

Aim:

You are required to write a C program that computes the shortest paths from a source vertex to all other vertices in a weighted, directed graph. The program should utilize Dijkstra's algorithm to solve this problem.

The program must perform the following tasks:

Input the Number of Vertices:

- Print: "Enter the number of vertices: "
- Read an integer V representing the number of vertices in the graph.

Input the Adjacency Matrix:

- Print: "adjacency matrix:"
- For each pair of vertices (i, j) , print: "Weight from i to j : "
- Read the weight of the edge between vertex i and vertex j . If there is no edge between them, input 0.

Input the Source Vertex:

- Print: "Enter the source vertex: "
- Read the source vertex src.

Validation:

- Ensure that the number of vertices does not exceed 100. If it does, print: "Number of vertices exceeds maximum allowed (100)" and exit the program.
- Ensure that the source vertex is within the valid range (0 to $V-1$). If it is not, print: "Invalid source vertex" and exit the program.

Compute Shortest Paths:

- Use Dijkstra's algorithm to compute the shortest paths from the source vertex to all other vertices.

Note: Refer to sample test cases for better understanding

Source Code:

Path.c

```
#include <stdio.h>
#include <limits.h>
#include <stdbool.h>

#define MAX_V 100

int minDistance(int dist[], bool sptSet[], int V) {

    // Write your code here...
    int min = INT_MAX, min_index = -1;
    for(int v = 0; v<V; v++){
        if(!sptSet[v] && dist[v] <= min){
            min = dist[v];
            min_index = v;
        }
    }
}
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        return min_index;
    }

void printSolution(int dist[], int V) {
    printf("Vertex \t Distance from Source\n");
    for (int i = 0; i < V; i++) {
        printf("%d \t %d\n", i, dist[i]);
    }
}

void dijkstra(int graph[MAX_V][MAX_V], int src, int V) {

    // Write your code here...
    int dist[MAX_V];
    bool sptSet[MAX_V];

    for(int i = 0; i<V; i++){
        dist[i] = INT_MAX;
        sptSet[i] = false;
    }

    dist[src] = 0;

    for(int count = 0; count < V - 1; count++){
        int u = minDistance(dist, sptSet, V);
        if(u == -1){
            break;
        }
        sptSet[u] = true;
        for(int v = 0; v<V; v++){
            if(!sptSet[v] && graph[u][v] > 0 && dist[u]!= INT_MAX && dist[u] + graph[u][v] < dist[v]){
                dist[v] = dist[u] + graph[u][v];
            }
        }
    }

    printSolution(dist,V);
}

int main() {
    int graph[MAX_V][MAX_V];
    int V, src;

    printf("number of vertices: ");
    scanf("%d", &V);

    if (V > MAX_V) {
        printf("Number of vertices exceeds maximum allowed (%d)\n", MAX_V);
        return 1;
    }

    for (int i = 0; i < V; i++) {

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        for (int j = 0; j < V; j++) {
            graph[i][j] = 0;
        }
    }

    printf("adjacency matrix:\n");
    for (int i = 0; i < V; i++) {
        for (int j = 0; j < V; j++) {
            printf("Weight from %d to %d: ", i, j);
            scanf("%d", &graph[i][j]);
        }
    }

    printf("Enter the source vertex: ");
    scanf("%d", &src);

    if (src < 0 || src >= V) {
        printf("Invalid source vertex\n");
        return 1;
    }

    dijkstra(graph, src, V);

    return 0;
}

```

Execution Results - All test cases have succeeded!

Test Case - 1	
User Output	
number of vertices:	3
adjacency matrix:	0
Weight from 0 to 0:	0
Weight from 0 to 1:	5
Weight from 0 to 2:	10
Weight from 1 to 0:	5
Weight from 1 to 1:	0
Weight from 1 to 2:	2
Weight from 2 to 0:	10
Weight from 2 to 1:	2
Weight from 2 to 2:	0
Enter the source vertex:	0
Vertex	Distance from Source
0	0
1	5
2	7