



DESIGN AND ANALYSIS OF ALGORITHMS

LAB WORKBOOK

WEEK – 4

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CLASS : CSE-B

Question 1: Write a C program that reads N integers from the user and sorts it using Merge sort

CODE:

```
C mergesort.c > main(void)
1   #include <stdio.h>
2   static void ms_merge(int*a,int*tmp,int l,int m,int r)
3   {
4       int i=l;
5       int j=m;
6       int k=l;
7       while(i<m&&j<r)
8       {
9           if(a[i]<=a[j])
10              tmp[k++]=a[i++];
11         else
12             tmp[k++]=a[j++];
13     }
14     while(i<m)
15         tmp[k++]=a[i++];
16     while(j<r)
17         tmp[k++]=a[j++];
18     for(i=l;i<r;i++)
19         a[i]=tmp[i];
20 }
21 static void ms_run(int*a,int*tmp,int n,int sz)
22 {
23     if(sz>=n)
24         return;
25     for(int s=0;s<n;s+=2*sz)
26     {
27         int m=s+sz;
28         int e=s+2*sz;
29         if(m>n)
30             m=n;
31         if(e>n)
32             e=n;
33         if(m<e)
34             ms_merge(a,tmp,s,m,e);
35     }
36     ms_run(a,tmp,n,sz*2);
37 }
```

```

38  ↘ void ms(int*a,int n,int buf[])
39  {
40      ms_run(a,buf,n,1);
41  }
42 ↘ int main(void)
43  {
44      int a[]={157,110,147,122,111,149,151,141,123,112,117,133};
45      int n=sizeof(a)/sizeof(a[0]);
46      int buf[n];
47      ms(a,n,buf);
48      for(int i=0;i<n;i++)
49      {
50          printf("%d ",a[i]);
51      }
52  }

```

OUTPUT:

```

110 111 112 117 122 123 133 141 147 149 151 157
PS C:\Users\123sr\OneDrive\Desktop\COLLEGE STUFF\SEM IV\DAA LAB\Week 4> 

```

Space Complexity: O(N)

Time Complexity: O(N log N)

Justification:

- The array is divided into two equal halves at each step, and the merge operation compares all n elements. Since this division continues for $\log n$ levels, the overall Time Complexity becomes $O(N \log N)$.
- An extra array is used during the merging process to temporarily store elements. This additional storage requires space proportional to the number of elements, resulting in $O(n)$ Space Complexity.

Question 2:

Create a C program that implements Quick Sort to sort an array of integers.

CODE:

```
1 #include <stdio.h>
2 static int part(int*a,int l,int r)
3 {
4     int p=a[r];
5     int i=l-1;
6     for(int j=l;j<r;j++)
7     {
8         if(a[j]<=p)
9         {
10             i++;
11             int t=a[i];
12             a[i]=a[j];
13             a[j]=t;
14         }
15     }
16     int t=a[i+1];
17     a[i+1]=a[r];
18     a[r]=t;
19     return i+1;
20 }
21 static void qs_run(int*a,int l,int r)
22 {
23     if(l<r)
24     {
25         int p=part(a,l,r);
26         qs_run(a,l,p-1);
27         qs_run(a,p+1,r);
28     }
29 }
30 void qs(int*a,int n)
31 {
32     qs_run(a,0,n-1);
33 }
34 int main(void)
35 {
36     int a[]={157,110,147,122,111,149,151,141,123,112,117,133};
37     int n=sizeof(a)/sizeof(a[0]);
```

```
38     qs(a,n);
39     for(int i=0;i<n;i++)
40         printf("%d ",a[i]);
41     printf("\n");
42     return 0;
43 }
```

OUTPUT:

```
110 111 112 117 122 123 133 141 147 149 151 157
PS C:\Users\123sr\OneDrive\Desktop\COLLEGE STUFF\SEM IV\DAA LAB\Week 4> ◻
```

Space Complexity: O(N)

Time Complexity: O(N^2)

Justification:

- In the worst case, Quick Sort makes highly unbalanced recursive calls, reducing the problem size by only one element at each step. As a result, the recursion depth becomes n , and the recursion stack stores up to n function calls, leading to $O(N)$ Space Complexity.
- This occurs when the pivot divides the array into highly unbalanced parts, such as in already sorted or reverse sorted array. Hence the Time Complexity is $O(N^2)$.