Drawing trees

In the supplied Tree class, we included example code that draws a rooted tree in its standard configuration with the root node at the top. In this practice activity, we review this drawing code and consider how drawing a tree can be expressed as a recursive process.

Computing the bounding box for a tree

Prior to drawing a tree, having an estimate of the canvas space required to draw a tree is very helpful. For this purpose, our first task is compute the height and width of a rectangular box that bounds the diagram of the tree. This box is referred to as the *bounding box* for the tree. We can then use the size of this box to determine the size of the required canvas. Note the size of this box can be computed directly from the height of the tree and the number of its leaves. However, we will compute these values recursively from the structure of the tree to provide more practice with recursion and trees.

In the base case, a tree consists of a single node. The constants NODE_HEIGHT and NODE_WIDTH represent the user-defined height and width of the bounding box for a single node. At this point, you are welcome to implement a recursive function <code>get_box_size(tree)</code> that takes a tree and returns the height and width of the bounding box of this tree using these constants. Our implementation of <code>get_box_size</code> is a method in the <code>TreeDisplay</code> class in <code>poc_draw_tree</code>. Feel free to use our implementation as a template for your efforts. Just hide the body of <code>get_box_size</code> using code folding while you reimplement it.

In the case where the root node has one or more subtrees, our solution computes the height and width of the bounding boxes for each subtree recursively. In this case, the height of the bounding box for the entire tree is NODE_HEIGHT plus the maximum of the heights of the bounding boxes for each subtree. The width of the bounding box for the entire tree is the larger of the width of the bounding box for the root and the sum of the widths of the subtrees.

Drawing a tree

When drawn as a diagram, a tree consists of a collection of nodes and edges. For rooted trees, this diagram can be drawn using a recursive method draw_tree with two parts:

- Draw the root node and the edges from this root node to the roots of its children,
- Call draw_tree to draw the diagrams for each of the root node's subtrees.

One subtle issue with draw_tree is that the line segments from the root node to its children should be drawn before the circles for these nodes. This ordering ensures that the edges aren't drawn on top of the nodes in the tree. This observation leads to the conclusion that these edges must be drawn before any recursive calls to draw_tree happen. However, the draw_line statements for these edges still require the positions of the root nodes's children.

Our solution to this problem is to call <code>get_box_size</code> on each of the subtrees prior to any drawing. With this information, we can compute the centers for all of the children of the root node and use <code>draw_line</code> to draw the required edges. After one call to <code>draw_circle</code> to draw the root node, we can then recursively call <code>draw_tree</code> on each subtree. For the calls to <code>draw_circle</code>, we used a diameter that is half of <code>NODE_HEIGHT</code>.

To finish this activity, you are welcome to attempt an implementation of draw_tree(canvas, tree,

mplementing it.	
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