# seL4 Verification

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## **CONTENTS**

- 1. Overview of seL4
- 2. Isabelle/HOL: The Verification Powerhouse
- 3. Refinement technic
- 4. Translation validation
- **5.** Invariants
- **6.** Conclusion

# Overview of seL4

#### seL4

A minimalistic open source microkernel providing core OS services:

- Process and thread management
- Memory isolation via capabilities
- Secure inter-process communication (IPC)

#### **Key Features**

- Strong isolation: Programs run in "sandboxes," preventing interference.
- Optimized for resource-constrained devices.
- Supports ARM, x86, RISC-V architectures.
- Formally verified for functional correctness.

## **Applications in Critical Systems**

#### Widely used in high-stakes systems:

- 1. Aviation (e.g., Boeing, DARPA projects)
- 2. Medical devices (e.g., pacemakers)
- **3.** Cybersecurity (e.g., secure smartphones)
- 4. Autonomous vehicles
- **5.** Military systems (e.g., DARPA HACMS)
- **6.** Internet of Things (IoT)

#### Why seL4?

- Verified reliability: Guarantees no crashes or vulnerabilities.
- Ideal for life-critical and high-security applications.

**Verification**: Mathematical proof that the kernel adheres to its specification in all possible scenarios.

#### Why It Matters

- **Reliability**: Eliminates crashes, even in edge cases.
- **Security**: Prevents exploitable bugs.
- Certification: Meets standards like Common Criteria, DO-178C.
- Uniqueness: First fully verified general-purpose microkernel.

**Common Criteria** and **DO-178C** are standards for software security and safety certification.

#### Development

Developed by NICTA (Australia) starting in the 2000s. Completed in 2009, fully verified by 2014. [1]

Currently maintained by Data61, led by Gernot Heiser.

#### Code

Written in **C** (8,700 lines) and **assembly** (600 lines), totaling 9,300 lines verified using **Isabelle/HOL**.

**License**: GPLv2 for open source; commercial licenses available.

Source code available on GitHub

# Isabelle/HOL: The Verification Powerhouse

**Isabelle/HOL**: An interactive proof assistant using higher-order logic (HOL) for formal verification.

Isabelle based on ITP - Interactive Theorem Proving

#### **Key Features**

- **Interactive Proofs**: Combines human insight with machine-checked accuracy.
- **Higher-Order Logic**: Models complex systems like operating systems.
- Versatile: Verifies software, hardware, and protocols.

#### **How It Works**

- You define a program and its desired properties (e.g., "no errors").
- Write **proof scripts** to show the properties hold.
- Isabelle checks each step, ensuring correctness.

## **Example 1: Proving a Sum Function**

#### Goal

Prove a function  $sum\_upto(n)$  computes 1 + 2 + ... + n correctly.

in case clauses substitutes arg to formula from definition

#### **Explanation**

- Defines sum\_upto recursively.
- Proves it equals the formula n \* (n + 1) / 2 using induction.
- Isabelle checks each case (base and step).

#### base

```
sum_upto 0 = (0 * (0 + 1)) \text{ div } 2

0 * (0 + 1) \text{ div } 2 = 0
```

#### step

```
sum\_upto (Suc n) = ((Suc n) * (Suc n + 1)) div 2

Suc n + (n * (n + 1)) div 2 = ((Suc n) * (Suc n + 1)) div 2
```

#### Goal

Prove reversing a list preserves its length.

```
fun reverse :: "'a list ⇒ 'a list" where
    "reverse [] = []"
| "reverse (x # xs) = reverse xs @ [x]" # [x] + [y...z] = [z...y] + [x]

theorem reverse_length:
    "length (reverse xs) = length xs"
    proof (induction xs)
        case Nil show ?case by simp # case Nil when list is empty
        case (Cons x xs) thus ?case by simp # case [x] + xs
        qed
```

#### **Explanation**

- Defines reverse recursively: empty list stays empty; otherwise, move head to end.
- Proves length (reverse xs) = length xs using induction.
- Isabelle verifies base case (empty list) and step case (non-empty list).

This guarantees reverse doesn't add or lose elements.

#### base

```
length(reverse[]) = length[]
length [] = length []
```

#### step

```
length(reverse(x # xs)) = length(x # xs)
length(reverse xs @ [x]) = length(xs) + 1
length(reverse(xs)) + length([x]) = length(xs) + 1
```

## Why Isabelle is chosen?

As mentioned before, **Isabelle/HOL** uses ITP, which is perfect for a such large project as seL4 (10k LOC). Other methods of verification would take enormous amount of time and resources.

# REFINEMENT TECHNIC

## Approach

- Used **Isabelle/HOL** for machine-checked proofs.
- Proved functional correctness via refinement[2]:
  - Abstract spec → Executable spec → C code.
- Prototyped in Haskell for design clarity.

## **Refinement Layers**

- **Abstract**: Defines **what** (e.g., system calls).
- **Executable**: Details **how** (Haskell-derived).
- **Concrete**: C code (8,700 LOC).

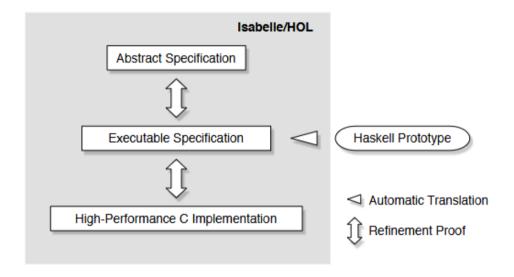


Figure 1: The refinement layers

## **Example: Abstract Scheduler**

## **Scheduler Specification**

The abstract specification defines **what** the scheduler does, not **how**.

```
schedule = do
  threads = all_active_tcbs;
  thread = select threads;
  switch_to_thread thread
od OR switch_to_idle_thread
```

- Rarely uses infinite type (like *nat*). Using 32-bit integers instead
- **Abstract types** (sets, lists, trees, etc.)
- Often non-deterministic: if there's several correct outputs fot an operation, this layer would return them all and make clear that there is a choice

## **Example: Executable Scheduler**

#### **Detailed Scheduler**

The executable specification adds **how** the scheduler works.

```
schedule = do
  action <- getSchedulerAction
  case action of
    ChooseNewThread -> do
      chooseThread
      setSchedulerAction ResumeCurrentThread
chooseThread = do
  r <- findM chooseThread' (reverse [minBound .. maxBound])
...</pre>
```

- Become deterministic
- Concrete data types (e.g. tree is now a double-linked list)
- Some fundamental restrictions (e.g. using 64bit to represent capabilities)

## Example: C Scheduler

## **C** Implementation

The final C code optimizes performance while matching the spec.

Its the most detailed layer. Written in a very large, pragmatic subset of C99

## What is prohibited

- *adress of* operator (&) on local variables because of an assumption that local variables are separate from stack. Using pointers to global variables instead
- function call through function pointers
- goto
- *switch* with fall-thgrouh cases
- unions

## The proof

A refinement proof establishes a correspondence between a high-level (abstract) and a low-level (concrete, or refined ) representation of a system.

The correspondence established by the refinement proof ensures that all Hoare logic properties of the abstract model also hold for the refined model.

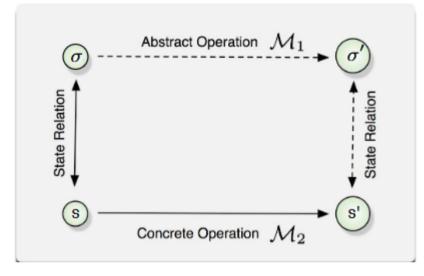


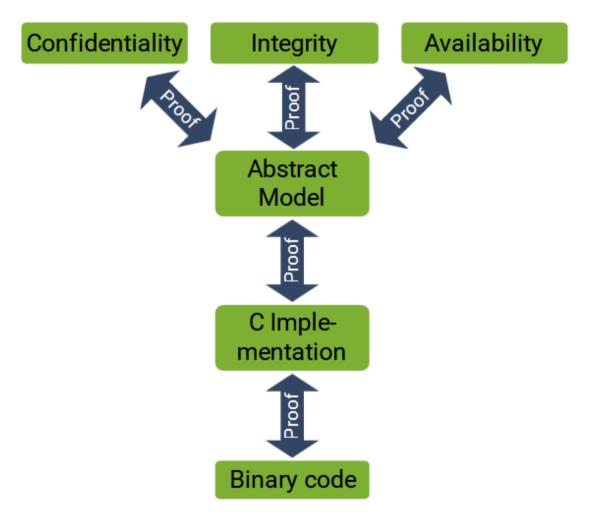
Figure 2: Forward simulation

#### **Forward Simulation**

To show that a concrete state machine M2 refines an abstract one M1, it is sufficient to show that for each transition in M2 that may lead from an initial state s to a set of states s', there exists a corresponding transition on the abstract side from an abstract state  $\sigma$  to a set  $\sigma'$  (they are sets because the machines may be non-deterministic)

The transitions *correspond* if there exists a relation R between the states s and  $\sigma$  such that for each concrete state in s' there is an abstract one in  $\sigma$ ' that makes R hold between them again

Proof chain



22/35

Figure 3: seL4 proof chain

#### Refinement of C

C is not a formal language; in order to allow reasoning about a C program in the theorem prover (we use Isabelle/HOL), it has to be transformed into mathematical logic (HOL).

This is done by a C parser written in Isabelle. The parser defines the semantics of the C program, and gives it meaning in HOL according to this semantics. It is this formalisation which we prove to be a refinement of the mathematical (abstract) model.

## Compiler's challenge

As already mentioned before, some features of C were restricted to get a subset of language with unambigious semantics.

However, this **does not guarantee** that our assumed semantics for that subset is the same as the compiler's.

Overall, we show that the behaviour of the C implementation is fully captured by the abstract specification. This is a strong statement, as **it allows us to conduct all further analysis of properties that can be expressed as Hoare triples on the massively simpler abstract specification instead of a complex C program**.

Coverage is complete. Any remaining implementation errors (deviations from the specification) can **only** occur **below the level of C** 

# TRANSLATION VALIDATION

#### Reason for binaries verification

In seL4 used GCC compiler which is itself a large, complex program that **may have bugs**. And when speaking about security systems, bugs are not the only problem, the compiler could also contain a **trojan** that automatically builds a back door when compiling an OS.

To protect against defective compilers, the executable binaries that are produced by the compiler are also verified

Specifically it is being proved, that the binary is a correct translation of the C code (which is already proved), and thus that the binary refines the abstract specification

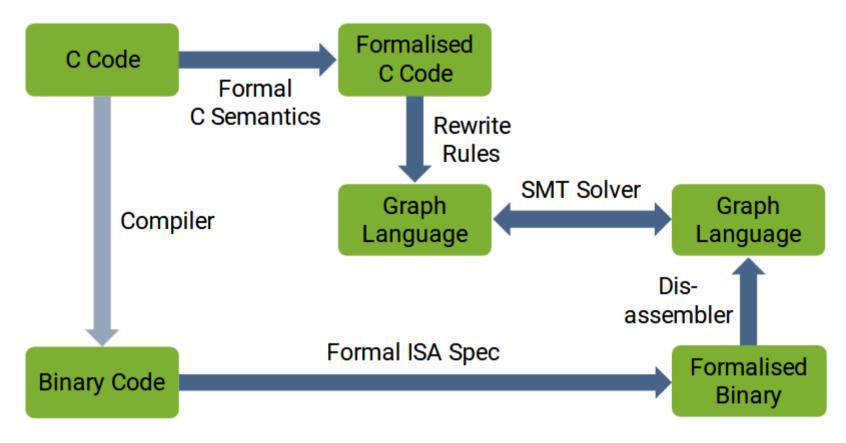


Figure 4: Translation validation proof chain

# **INVARIANTS**

As part of the refinement proof between layers, were introduced (and prooved) a large number of invariants (more than 150)

These invariants are not a proof device, but provide valuable information and assurance. In essence, they collect information about **what we know to be true** of each data structure in the kernel, before and after each system call, and also for large parts during kernel execution where some of these invariants **may be temporarily violated and reestablished later** 

The overall proof effort was clearly **dominated by invariant proofs**, with the actual refinement statements between abstract and executable specification accounting for at most 20 % of the total effort for that stage

There are **four main categories** of invariants in our proof: **low-level memory** invariants, **typing** invariants, **data structure** invariants, and **algorithmic** invariants.

## Invariants: low-level memory & typing

#### low-level

low-level memory invariants include that:

- there is no object at address 0
- kernel objects are aligned to their size, and that they do not overlap

## typing

The typing invariants say that each kernel object has a well-defined type and that its references in turn point to objects of the right type

**Example:** An example would be a capability slot containing a reference to a thread control block (TCB). Intuitively, this invariant implies that *all reachable*, *potentially used references in the kernel—be it in capabilities*, *kernel objects or other data structures —always point to an object of the expected type*.

## Invariants: Data structures & Algorithmic

#### Data structures

These are classical data structure invariants, such that correct back links in doubly-linked lists, a statement that there are no loops in specific pointer structures, that other lists are always terminated correctly with NULL, etc.

## algorithmic

These are the most complex invariants in our proof and they are where most of the proof effort was spent.

These invariants are either required to prove that specific optimisations are allowed (e.g. that a check can be left out because the condition can be shown to be always true), or they are required to show that an operation executes safely and does not violate other invariants, especially not the typing invariant.

# Conclusion

Table 1: Code and proof statistics

	Haskell/C	Isabelle	Invariants	Proof
	LOC	LOC		LOP
abst.		4,900	$\sim 75$	110,000
exec.	5,700	13,000	$\sim 80$	55,000
impl.	8,700	15,000	0	35,000

The overall size of the proof, including framework, libraries, and generated proofs (not shown in the table) is 200,000 lines of Isabelle script.

The total effort for the seL4-specific proof was 11 py.

## Recent Developments and Future Directions

#### **Ecosystem**

- **seL4 Foundation**: Supports open-source community and development.
- **seL4 Summit**: Annual event for sharing advancements.

#### **Innovations**

- **seL4 Microkit**: Framework for static system design.
- Rust Support: Safer user-level code without full verification.
- Commercial Use: NIO's SkyOS for electric vehicles.

#### **Future**

- Enhanced hardware support (e.g., FPGAs, IOMMU).
- Verification of multi-core and application layers.

#### REFERENCES

- [1] G. Klein *et al.*, "SeL4: Formal verification of an OS kernel," 2009, pp. 207–220. doi: 10.1145/1629575.1629596.
- [2] G. Heiser, "The seL4 Microkernel An Introduction," 2020, pp. 8–14. [Online]. Available: https://api.semanticscholar.org/CorpusID:219781028