

THE SLOPE OF THE CLUSTER ELLIPTICAL RED SEQUENCE: A PROBE OF CLUSTER EVOLUTION

MICHAEL D. GLADDERS,^{1,2} OMAR LÓPEZ-CRUZ,^{1,3,4} H. K. C. YEE,^{1,4} AND TADAYUKI KODAMA⁵

Received 1997 December 5; accepted 1998 February 18

ABSTRACT

The current formation models for cluster elliptical galaxies, which incorporate a mechanism for the metallicity enhancement of massive elliptical galaxies, predict a change in the observed slope of the red sequence of elliptical galaxies as a function of redshift. This change occurs primarily because the metal-rich galaxies become redder faster than the more metal-poor galaxies with increasing age. This effect is most pronounced within ~ 4 Gyr of formation. Observations of the change of the slope of the red sequence with redshift may thus be used to constrain the formation epoch for galaxy clusters. We examine the red sequence of cluster elliptical galaxies using publicly available *Hubble Space Telescope* imaging data for a set of six $0.75 > z > 0.2$ clusters and a sample of 44 Abell clusters at $z < 0.15$, imaged with the KPNO 0.9 m. We compare the derived slopes of the red sequences with a set of cluster elliptical evolution models and find good agreement. We demonstrate that such a comparison provides a useful constraint on the formation epoch for clusters, which can be made independently from considerations of absolute color evolution and scatter in the red sequence. From our initial comparison of the observed and model slopes as a function of redshift, we conclude, conservatively, that most of the elliptical galaxies in the cores of clusters must form at $z > 2.0$ and that these galaxies are coeval and passively evolving.

Subject headings: galaxies: clusters: general — galaxies: elliptical and lenticular, cD — galaxies: evolution — galaxies: formation — galaxies: photometry — galaxies: stellar content

1. INTRODUCTION

The existence of a color-magnitude relation (CMR) for field elliptical galaxies, in which the brighter elliptical galaxies are in general redder, was first noted by Baum (1959). Locally, the elliptical galaxies in individual clusters form a red sequence with a well-defined slope and small scatter (Bower et al. 1992a, 1992b). Recent results from the *Hubble Space Telescope* (HST) demonstrate the existence of a tight red sequence, comparable in scatter and slope to that observed in the red sequence of the Coma Cluster, in clusters at redshifts up to $z = 0.9$ (Stanford, Eisenhardt, & Dickinson 1998, hereafter SED98; Ellis et al. 1997, hereafter E97). Although the CMR in clusters can be interpreted at the present epoch as either an age effect or a metallicity effect, the existence of the red sequence at redshifts greater than 0.3 makes the age explanation untenable (Kodama 1997, hereafter K97). Specifically, the existence of the red sequence at higher redshifts indicates that cluster elliptical galaxies are a passively evolving population in which the reddening of massive galaxies is the result of a mass-metallicity relation rather than an age effect (Kodama & Arimoto 1997; Kauffmann & Charlot 1998; K97).

The apparent passive evolution of cluster elliptical galaxies is broadly consistent with models in which elliptical galaxies form in a monolithic collapse at high redshift and evolve passively after this initial starburst (Eggen, Lynden-

Bell, & Sandage 1962). The origin of the mass-metallicity relation in this collapse scenario was first explored in detail by Arimoto & Yoshii (1987), who included the effects of supernova winds (Larson 1974). The heating of the interstellar medium by supernovae in the initial starburst triggers the formation of a galactic wind when the thermal energy of the gas exceeds the gravitational binding energy. This galactic wind ejects the gas in low-mass galaxies more efficiently because of their shallower potential wells, resulting in a trend of increasing metallicity with mass (e.g., Carlberg 1984a, 1984b). The more massive galaxies are more likely to retain the enriched supernova ejecta and have starbursts of longer duration.

The initial enrichment difference between elliptical galaxies of different masses is manifested in the present epoch as the slope of the red sequence, which appears to be constant from cluster to cluster (Lopez-Cruz & Yee 1998; Lopez-Cruz 1997, hereafter LC97). However, this mass-metallicity relation causes elliptical galaxies of different masses to display slightly differing photometric properties with age. This differing color evolution is manifested as a change in the slope of the red sequence with redshift. In a scenario in which elliptical galaxies in the cores of clusters form concurrently in a monolithic collapse at high redshift, we expect the observed slope of the red sequence to be significantly flatter at ages less than ~ 4 Gyr after formation (K97; Kodama & Arimoto 1997) when compared to later times.

An alternative explanation for the origin of the slope of the red sequence is provided by Kauffmann & Charlot (1998), in which elliptical galaxies are formed hierarchically through the merger of disk systems. In this model there is again a mass-metallicity relation for the progenitor disk systems, and the enrichment occurs prior to the assembly of elliptical galaxies. Massive elliptical galaxies tend to form from the more massive disk systems in hierarchical merging,

¹ Department of Astronomy, University of Toronto, Toronto, ON M5S 3H8, Canada; gladders@astro.utoronto.ca, hyee@astro.utoronto.ca.

² Guest User, Canadian Astronomy Data Center, which is operated by the Dominion Astrophysical Observatory for the National Research Council of Canada's Herzberg Institute of Astrophysics.

³ Instituto Nacional de Astrofísica, Óptica y Electrónica (INAOE), Tonantzintla, Puebla, México; omar@inaoe.mx.

⁴ Visiting Astronomer, Kitt Peak National Observatory, which is operated by AURA, Inc., under contract to the National Science Foundation.

⁵ Institute of Astronomy, Madingley Road, Cambridge CB3 0HA, England, UK; kodama@ast.cam.ac.uk.

TABLE 1
THE KPNO SUBSAMPLES

| z Range | Clusters |
|--------------------|--|
| 0.0232..... | Coma (A1656) |
| 0.0414–0.0622..... | A85, A154, A168, A407, A671, A957, A1213, A1291, A1795, A1913, A1983, A2256, A2271, A2399, A2415, A2593, A2626, A2657 |
| 0.0715–0.0852..... | A399, A401, A415, A514, A690, A1569, A1650, A1775, A2029, A2255, A2410, A2420, A2597, A2670, |
| 0.0904–0.1161..... | A21, A84, A98, A2244, A2356, A2384, A2440, A2554 |
| 0.1303–0.1470..... | A629, A646 A1413 A2328 |

resulting in a mass-metallicity relation for elliptical galaxies. In this model the observed slope of the red sequence is also expected to flatten at high redshifts, because the stellar populations in massive elliptical galaxies are on average younger and become bluer relative to low-mass systems as the formation epoch is approached.

In theory, then, the change in the slope of the red sequence with redshift can be used to constrain the formation epoch of the dominant stellar population in elliptical galaxies (K97; LC97). This constraint can be made independently of the intrinsic scatter in early-type galaxy colors about the red sequence (Bower et al. 1992a, 1992b; Stanford, Eisenhardt, & Dickinson 1995; E97; SED98) and the evolution of the apparent color with redshift (Aragón-Salamanca et al. 1993; K97; E97; SED98; Kodama et al. 1998). The measurement of the slope offers a significant advantage over measurements of color and scatter in that it is calibration-independent. The slope can be measured with the same precision, even in the presence of large systematic errors in photometric zero points.

In this paper we present an analysis of the slopes of the red sequences for a total of 50 clusters spanning the redshift range $0 < z < 0.75$, and we demonstrate that such an analysis offers a powerful tool in constraining the formation epoch of elliptical galaxies in clusters. Our data are drawn from two sources: a subset of the imaging survey of LC97 of 45 Abell clusters at $z < 0.2$ and six clusters at $z > 0.2$ drawn from the *HST* archive. We consider only the interior 0.5 Mpc of each cluster and select early-type galaxies in the high-redshift sample, using an automated galaxy classifier based on central concentration (see Abraham et al. 1994). In § 2 we define the imaging data set in detail and discuss the galaxy photometry and morphology parameters derived from these data. In § 3 we present our analysis of the red-sequence slopes in these clusters; we compare these results to the models of K97 in § 4. In § 5 we summarize our conclusions and comment on the applicability of this analysis to even higher redshift observations. We use $H_0 = 50$, $\Omega_m = 1.0$, and $\Omega_\Lambda = 0.0$ throughout this paper, unless otherwise noted.

2. THE DATA

2.1. The KPNO Sample

The low-redshift data for this paper are taken from the KPNO 0.9 m survey of 45 Abell clusters of LC97. This is a three-color (B , R , and I) wide-field ($23' \times 23'$) survey of high Galactic latitude ($|b| \geq 30$), X-ray-luminous clusters at $z \leq 0.2$. Details of the data reduction and a more comprehensive analysis of the CMR for each cluster can be found in Lopez-Cruz & Yee (1998). In this paper, we use only the B and R photometry for all but one of these clusters to derive the color-magnitude diagram (CMD) of the

inner 0.5 Mpc radius of each cluster. We have excluded the highest redshift cluster (A665, $z = 0.18$) in the survey, as the data do not provide accurate photometry for all but the brightest members of this cluster. The remaining 44 clusters have been binned into five subsamples in redshift; the identification of the clusters in each subsample is given in Table 1.

2.2. The *HST* Sample

The *HST* data used in this paper have all been drawn from the *HST* archive. We selected six clusters for this study, requiring that each have deep Wide-Field Planetary Camera 2 (WFPC2) imaging in at least two bandpasses and spanning as large a redshift range as possible within this constraint. The specifics of these observations are presented in Table 2. In all cases, the F814 image is the deepest and is complemented by a deep F555 image for four clusters at $z < 0.6$ and an F606 image for the two at $z \approx 0.75$. The data have been processed using the Canadian Astronomical Data Centre standard WFPC2 pipeline, utilizing the most up-to-date calibration frames available. We have not attempted to correct for charge transfer efficiency effects (see Holtzman et al. 1995), as this effect is position-dependent and has little effect on colors measured between two frames at the same position. The individual exposures for each field have been shifted and combined using a σ -clipping algorithm to reject cosmic rays and hot pixels. For clusters where there are no offsets between the frames, a bad-pixel map has been used to eliminate hot pixels from consideration in the photometry and morphological analysis.

2.3. Photometry

The photometry for both the KPNO and the *HST* imaging data has been computed using the Picture Processing Package (PPP; Yee 1991). PPP is an integrated photometry system that performs object finding and computes photometry parameters based on an analysis of the curve of growth for each object. In all cases, the redder

TABLE 2
THE *HST* SUBSAMPLE

| Cluster | z | F814 | F606 | F555 |
|--------------------|---------------------|-------|-------|-------|
| A2390 | 0.2279 ^a | 10500 | ... | 8400 |
| CL 2244–0221 | 0.33 ^b | 12600 | ... | 8400 |
| CL 0016+1609 | 0.5479 ^a | 16800 | ... | 12600 |
| J1888.16CL | 0.560 ^b | 16800 | ... | 12600 |
| GHO 1322+3114..... | 0.755 ^c | 20800 | 10800 | ... |
| GHO 1322+3027..... | 0.757 ^c | 32000 | 16000 | ... |

^a Yee, Ellingson, & Carlberg 1996.

^b SED98.

^c Castander et al. 1994.

image for each cluster was used to find objects, and each frame has been examined individually to confirm the reliability of the object finding. PPP reliably separates stars from galaxies by reference to the curve of growth of a set of reference stars, and we have excluded all objects identified by PPP as stars. This classification has been visually checked for all bright objects in the KPNO data, as bright stars can be misclassified because of variations in the point-spread function at the edges of the field. The magnitudes used here are total magnitudes (see Yee 1991 and LC97 for details). A standard metric aperture of 11 kpc was used when computing colors for the KPNO data at $z < 0.06$ and all the *HST* data. For the KPNO data at $z > 0.06$, we have used a fixed observed aperture of 6", corresponding to ≈ 21 kpc at $z = 0.15$. The larger observed apertures have been used in the KPNO data for clusters at $z > 0.06$, because the 11 kpc metric aperture is too small relative to the seeing disk to allow for a reliable color determination. However, the difference in apertures is insignificant, as the color gradients in elliptical galaxies are very small (Peletier et al. 1990), and the variation this induces in the expected slope of the red sequence is negligible (K97).

The KPNO imaging data have the added complication of containing a large number of clusters with massive cD galaxies. These galaxies have been treated individually by isophote modeling (Brown 1997) and removed from the cluster images prior to the computation of photometry on all other objects in the field. This avoids the difficulty of computing the background for objects within the extended cD halos.

2.4. Morphological Classification

The CMDs for the higher redshift clusters in our sample are significantly contaminated by field galaxies along the line of sight. Because the slope of the red sequence is well determined only when this background contamination is minimal, we have used morphological classification to select only the early-type population. Dressler et al. (1994) have demonstrated that *HST* images have sufficient resolution to allow reliable classification of galaxy morphologies at high redshift. More recently, E97 have used this to identify the E/S0 population in three clusters at $z \approx 0.55$. In this paper we attempt a similar procedure to isolate the early-type galaxies in the *HST* subsample, with the aim of improving the signal of the red sequence in the CMD. Following the prescription of Abraham et al. (1994), we use central concentration as our primary classification tool. The concentration index, C , is defined as the ratio of the flux in the central third of the object to the total flux contained within the 2σ isophote. We chose to use the object magnitude rather than surface brightness (as adopted by Abraham et al. 1994) as our secondary classification criterion in the "classification plane" (see Fig. 1a).

To isolate the red sequence in the *HST* subsample most optimally, we proceeded as follows: First, we made a cut in the concentration-magnitude plane and examined the CMD resulting from concentrated objects selected by this cut. In all cases, the red sequence was apparent. We then defined the "red-sequence region" in the CMD and examined the position of *all* objects in the region in the classification plane. We next made a new cut in the classification plane that best separated the two groups (see Fig. 1a). Objects that passed this second cut were then individually examined, and galaxies that were obviously not E/S0 galaxies were excluded. This visual examination excluded

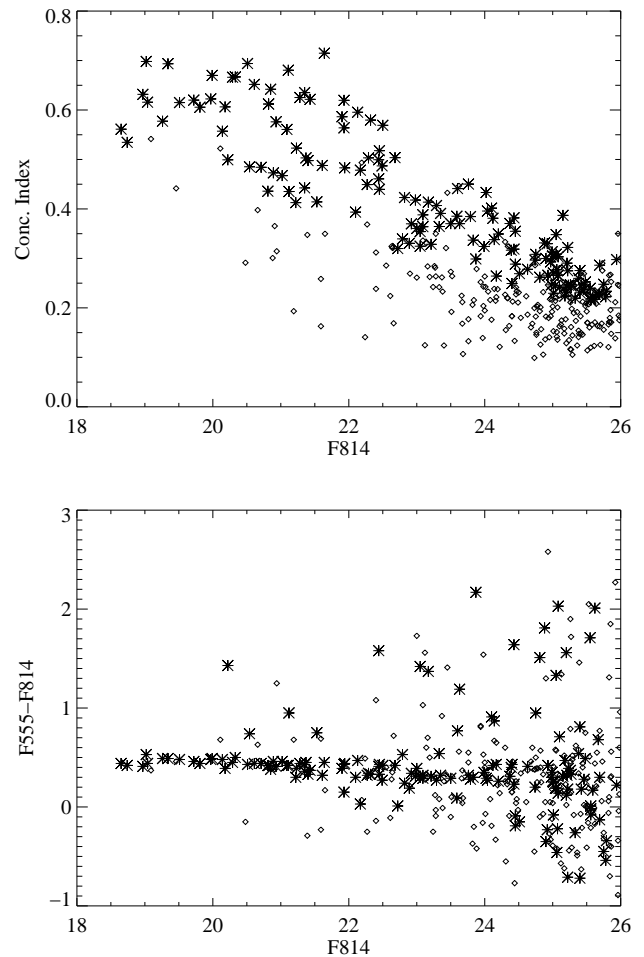


FIG. 1.—(Upper panel) Classification plane (concentration index vs. magnitude) for morphological selection of galaxies in A2390. All objects above the cut line (asterisks) have been used in the CMD fitting procedure described in the text. (Lower panel) CMDs for all objects (diamonds) and a morphologically selected subset (asterisks) of objects in A2390. Note that the restriction of the sample to those objects with a high central concentration enhances the visibility of the red sequence, particularly at the faint end.

$\approx 10\%$ of the remaining objects. These excluded objects were typically spiral galaxies with concentrated central bulges or crowded objects. The final subset of concentrated objects is composed predominantly of early-type galaxies, and in all cases the visibility of the red sequence in the cluster CMD was strongly enhanced (see Fig. 1b).

2.5. Color-Magnitude Diagrams

As we are interested in only the early-type cluster members, we have used only the inner 0.5 Mpc projected radius of each cluster to construct its CMD. This reduces the relative contamination of the CMD by field objects (particularly important for the highest redshift clusters), since we are examining the density peak of the cluster. Furthermore, the cores of clusters are in general dominated by early-type galaxies (Dressler 1980). Recent analysis of several clusters at $z \approx 0.55$ (Dressler et al. 1997) shows a paucity of S0 galaxies in the cores of rich clusters, relative to a well-established, centrally concentrated population of elliptical galaxies. We have made no attempt to segregate the E and S0 populations morphologically, but we expect that the restricted field size used here favors elliptical gal-

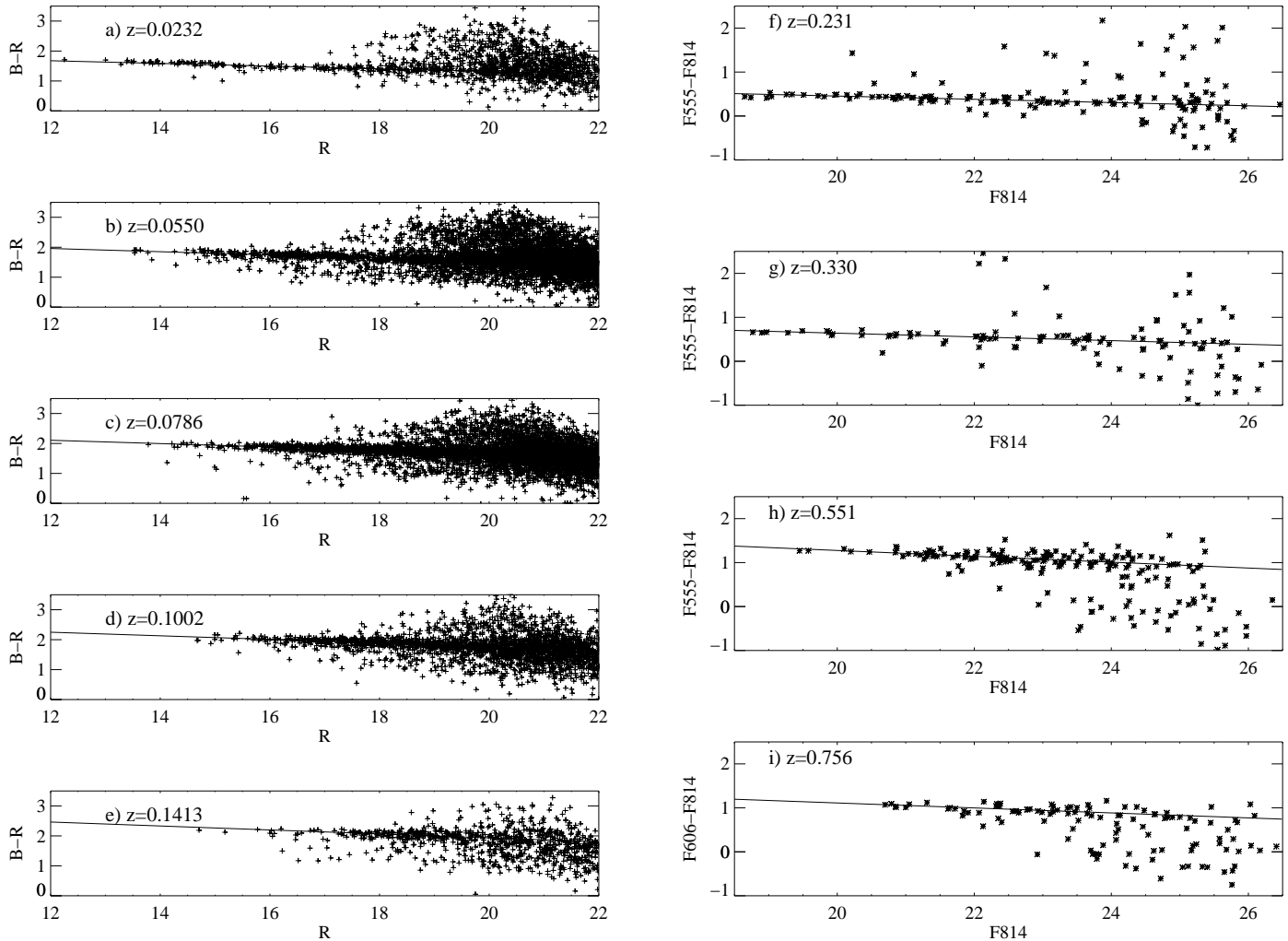


FIG. 2.—Combined CMDs for the KPNO subsample, consisting of data for 36,385 galaxies (a–e) and the *HST* morphologically selected subsample, consisting of data for 555 galaxies (f–i). The best-fitting red sequences are shown as solid lines.

axies over S0 galaxies. Notably, Bower et al. (1992b) and E97 found no discernible difference between the slope and zero point of the red sequences of cluster E and S0 galaxies at $z \approx 0$ and $z \approx 0.55$, respectively, so the inclusion of some S0 galaxies is unlikely to have a significant effect. Ellingson et al. (1998) have performed a principal-component analysis of the spectra of cluster members for 14 clusters in the CNOC1 survey and find an increase in the Balmer component of the spectra only at radii comparable to, or greater than, r_{200} , the radius at which the average interior density for the cluster is $\approx 200\rho_c$, where ρ_c is the critical density. Ellingson et al. interpret this increase in the Balmer component as the signature of recent star formation, truncated by infall into the intercluster medium. Following Carlberg et al. (1997), the expected value of r_{200} for a cluster at $z = 0.75$, with a velocity dispersion $\sigma_c = 800 \text{ km s}^{-1}$, is $\approx 1 \text{ Mpc}$, well beyond the 0.5 Mpc radius used here. The observation that there is no significant spectroscopic evidence for recent star formation in S0 galaxies in the cores of clusters is also consistent with Van Dokkum et al. (1998), who found a blueing of the S0 population in CL 1358 + 62 ($z = 0.33$) only at radii greater than $0.7 h_{50}^{-1} \text{ Mpc}$. We thus expect our sample to be dominated by elliptical galaxies, with a contribution from quiescent S0 galaxies with no

remnant signature of star formation. Moreover, the inclusion of a small population of quiescent S0 galaxies is not expected to affect our slope measurements significantly, because an S0 galaxy that ceases star formation in the disk will enter the red sequence within a few Gyr (Bower, Kodama, & Terlevich 1998) and be indistinguishable from an elliptical.

The 44 clusters in the KPNO subsample have been subdivided into five redshift groups, and the CMDs ($B-R$ vs. R , in all cases) for all clusters in each group have been combined. Three corrections have been applied to the individual CMDs prior to combination. First, we have applied Galactic extinction corrections, using the maps and tabulations of Burstein & Heiles (1982, 1984). Second, we have corrected the colors using the fit to the red sequence $B-R$ color versus redshift of LC97: this is essentially an empirically determined color K -correction. Third, we have corrected the R -band magnitudes to a common absolute magnitude, considering only cosmological effects with no K -correction. This correction to a common absolute magnitude is sufficient, as the total spread in redshift in each group is only ≈ 0.02 .

The CMDs for the two pairs of the highest redshift clusters with *HST* data have also been combined. To combine

J1888.16CL with CL0016+1609, we have applied the color correction from E97 of -0.025 mag to the CMD of J1888.16CL. We have combined the CMDs of GHO 1322+3027 and GHO 1322+3114 directly, because the Galactic extinction for these two clusters is the same and their redshifts are only marginally different.

The final combined CMDs for both subsets of the data are shown in Figures 2*a*–2*i*. In each combined set, the red sequence is apparent. There is significant contamination of the CMD by non-red-sequence objects in the KPNO subsample, but the large number of clusters in each group adequately compensates for this.

3. RED-SEQUENCE SLOPES

We have computed the red-sequence slopes for our CMD sample using both standard linear regression and a method based on minimizing the absolute deviation (Press et al. 1992). The minimization of the least absolute deviation is expected to be more robust in the presence of outliers. The estimated color errors were used to weight the data for all fits. We have investigated the two above methods in conjunction with σ clipping about the red sequence to exclude obvious outliers, and have found that linear regression plus an iterated 3 σ clip provided the most stable results. All results discussed below were produced using this fitting technique.

Specifically, the fits to each CMD reported in Table 3 were computed as follows: First, a limiting magnitude was selected for each CMD, under the condition that the red sequence be apparent up to this limit. An initial estimate of the fit was then made in a visually selected subregion of the CMD containing the red sequence. The CMD was rectified by this fit, and the color distribution of *all* objects in the color-corrected CMD was computed. A Gaussian was then fitted to the color peak corresponding to the red sequence, and only points less than 3 σ from the peak were used to construct a new red-sequence fit. This process was iterated until convergence on a final solution was obtained. We have investigated the sensitivity of this solution to reasonable choices of limiting magnitude and initial fit and found no significant deviations from our final fits in all cases. The final errors on the slopes reported in Table 3 were estimated by a bootstrap analysis of our fitting procedure. For CMDs comprising data from more than one cluster, the effective redshift is estimated as the mean of the cluster redshifts in the subsample, weighted by the number of galaxies from each cluster in the final fitted region of the CMD.

4. CLUSTER FORMATION TIME

We have chosen to compare our derived red-sequence slopes to the models of K97. We make no detailed comparison to the hierarchical-clustering-based model of Kauffmann & Charlot (1998), because they do not provide sufficiently detailed predictions of the red-sequence slopes in the different bandpasses used here to allow such a comparison.

The models of K97 are normalized to reproduce the slope of the red sequence in the Coma Cluster (A1656) observed by Bower et al. (1992b), and we use that normalization here. We use the models of K97 to correct our observed slopes in various colors to a common color, which allows us to make a comparison of all the observed slopes to the models in a single color. We have chosen to correct all the slopes to the F555–F814 versus F814 slopes of the intermediate-redshift sample. This is done by correcting the observed slope by the change between the model slopes at the observed and adopted bandpasses. This correction assumes that the difference between the model and observed slopes is independent of wavelength. It should be noted that this assumption is correct only to first order, but it should be essentially true over a small range of wavelengths. Our main results hinge upon observations of the highest redshift clusters, where the change in bandpasses is small (F606–F814 vs. F555–F814), so this correction is sufficient and does not affect our conclusions. We have corrected to a single color primarily to allow for a comprehensive examination of the whole sample.

The comparison of our observed red-sequence slopes to a suite of four models with different formation epochs is presented in Figure 3. The overall slope of the red sequence seems to be consistent with passive evolution for all clusters, implying that the population we have sampled have similar evolutionary histories and timescales. We note that the observed slopes for the 46 clusters below redshift 0.35 are all consistent with the models, implying that the mass-metallicity relation used is reasonable. The observed slopes of the higher redshift clusters are perfectly consistent with a high formation redshift, and a conservative limit of $z \geq 2$ can be set. Note that, up to redshifts of $z \approx 0.4$, observations of the slope of the red sequence have little power to distinguish between formation epochs with $z \geq 1.0$. The change in slope at $z \leq 0.4$ is exclusively due to blueshifting of the rest-frame bandpasses. However, beyond $z \approx 0.5$, the expected slopes for the lowest formation epoch models rapidly diverges from the observed slopes. This turnover is a

TABLE 3
THE COMBINED CMD SAMPLE

| CMD | z | Δz | Slope | Δ Slope |
|---------------------------------------|--------|------------|-----------|----------------|
| A1656 | 0.0232 | ... | -0.0450 | 0.0029 |
| KPNO 1 | 0.0550 | 0.0068 | -0.0539 | 0.0018 |
| KPNO 2 | 0.0786 | 0.0042 | -0.0558 | 0.0021 |
| KPNO 3 | 0.1002 | 0.0076 | -0.0596 | 0.0034 |
| KPNO 4 | 0.1413 | 0.0054 | -0.0662 | 0.0047 |
| A2390 | 0.2279 | ... | -0.0370 | 0.0041 |
| CL 2244–0221 | 0.330 | ... | -0.0423 | 0.0042 |
| J1888.16CL and CL 0016+1609 | 0.551 | 0.008 | -0.0666 | 0.0067 |
| GHO 1322+3114 and GHO 1322+3027 | 0.756 | 0.001 | -0.0566 | 0.0066 |

NOTE.—The KPNO subsample is divided into four groups + Coma (A1656); see Table 1 for details. Slopes are given in the original observed bandpass.

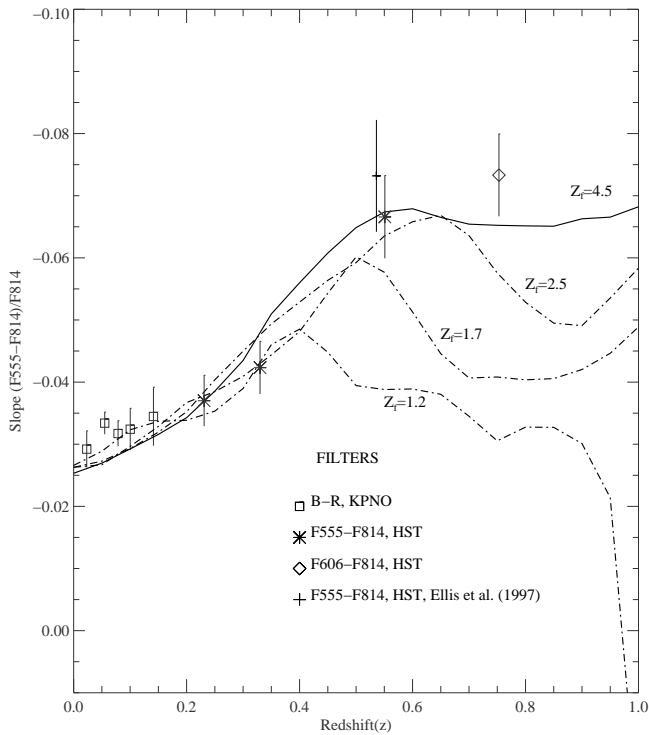


FIG. 3.—Comparison of observed red-sequence slopes and the predicted slopes from models with different formation epochs. The cosmology used here, to map the age onto redshift, is $H_0 = 50$, $\Omega_m = 1.0$, and $\Omega_\Lambda = 0.0$. For comparison, we also plot the measured slope for the combined CMD of CL 0016 + 1609, J1888.16CL, and CL 0412-65 from E97 and note that our measured slope is perfectly consistent with it.

result of the differing metallicities in the elliptical population as a function of mass; at ages younger than ~ 4 Gyr, the color evolution of the stellar population in a metal-rich elliptical is significantly different from that of a more metal-poor elliptical (K97; Kodama & Arimoto 1997).

It should be noted that there is another model solution to the observed slopes that does not require cluster elliptical galaxies to form at $z \geq 2$. However, this solution requires a correlation to exist between formation age and galaxy mass, so that the less massive elliptical galaxies form later. We have investigated this possible solution in some detail, and we note that, while it is possible to produce the observed slopes with this model, it requires a very specific linear mass versus formation time relation (amounting to about a 1 Gyr delay in formation time over the observable 6 magnitudes of the red sequence) and a small scatter about that relation. In the overall parameter space of formation epoch, the mass versus formation time relationship slope, and the formation time scatter, this particular solution occupies a very small volume compared to the high-redshift formation scenario. In the absence of a strong physical motivation for expecting such a specific mass versus formation time relation, we prefer the high-redshift formation solution, with concurrent formation time for galaxies of different masses.

To investigate the sensitivity of our conclusion to cosmological effects, we have constructed an additional two suites of models with differing cosmologies: $H_0 = 65$, $\Omega_m = 0.1$, $\Omega_\Lambda = 0.0$ and $H_0 = 80$, $\Omega_m = 0.2$, $\Omega_\Lambda = 0.8$. The three suites of models all have similar overall ages, although the precise mapping of the ages to redshift is somewhat different in each. As can be seen in Figure 4, the differences between the

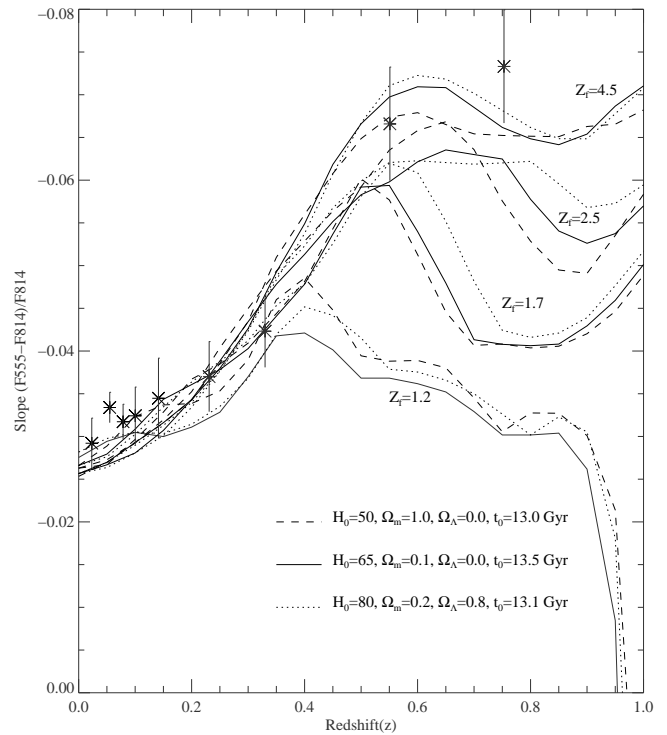


FIG. 4.—Predicted slopes for formation models using three different cosmologies to map age onto redshift. Note that while the details of the turnover in the slope for a model at a given formation redshift change slightly in different cosmologies, the change is not significant enough to affect the conclusion that at least some clusters form at $z > 2$.

predicted slopes in different cosmologies are minor, and we may thus parameterize the formation epoch as a formation redshift. We note that even in a cosmology of a quite different total age, we would still conclude that at $z = 0.75$ (the highest redshift in our sample), at least some clusters are older than ~ 4 Gyr.

We note that this result does not preclude the formation of some clusters at lower redshifts, as our sample may be preselected to examine a particular set of “old” objects (SED98). We may be simply observing the “oldest” objects at any particular epoch; it is not clear that the high-redshift clusters in our sample are in fact the antecedents of the low-redshift sample (Kauffmann & Charlot 1998). SED98 discuss this possibility in some detail, and they note that the results of Kauffmann & Charlot are derived for a $\Omega = 1$, cold dark matter universe and that, in a low- Ω open universe (Carlberg et al. 1996), clusters are assembled at significantly higher redshifts. It may also be possible that at $z > 0.5$ there is an envelope of red-sequence slopes, where some later forming clusters populate the turnover region. In most reasonable cosmologies, we would expect these later forming clusters to be generally less massive. Future observations of a large unbiased sample of clusters at $0.5 < z < 1.0$ might thus allow us to constrain the average formation epoch of clusters as a function of mass.

5. CONCLUSIONS

We have demonstrated that the slope of the red sequence, which can be determined to be independent of calibration, can be used to constrain the formation epoch of the early-type galaxies in the cores of rich clusters. We have computed the slopes of the red sequences for a total of 50

clusters, spanning the redshift range $0 < z < 0.75$. The data have been reduced and analyzed in a consistent manner for all clusters, in an effort to reduce systematic variations in the derived photometry. The low-redshift subsample uses large ensembles of clusters to strengthen the red-sequence signal; the sparser high-redshift *HST* data have been analyzed morphologically to similarly isolate the red sequence. We compare these observations to the latest galactic-wind models for monolithic formation of elliptical galaxies, and overall find good agreement. The observed slopes show no evidence for a turnover prior to $z = 0.75$, from which we conclude, conservatively, that at least some clusters must have formed at $z > 2$. Finally, we note that the change of the slope of the red sequence with redshift is a potentially powerful tool to discriminate between formation scenarios for cluster elliptical galaxies, particularly at redshifts greater than 0.75. A more thorough investigation of the formation history of cluster elliptical galaxies awaits the

identification and observation of a significant unbiased cluster sample at these redshifts.

M. D. G. thanks the Natural Sciences and Engineering Research Council of Canada for support through a PSGA graduate scholarship. O. L. C. thanks CONACyT-Mexico for an overseas scholarship for graduate studies at the University of Toronto, and INAOE-Tonantzintla for financial support. T. K. thanks the Japan Society for Promotion of Science (JSPS) Postdoctoral Fellowships for Research Abroad for supporting his stay at the Institute of Astronomy, Cambridge. H. Y. acknowledges support from NSERC of Canada via an operating grant. We are also grateful to the referee, J. M. Schombert, and the editor, G. Bothun, for helpful suggestions that improved the overall quality of the paper and, in particular, clarified our discussion of S0 contamination.

REFERENCES

- Abraham, R. G., Valdes, F., Yee, H. K. C., & van den Bergh, S. 1994, *ApJ*, 432, 75
Aragón-Salamanca, A., Ellis, R. S., Couch, W. J., & Carter, D. 1993, *MNRAS*, 262, 764
Arimoto, N., & Yoshii, Y. 1987, *A&A*, 173, 23
Baum, W. A. 1959, *PASP*, 71, 106
Bower, R., Kodama, T., & Terlevich, A. 1998, *MNRAS*, submitted
Bower, R., Lucey, J. R., & Ellis, R. S. 1992a, *MNRAS*, 254, 589
———. 1992b, *MNRAS*, 254, 601
Brown, J. P. 1997, Ph.D. thesis, Univ. Toronto
Burstein, D., & Heiles, C. 1982, *AJ*, 87, 1165
———. 1984, *ApJS*, 54, 33
Carlberg, R. G. 1984a, *ApJ*, 286, 403
———. 1984b, *ApJ*, 286, 416
Carlberg, R. G., Yee, H. K. C., Ellingson, E., Abraham, R. G., Gravel, P., Morris, S. L., & Pritchet, C. J. 1996, *ApJ*, 462, 32
Carlberg, R. G., et al. 1997, *ApJ*, 485, L13
Castander, F. J., Ellis, R. S., Frenk, C. S., Dressler, A., & Gunn, J. E. 1994, *ApJ*, 424, L79
Dressler, A. 1980, *ApJ*, 236, 351
Dressler, A., Oemler, A., Butcher, H. R., & Gunn, J. E. 1994, *ApJ*, 430, 107
Dressler, A., et al. 1997, *ApJ*, 490, 577
Eggen, O. J., Lynden-Bell, D., & Sandage, A. R. 1962, *ApJ*, 136, 748
Ellingson, E., et al. 1998, in preparation
Ellis, R. S., Smail, I., Dressler, A., Couch, W. J., Oemler, A., Butcher, H., & Sharples, R. M. 1997, *ApJ*, 483, 582 (E97)
Holtzman, J. A., Burrows, C. J., Casertano, S., Hester, J. J., Trauger, J. T., Watson, A. M., & Worthey, G. 1995, *PASP*, 107, 1065
Kauffmann, G., & Charlot, S. 1998, *MNRAS*, 294, 705
Kodama, T. 1997, Ph.D. thesis, Univ. Tokyo (K97)
Kodama, T., & Arimoto, N. 1997, *A&A*, 320, 41
Kodama, T., Arimoto, N., Barger, A. J., & Aragón-Salamanca, A. 1998, *A&A*, 334, 99
Larson, R. B. 1974, *MNRAS*, 169, 229
Lopez-Cruz, O. 1997, Ph.D. thesis, Univ. Toronto (LC97)
Lopez-Cruz, O., & Yee, H. K. C. 1998, in preparation
Peletier, R. F., Davies, R. L., Davis, L. E., Illingworth, G. D., & Cawson, W. 1990, *AJ*, 100, 1091
Press, W. H., Teukolsky, S. A., Vetterling, W. T., & Flannery, B. P. 1992, *Numerical Recipes: The Art of Scientific Computing* (2d ed.; Cambridge: Cambridge Univ. Press)
Stanford, S. A., Eisenhardt, P. R., & Dickinson, M. 1995, *ApJ*, 450, 512
———. 1998, *ApJ*, 492, 461 (SED98)
Van Dokkum, P. G., Franx, M., Kelson, D. D., Illingworth, G. D., Fisher, D., & Fabricant, D. 1998, *ApJ*, 500, 714
Yee, H. K. C. 1991, *PASP*, 103, 662
Yee, H. K. C., Ellingson, E., & Carlberg, R. G. 1996, *ApJS*, 102, 269