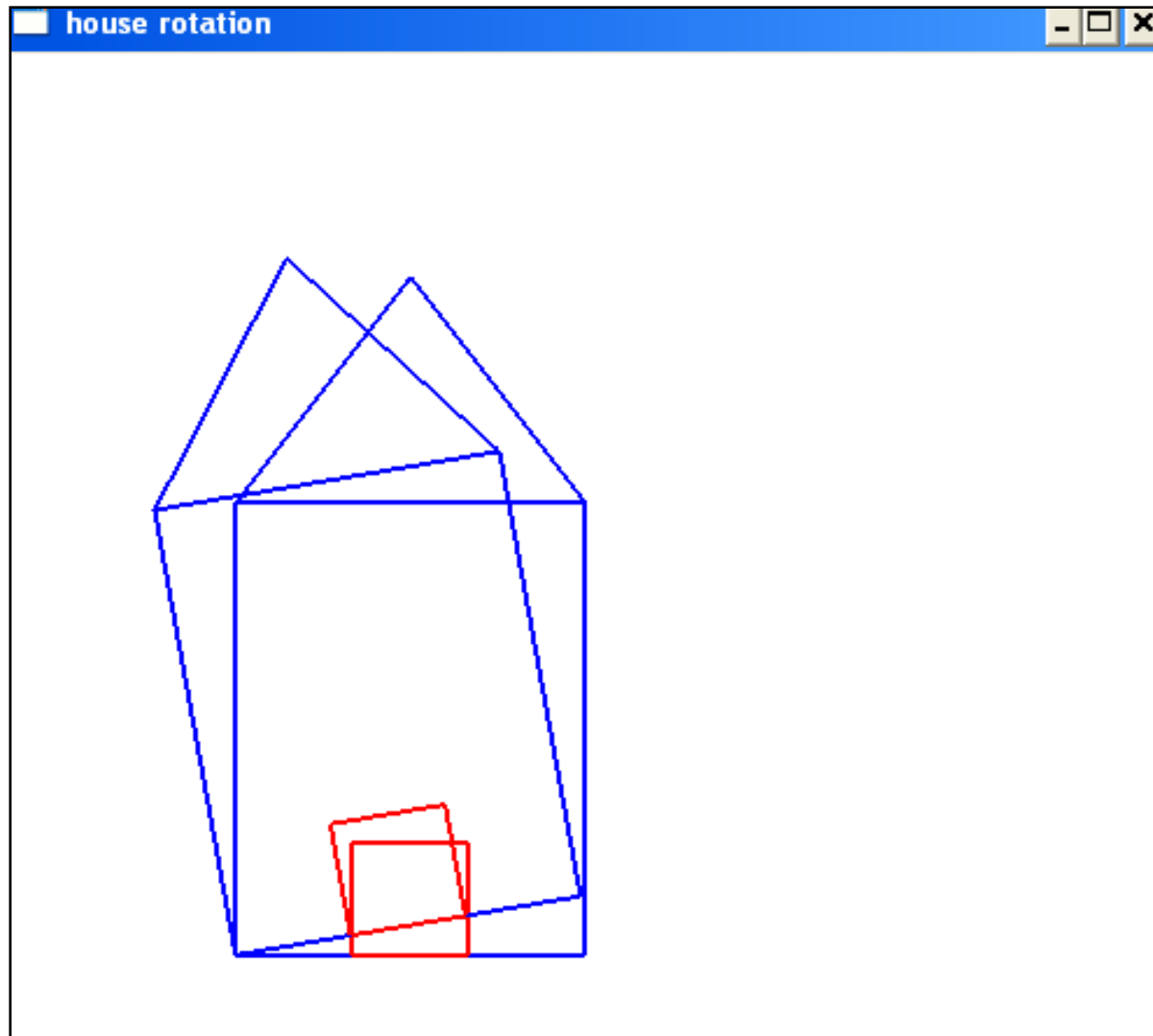


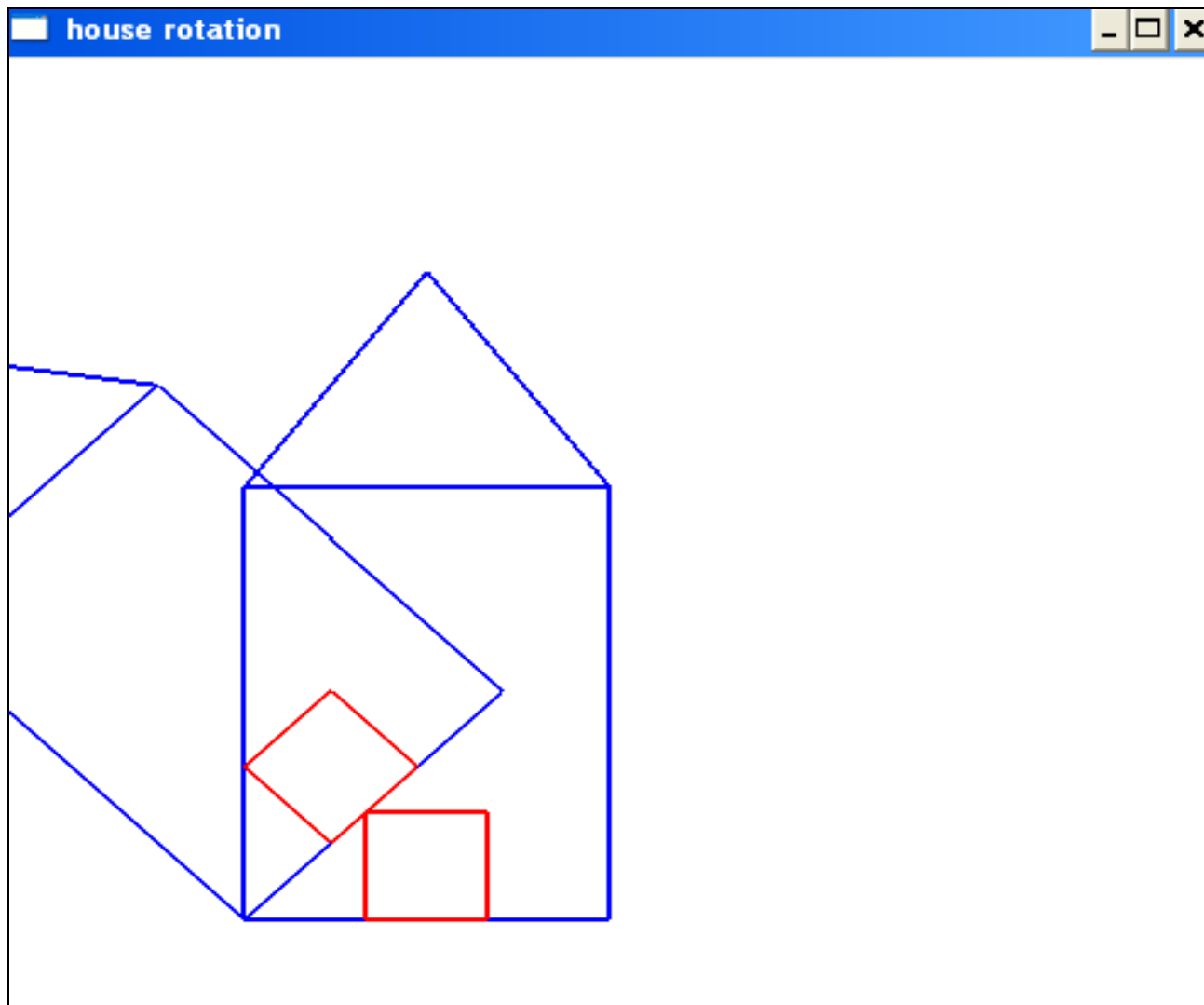
Program 4

Program to create a house like figure and rotate it about a *given fixed point* using OpenGL functions.

Enter the rotation angle
10



Enter the rotation angle
45

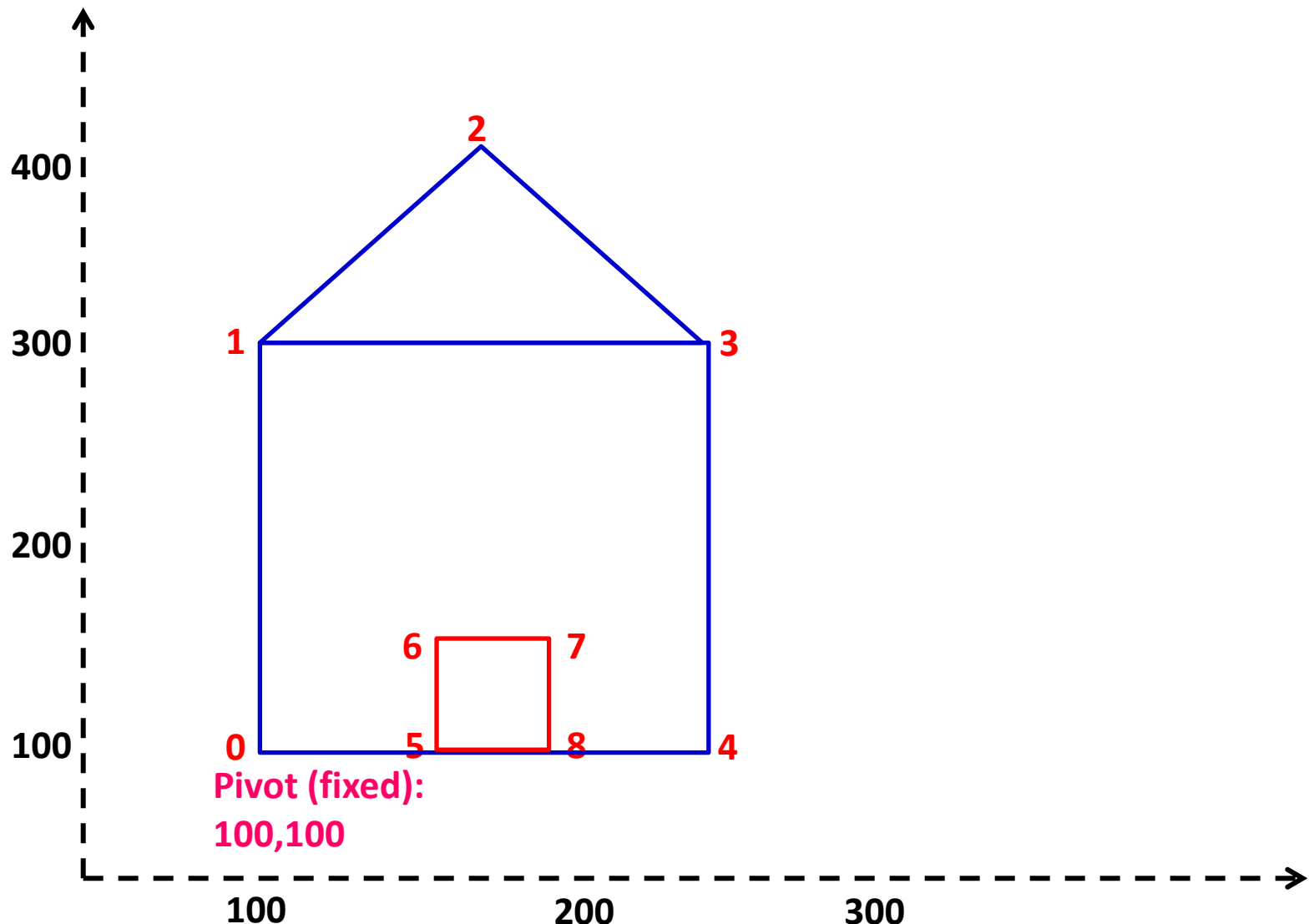


	0	1	2	3	4	5	6	7	8
0(x)	100	100	175	250	250	150	150	200	200
1(y)	100	300	400	300	100	100	150	150	100
2	1	1	1	1	1	1	1	1	1

LINE_LOOP : 0,1,3,4

LINE_LOOP : 1,2,3

LINE_LOOP : 5,6,7,8



2D Transformations in Computer Graphics

In computer graphics, the 3 transformations are

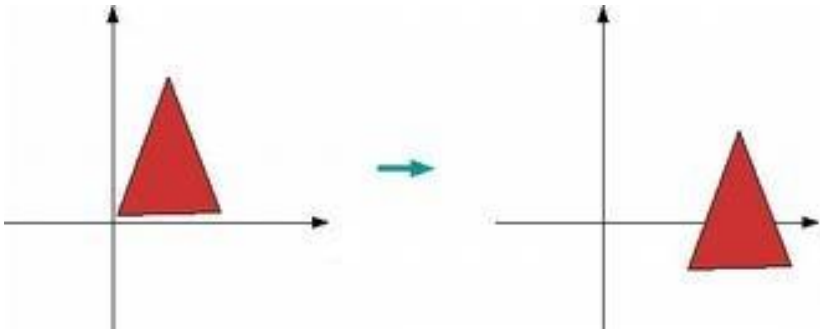
1. Translation

2. Rotation

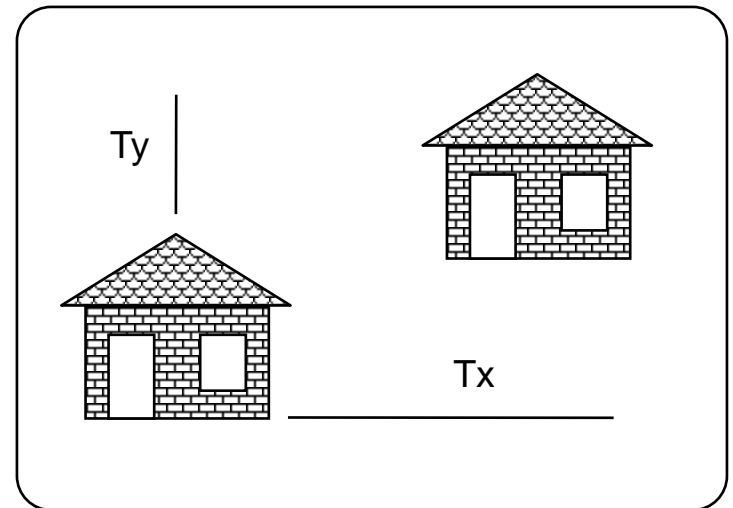
- About the origin
- About the fixed (pivot) point

3. Scaling

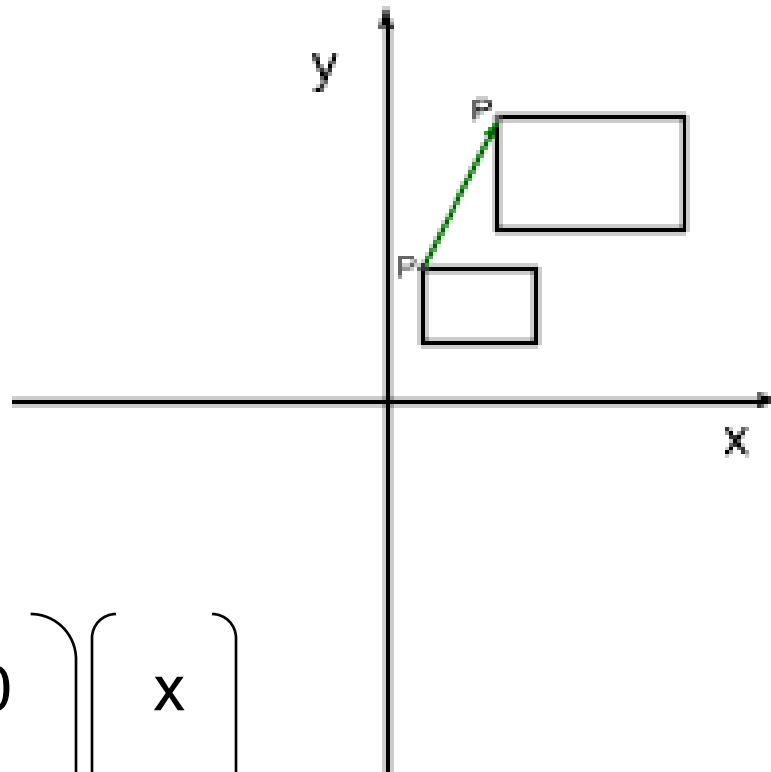
1. Translation



$$\begin{aligned}x' &= x + T_x \\ y' &= y + T_y\end{aligned}$$



2. Scaling

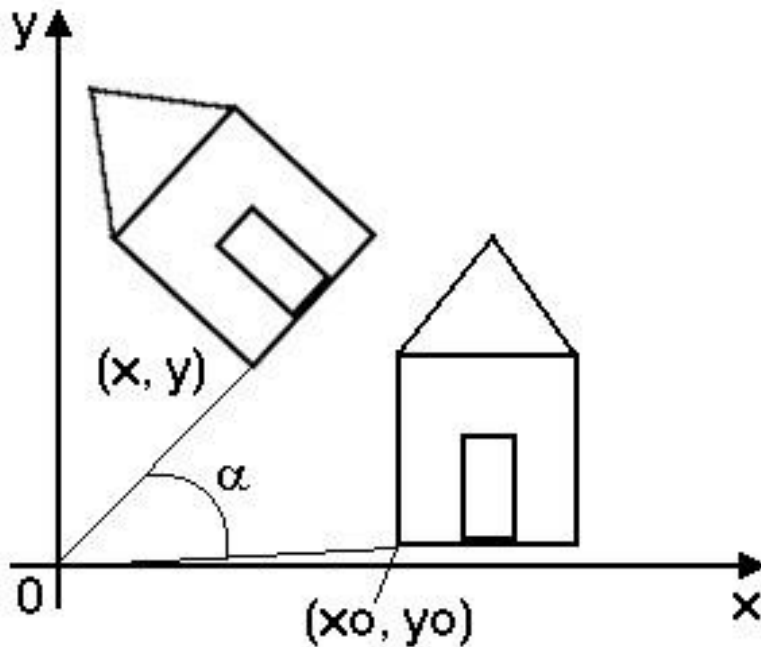


$$\begin{pmatrix} x' \\ y' \end{pmatrix} = \begin{pmatrix} S_x & 0 \\ 0 & S_y \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix}$$

3. Rotation

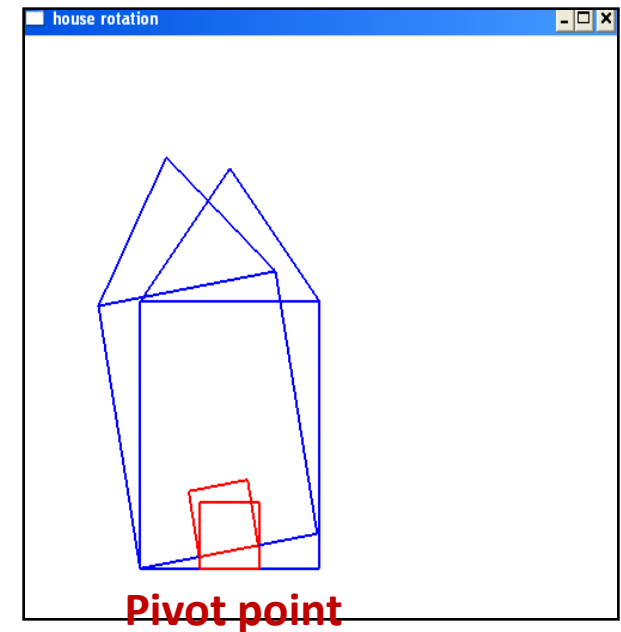
Rotation

about the origin

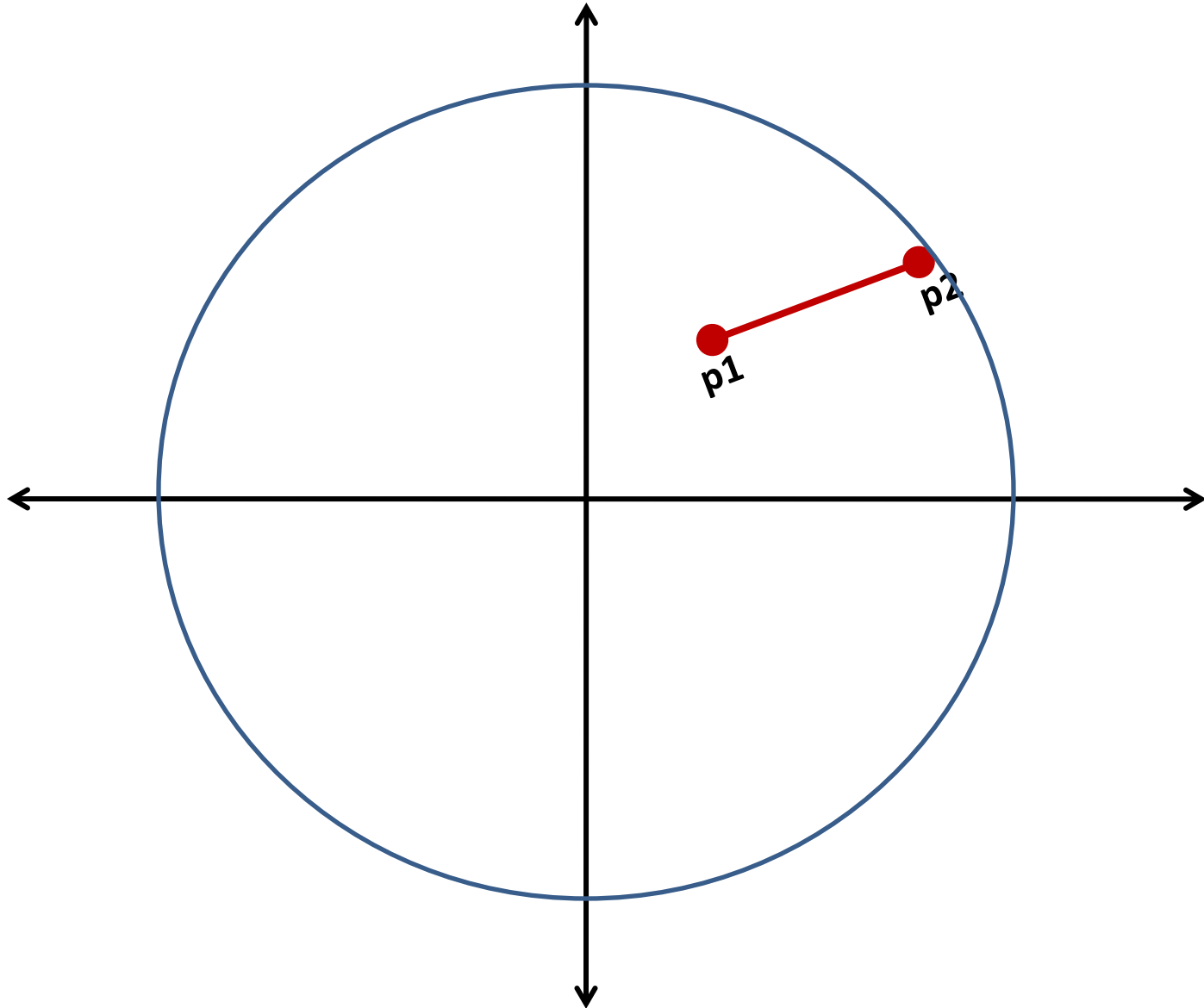


Rotation

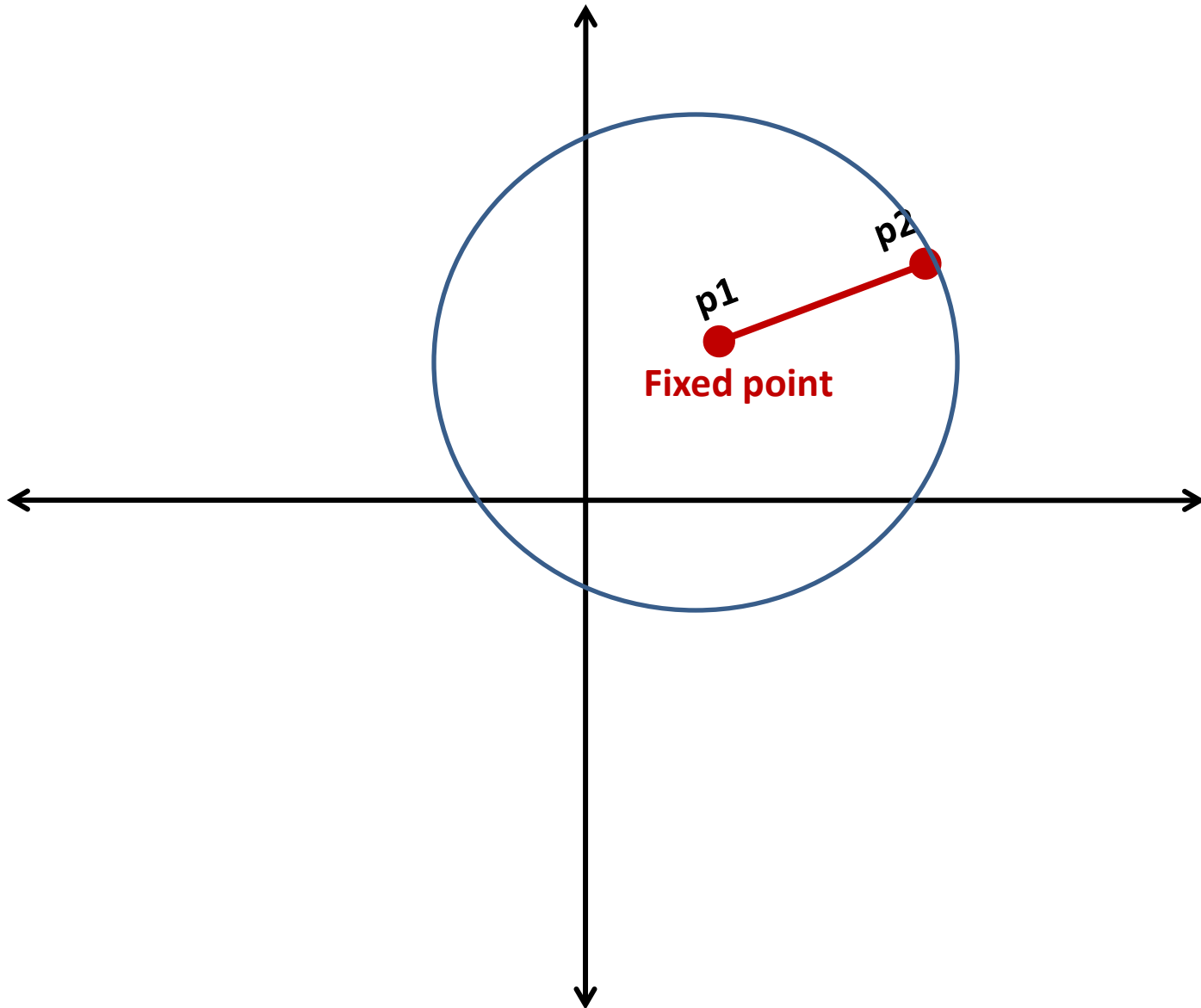
about the fixed (pivot) point



Rotation about the *origin*



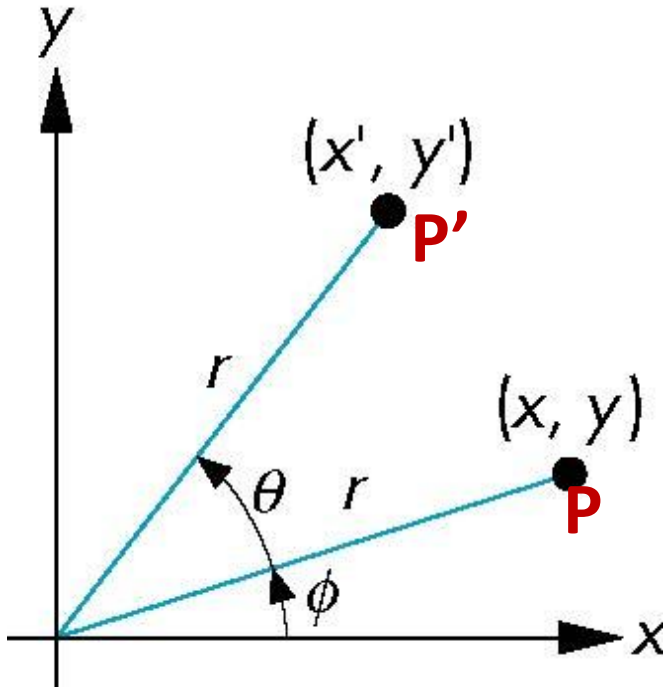
Rotation about the *fixed point*



Rotation about the origin

Consider rotation about the origin by θ degrees:

The radius r stays the same, angle increases by θ



Original point $P(x,y)$

$$x = r \cos \phi$$

$$y = r \sin \phi$$

Rotated point $P'(x',y')$

$$x' = r \cos (\phi + \theta)$$

$$y' = r \sin (\phi + \theta)$$

Rotation about the origin

Original point $p(x,y)$

$$x = r \cos \phi$$

$$y = r \sin \phi$$

WKT

$$\sin(A+B) = \sin A \cos B + \cos A \sin B$$

$$\cos(A+B) = \cos A \cos B - \sin A \sin B$$

Substituting for x' and y'

$$x' = r \cos (\phi + \theta)$$

$$\mathbf{x' = x \cos \theta - y \sin \theta}$$

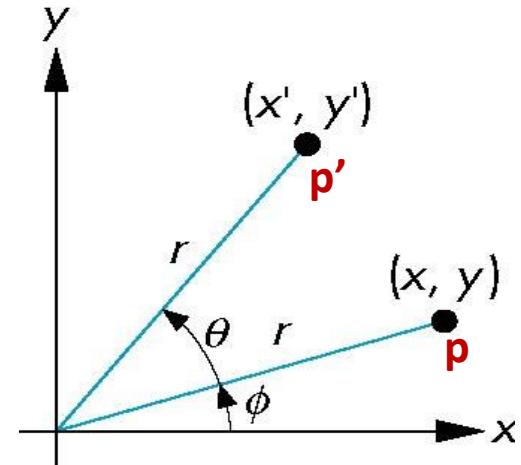
$$y' = r \sin (\phi + \theta)$$

$$\mathbf{y' = x \sin \theta + y \cos \theta}$$

Rotated point $p'(x',y')$

$$x' = r \cos (\phi + \theta)$$

$$y' = r \sin (\phi + \theta)$$



$$\begin{pmatrix} x' \\ y' \end{pmatrix} = \begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix}$$

Rotation about the origin

$$x' = x \cos\theta - y \sin\theta$$

$$y' = x \sin\theta + y \cos\theta$$

$$\begin{pmatrix} x' \\ y' \end{pmatrix} = \begin{pmatrix} \cos\theta & -\sin\theta \\ \sin\theta & \cos\theta \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix}$$

Homogeneous co-ordinate System

$$\begin{pmatrix} x' \\ y' \\ 1 \end{pmatrix} = \begin{pmatrix} \cos\theta & -\sin\theta & 0 \\ \sin\theta & \cos\theta & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \\ 1 \end{pmatrix}$$

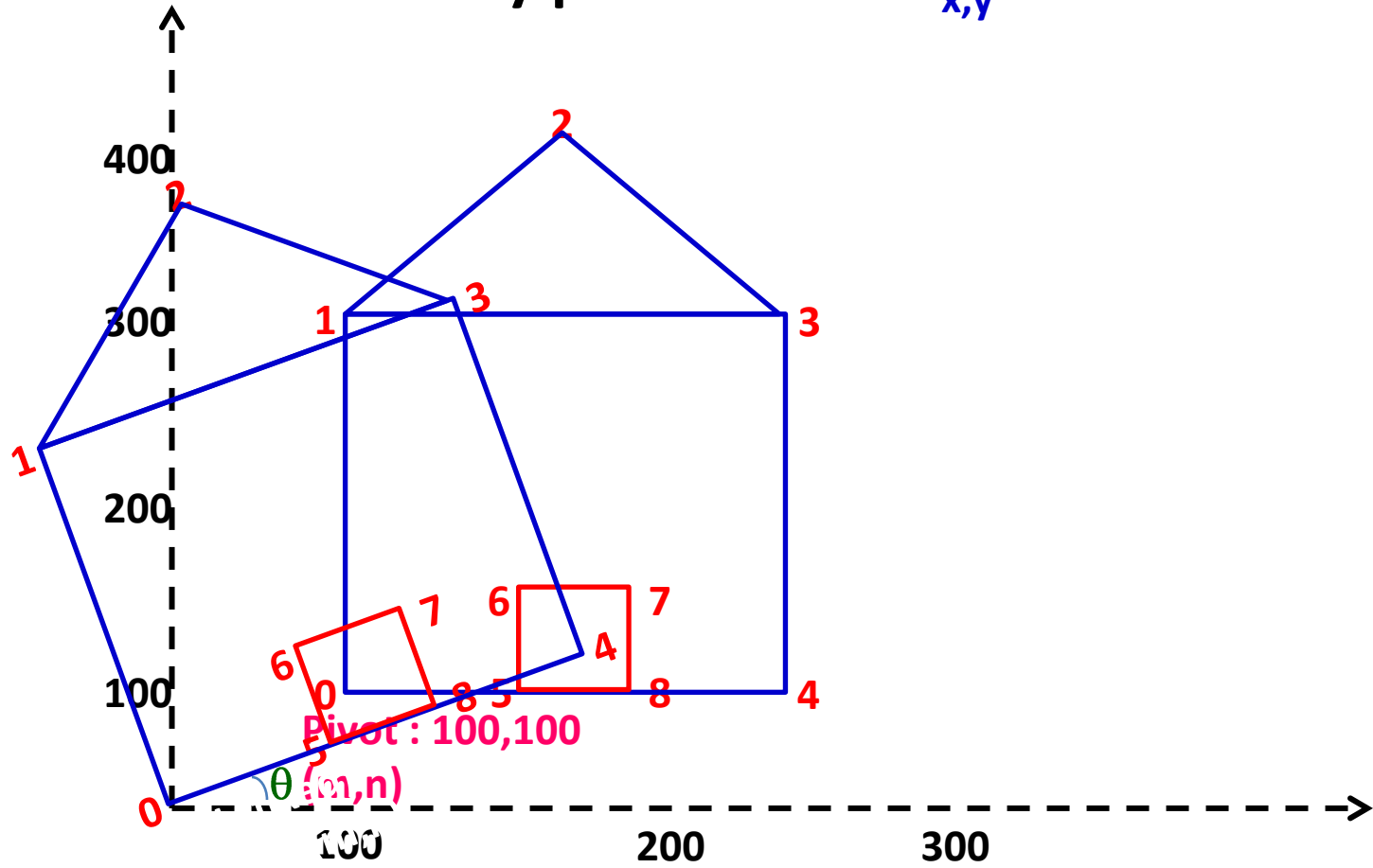
2D Transformations

Transformation	Equation	Homogeneous Equation
Translation	$x' = x + dx$ $y' = y + dy$	$\begin{pmatrix} x' \\ y' \\ 1 \end{pmatrix} = \begin{pmatrix} 1 & 0 & dx \\ 0 & 1 & dy \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \\ 1 \end{pmatrix}$
Rotation	$\begin{pmatrix} x' \\ y' \end{pmatrix} = \begin{pmatrix} \cos\theta & -\sin\theta \\ \sin\theta & \cos\theta \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix}$	$\begin{pmatrix} x' \\ y' \\ 1 \end{pmatrix} = \begin{pmatrix} \cos\theta & -\sin\theta & 0 \\ \sin\theta & \cos\theta & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \\ 1 \end{pmatrix}$
Scaling	$\begin{pmatrix} x' \\ y' \end{pmatrix} = \begin{pmatrix} S_x & 0 \\ 0 & S_y \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix}$	$\begin{pmatrix} x' \\ y' \\ 1 \end{pmatrix} = \begin{pmatrix} S_x & 0 & 0 \\ 0 & S_y & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \\ 1 \end{pmatrix}$

Rotation about an arbitrary point

Rotation about an arbitrary point (m,n)

1. Translate to origin -----> $T_{-x, -y}$
2. Rotate through θ -----> R_{θ}
3. Translate back to the arbitrary point -----> $T_{x,y}$



Rotation about an arbitrary point (m,n)

1. Translate to origin -----> $T_{-x, -y}$
2. Rotate through θ -----> R_θ
3. Translate back to the arbitrary point -----> $T_{x, y}$

Result C =

$$\begin{pmatrix} 1 & 0 & m \\ 0 & 1 & n \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} \cos\theta & -\sin\theta & 0 \\ \sin\theta & \cos\theta & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 & -m \\ 0 & 1 & -n \\ 0 & 0 & 1 \end{pmatrix}$$

$T_{x,y} \qquad R_\theta \qquad T_{-x,-y}$

Rotation about an arbitrary point (m,n)

Result C =

$$\begin{matrix} \begin{pmatrix} 1 & 0 & m \\ 0 & 1 & n \\ 0 & 0 & 1 \end{pmatrix} & \begin{pmatrix} \cos\theta & -\sin\theta & 0 \\ \sin\theta & \cos\theta & 0 \\ 0 & 0 & 1 \end{pmatrix} & \begin{pmatrix} 1 & 0 & -m \\ 0 & 1 & -n \\ 0 & 0 & 1 \end{pmatrix} \\ T_{x,y} & R_\theta & T_{-x,-y} \end{matrix}$$

$$\begin{matrix} \begin{pmatrix} \cos\theta & -\sin\theta & m \\ \sin\theta & \cos\theta & n \\ 0 & 0 & 1 \end{pmatrix} & \begin{pmatrix} 1 & 0 & -m \\ 0 & 1 & -n \\ 0 & 0 & 1 \end{pmatrix} \\ T_{x,y} \times R_\theta & T_{-x,-y} \end{matrix}$$

$$\begin{matrix} \begin{pmatrix} \cos\theta & -\sin\theta & -x\cos\theta + y\sin\theta + x \\ \sin\theta & \cos\theta & -x\sin\theta - y\cos\theta + y \\ 0 & 0 & 1 \end{pmatrix} \\ T_{x,y} \times R_\theta \times T_{-x,-y} \end{matrix}$$

Rotation Matrix

$$R(\theta) = \begin{pmatrix} \cos\theta & -\sin\theta & -x\cos\theta + y\sin\theta + x \\ \sin\theta & \cos\theta & -x\sin\theta - y\cos\theta + y \\ 0 & 0 & 1 \end{pmatrix}$$

```
#include <stdio.h>
#include <math.h>
#include <GL/glut.h>
```

```
GLfloat house[3][9]={
{100.0,100.0,175.0,250.0,250.0,150.0,150.0,200.0,200.0},
{100.0,300.0,400.0,300.0,100.0,100.0,150.0,150.0,100.0},
{1.0,1.0,1.0,1.0,1.0,1.0,1.0,1.0,1.0}
};
GLfloat rot_mat[3][3]={ {0}, {0}, {0} };
GLfloat result[3][9]={ {0}, {0}, {0} };
GLfloat x=100.0; // Pivot point
GLfloat y=100.0; // Pivot point
GLfloat theta;
```

/ Rotation MATRIX and Object Matrix => Resultant Transformed House */*

```
void multiply()
{
    int i,j,k;
    for(i=0;i<3;i++)
    for(j=0;j<9;j++)
    {
        result[i][j]=0;
        for(k=0;k<3;k++)
            result[i][j]=result[i][j]+rot_mat[i][k]*house[k][j];
    }
}
```

// Build the rotation matrix

```
void rotate()
```

```
{
```

```
    GLfloat m,n;
```

```
    m=x-(x*cos(theta))+(y*sin(theta)); // m=-xcosθ + ysinθ + x
```

```
    n=y-(x*sin(theta))-(y*cos(theta)); // n -xsinθ - y cosθ + y
```

```
    rot_mat[0][0]=cos(theta);
```

```
    rot_mat[0][1]=-sin(theta);
```

```
    rot_mat[0][2]=m;
```

```
    rot_mat[1][0]=sin(theta);
```

```
    rot_mat[1][1]=cos(theta);
```

```
    rot_mat[1][2]=n;
```

```
    rot_mat[2][0]=0;
```

```
    rot_mat[2][1]=0;
```

```
    rot_mat[2][2]=1;
```

```
    multiply();
```

```
}
```

```
void drawhouse()
{
    glColor3f(0.0, 0.0, 1.0);
    glBegin(GL_LINE_LOOP);
        glVertex2f(house[0][0],house[1][0]);
        glVertex2f(house[0][1],house[1][1]);
        glVertex2f(house[0][3],house[1][3]);
        glVertex2f(house[0][4],house[1][4]);
    glEnd();

    glColor3f(1.0,0.0,0.0);
    glBegin(GL_LINE_LOOP);
        glVertex2f(house[0][5],house[1][5]);
        glVertex2f(house[0][6],house[1][6]);
        glVertex2f(house[0][7],house[1][7]);
        glVertex2f(house[0][8],house[1][8]);
    glEnd();
}
```



```
glColor3f(0.0, 0.0, 1.0);  
glBegin(GL_LINE_LOOP);  
    glVertex2f(house[0][1],house[1][1]);  
    glVertex2f(house[0][2],house[1][2]);  
    glVertex2f(house[0][3],house[1][3]);  
glEnd();  
}
```

```
void drawrotatedhouse()
{
    glColor3f(0.0, 0.0, 1.0);
    glBegin(GL_LINE_LOOP);
        glVertex2f(result[0][0],result[1][0]);
        glVertex2f(result[0][1],result[1][1]);
        glVertex2f(result[0][3],result[1][3]);
        glVertex2f(result[0][4],result[1][4]);
    glEnd();

    glColor3f(1.0,0.0,0.0);
    glBegin(GL_LINE_LOOP);
        glVertex2f(result[0][5],result[1][5]);
        glVertex2f(result[0][6],result[1][6]);
        glVertex2f(result[0][7],result[1][7]);
        glVertex2f(result[0][8],result[1][8]);
    glEnd();
}
```

```
glColor3f(0.0, 0.0, 1.0);  
glBegin(GL_LINE_LOOP);  
    glVertex2f(result[0][1],result[1][1]);  
    glVertex2f(result[0][2],result[1][2]);  
    glVertex2f(result[0][3],result[1][3]);  
glEnd();  
}
```

```
void display()
{
    glClear(GL_COLOR_BUFFER_BIT);
    drawhouse();
    rotate();
    drawrotatedhouse();
    glFlush();
}
```

```
void myinit()
{
    glClearColor(1.0,1.0,1.0,1.0);
    glColor3f(1.0,0.0,0.0);
    glMatrixMode(GL_PROJECTION);
    glLoadIdentity();
    gluOrtho2D(0.0,499.0,0.0,499.0);
}
```

```
void main(int argc, char** argv)
{
    printf("Enter the rotation angle\n");
    scanf("%f", &theta);
    theta=(3.14/180)*theta;
    glutInit(&argc,argv);
    glutInitDisplayMode(GLUT_SINGLE|GLUT_RGB);
    glutInitWindowSize(500,500);
    glutCreateWindow("house rotation");
    glutDisplayFunc(display);
    myinit();
    glutMainLoop();
}
```