Infinity (and beyond)

Help Center

Often times when constructing algorithms we want to set variables to a symbolic value to signify a special state in our algorithm. For example, if we want to compute the distance between two nodes in a graph, what should that value be when no path connects them? 0? -1? None? Infinity? Each has advantages and drawbacks. Consider the case of finding the minimum value in a list of numbers:

```
def find_minimum(list_of_numbers):
smallest_seen = None
for i in list_of_numbers:
    if i < smallest_seen:
        smallest_seen = i</pre>
```

What do you expect the output of find_minimum([2, 3, 2, 1, 5]) to be? Interestingly enough, this invocation yields None. Why? Because in Python None < 1 is true. So what first seems like a logical choice (we have never seen any value yet, so clearly the smallest seen number is nonexistent) can turn out to be problematic in our implementation. Great care and thought must be taken when selecting these symbolic values as their choice may impact your program's correctness.

```
def find_minimum(list_of_numbers):
smallest_seen = None
for i in list_of_numbers:
    if (smallest_seen == None) or (i < smallest_seen):
        smallest_seen = i

return smallest_seen</pre>
```

Using None therefore required an awkward check that must occur every time through the loop, even though smallest_seen will never be None after the first iteration. So, what value then should we initially assign to smallest_seen? Infinity seem like a good choice. Anything inside the list must be smaller than infinity (unless infinity appears in the list. Is that an issue for this algorithm?). We can represent infinity in Python using float('inf'):

```
def find_minimum(list_of_numbers):
smallest_seen = float('inf')
for i in list_of_numbers:
    if i < smallest_seen:
        smallest_seen = i</pre>
```

Now find_minimum([2, 3, 2, 1, 5]) produces 1. What though is the output of find_minimum([]) and find_minimum([float('inf')])? Both are float('inf') so how do we know if the input list was empty or contained only one element? As you can see, no implementation is perfect. The important part though is to know the limitations of your implementation, understand their impact on your algorithm and compensate for those cases (for example, we could check for a zero length list before calling find_minimum).

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