

Averages around and including each point in a matrix X:

$$A = (M(MX)^T)^T \oslash D$$

Where \oslash is piece-wise division. A, X are n by n matrices.

$$\begin{aligned} \text{M is an n by n matrix} &= \begin{bmatrix} 1 & 1 & 0 & 0 & 0 & 0 & \dots \\ 1 & 1 & 1 & 0 & 0 & 0 & \dots \\ 0 & 1 & 1 & 1 & 0 & 0 & \dots \\ 0 & 0 & 1 & 1 & 1 & 0 & \dots \\ \dots & \dots & \dots & \dots & \dots & \dots & \dots \\ \dots & 0 & 0 & 0 & 0 & 1 & 1 \end{bmatrix} \\ \text{D is an n by n matrix} &= \begin{bmatrix} 4 & 6 & \dots & 6 & 4 \\ 6 & 9 & \dots & 9 & 6 \\ \dots & \dots & \dots & \dots & \dots \\ 6 & 9 & \dots & 9 & 6 \\ 4 & 6 & \dots & 6 & 4 \end{bmatrix} \end{aligned}$$

Without the piece-wise division by D you have the sums around (and including) each point.

If you only want the sums around the point (not including):

$$A = (M(MX)^T)^T - X$$

For the averages you can do piece-wise division by D with every element by one:

$$A = ((M(MX)^T)^T - X) \oslash (D - O)$$

Where O is the n by n matrix consisting only of 1's.

Example:

$$X = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \\ 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \end{bmatrix}$$

$$M = \begin{bmatrix} 1 & 1 & 0 & 0 \\ 1 & 1 & 1 & 0 \\ 0 & 1 & 1 & 1 \\ 0 & 0 & 1 & 1 \end{bmatrix}$$

$$D = \begin{bmatrix} 4 & 6 & 6 & 4 \\ 6 & 9 & 9 & 6 \\ 6 & 9 & 9 & 6 \\ 4 & 6 & 6 & 4 \end{bmatrix}$$

$$S = (M(MX)^T)^T = \begin{bmatrix} 2 & 3 & 3 & 2 \\ 3 & 5 & 4 & 3 \\ 3 & 4 & 5 & 3 \\ 2 & 3 & 3 & 2 \end{bmatrix}$$

$$A = S \otimes D = \begin{bmatrix} \frac{1}{2} & \frac{1}{2} & \frac{1}{2} & \frac{1}{2} \\ \frac{1}{2} & \frac{1}{2} & \frac{1}{2} & \frac{1}{2} \\ \frac{1}{2} & \frac{1}{2} & \frac{1}{2} & \frac{1}{2} \\ \frac{1}{2} & \frac{1}{2} & \frac{1}{2} & \frac{1}{2} \end{bmatrix}$$