# criteo\_017\_v5\_adf\_tit-nye

### 2016년 5월 29일

# 제1절 빅데이터 분석을 위한 실시간 로지스틱 회귀모형에 관현 연구

1.1 : 베이지안 접근법을 중심으로

- 1.2 1. 배경
- 1.3 2. 해싱을 이용한 가변수 코딩(Feature Hashing)
- 1.4 3. 온라인 최적화 알고리즘
- 1.4.1 3.1. 확률적 경사 하강법(Stochastic Gradient Descent)

최적화(optimization) 알고리즘의 하나인 경사하강법(Gradient descent)에서는 전체 샘플 데이터를 스캔 할 때마다 회귀 계수 추정치를 갱신해 나간다. 비용함수(cost function)를  $J(w)=\frac{1}{2}\sum_i(target^{(i)}-output^{(i)})^2$ 라 할때 길이가 j인 계수 벡터(weight vector)  $w_i$ 를  $w_{i+1}=w_i+\Delta w$ 로 갱신하는 매 반복에서 j개의 모수 추정치(w)를 얼마만큼 줄일지혹은 늘릴지  $\Delta w$  값을 결정해야 한다. 여기에서  $\Delta w$ 는 아래와 같다.

$$\Delta w_j = -\alpha \frac{\delta J}{\delta w_j} \tag{1}$$

$$= -\alpha \sum_{i}^{J} (target^{(i)} - output^{(i)})(-x^{(i)j})$$
 (2)

$$= \alpha \sum_{i} (target^{(i)} - output^{(i)})(x^{(i)j})$$
 (3)

즉 비용함수(cost function)의 경사도가 크면 그만큼 많이 w값을 수정하게 되는데, 학습 계수(learning rate, step size)  $\alpha$ 에 비례하여 수정치가 결정된다.

경사하강법에서는 한번 w값을 수정하기 위하여 전체 샘플 데이터를 스캔하게 된다. 그런데 이런 방식은 샘플의 수가 많은 경우 비용함수 J(w)를 최소로 하는 w값을 찾기 까지

그 처리 시간이 길어 지게 된다. 모수에 대한 학습(learning)이나 추론(inference)를 진행할 때 데이터의 크기가 작거나 데이터의 수집으로부터 예측까지 시간적 여유가 있을 경우 데이터 전체를 한꺼번에 활용하는 일괄 처리(batch processing) 방식을 사용한다. 반면 데이터를 한꺼번에 처리하기에 그 크기가 지나치게 크거나 스트리밍(streaming)으로 유입되는 데이터에 대해서 실시간으로 예측을 처리해야 하는 경우 온라인 학습 (online learning)을 사용해야 할 필요성이 있다.

이처럼 때 갱신에서 전체 샘플 데이터를 사용하는 대신 샘플 하나 혹은 일부분만을 사용하여 w 값을 갱신해 가는 경사하강법을 확률적 경사 하강법(Stochastic Gradient Descent, Online Gradient Descent)이라 하며, 확률적 이라는 단어에서 알 수 있듯이 J(w)를 최소로 하는 w값을 확률적 근사방법으로 찾아가는 것이다. 하나의 샘플만을 이용해 w의 갱신 방향과 크기를 결정하기 때문에 경사하강법과는 달리 J(w)값이 커지는 경우도 있으나 샘플 수가 충분할 경우 J(w)의 전역 최소값으로 수렴하는 w를 찾을 수 있는 것으로 알려져 있다.

- 본 연구에서는 전체 파라미터 벡터에 동일한 step size 초기값을 설정하고, iteration 이 증가하면서 각 hashed-feature가 등장하는 횟수로 step size를 나눈다.
- 즉 특정 hashed-feature가 많이 등장할 수록 해당 회귀 모수에 대한 step-size가 감소하게 되고, 자주 등장하지 않는 hashed-feature의 경우 비교적 큰 step-size를 갖게 된다.

# [알고리즘]

```
y = 1. if row[c_fi.ylab] == '1' else 0.
          del row[c_fi.ylab]
          x = get_x_mmh3(row, D)
          p = get_p(x, w)
          w, n = update_w_withn(w, n, x, p, y, alpha)
       f.close()
       NameError
                                            Traceback (most recent call last)
       <ipython-input-2-911b9639ded6> in <module>()
        1 # simplified version of SGD
   ----> 2 c_fi = fi_titanic
        3
        4 D = 2 ** 20
        NameError: name 'fi_titanic' is not defined
In [3]: def update_w_withn(w, n, x, p, y, alpha):
          for i in x:
              w[i] = (p - y) * alpha / (sqrt(n[i]) + 1.)
              n[i] += 1.
          return w, n
```

# 1.4.2 3.2. 추정된 밀도 필터링(Assumed Density Filtering)

추정된 밀도 필터링(Assumed-density filtering, ADF) 이란?

추정된 밀도 필터링(Assumed-density filtering, ADF)는 베이지안 네트워크 혹은 여타의 통계 모형에서 사후분포를 근사적으로 계산하는 방법으로서 통계학에는 Lauritzen, 1992이 제안. 분야에 따라 달리 불림

- 추정된 밀도 필터링(Assumed-density filtering)
- 온라인 베이지안 학습(On-line Bayesian learning)
- 적률 대응(Moment matching)
- 약한 주변화(Weak marginalization)

ADF에서는 사후분포를 가우시안과 같은 특정 분포로 근사하는 방법으로서 예측-갱신-투영(predict-update-project)과정을 반복한다.

- 예측(predict): 모수  $\theta$ 에 대한 t-1 시점의 사전분포,  $q_{t-1}(\theta_{t-1})$ 와 t시점의 관측치를 이용하여 이후 시점 t에서의  $\theta$ 에 대한 사후예측분포,  $q_{t|t-1}(\theta_t)$ 를 구함
- 갱신(update): 앞서 구한 사전분포와 사후예측분포를 이용하여  $\theta$ 에 대한 사후분포,  $\hat{p}(\theta_t)$ 를 구함
- 투영(project): 마지막으로 이 사후 분포가 다루기 쉬운 형태가 아닌 경우가 빈번하기 때문에 다루기 쉬운 분포로 투영(project)\_
- 근사 사전분포:

$$q_{t-1}(\theta_{t-1}) \approx p(\theta_{t-1}|y_{1:t-1})$$

• 1단계 사후예측분포:

$$q_{t|t-1}(\theta_t) = \int p(\theta_t|\theta_{t-1})q_{t-1}(\theta_{t-1})d\theta_{t-1}$$

• 사후분포:

$$\hat{p}(\theta_t) = \frac{1}{Z_t} p(y_t | \theta_t) q_{t|t-1}(\theta_t)$$

• 정규화 상수(normalizing constant):

$$Z_t = \int p(y_t|\theta_{t-1})q_{t|t-1}(\theta_t)d\theta_t$$

• 근사 사후분포:

$$q(\theta_t) = \arg\min_{q \in Q} \mathrm{KL}(\hat{p}(\theta_t || q(\theta_t)))$$

지수족에서의 추정된 밀도 필터링(Assumed-density filtering, ADF)

투영하려는 분포 q가 지수족에 속할 경우 단순히 적률 대응(moment matching)만으로  $q(\theta_t)$ 를 구할수 있다. 따라서 일반화 선형모형에 적률 대응을 적용.

편의를 위해 설명변수와 회귀계수의 선형식(systematic component)을  $s_t = \theta_t^T x_t$ 라 하고, 만약  $\theta_t$ 에 대한 1단계 사후예측분포,  $q_{t|t-1}(\theta_t)$ 가 $\prod_i N(\theta_{t,i}; \mu_{t|t-1,i}, \sigma^2_{t|t-1,i})$ 라면  $s_t$ 의 사후 예측분포,  $q_{t|t-1}(s_t)$ 는 아래와 같다.

$$q_{t|t-1}(s_t) \equiv N(s_t; m_{t|t-1}, v_{t|t-1})$$
 (4)

$$m_{t|t-1} = \sum_{i=1}^{N} x_{t,i} \mu_{t|t-1,i}$$
 (5)

$$v_{t|t-1} = \sum_{i=1}^{N} x_{t,i}^2 \sigma_{t|t-1,i}^2$$
 (6)

이때  $s_t$ 의 사후분포,  $q_t(s_t)$ 는 아래와 같다.

$$q_t(s_t) \equiv N(s_t; m_t, v_t) \tag{7}$$

$$m_t = \int s_t \frac{1}{z_t} f(y_t|s_t) q_{t|t-1}(s_t) ds_t$$
 (8)

$$v_t = \int s_t^2 \frac{1}{z_t} f(y_t|s_t) q_{t|t-1}(s_t) ds_t - m_t^2$$
 (9)

$$z_t = \int f(y_t|s_t)q_{t|t-1}(s_t)ds_t \tag{10}$$

$$f(y_t|s_t) \equiv Ber(y_t; \pi = sigmoid(s_t))$$
 (11)

$$= \pi^{y_t} (1 - \pi)^{(1 - y_t)}, \quad y_t \in \{0, 1\}$$
 (12)

가우시안 구적법(Gaussian quadrature)을 이용해 위 적분식 근사

$$\int_{a}^{b} W(x)f(x)dx \approx \sum_{j=1}^{N} w_{j}f(x_{j})$$

$$\chi = \chi' \sqrt{2} \sigma_{s_t} + \mu_{s_t}$$
$$\omega_i = \frac{\omega'}{\sqrt{\pi}}$$

$$q_t(s_t) = N(s_t; \tilde{m}_t, \tilde{v}_t) \tag{13}$$

$$\tilde{m}_t = \frac{1}{\tilde{z}_t} \sum_i \chi_i f(y_t; \chi_i) \omega_i \tag{14}$$

$$\tilde{v}_t = \frac{1}{\tilde{z}_t} \sum_i \chi_i^2 f(y_t; \chi_i) \omega_i - \tilde{m}_t^2$$
(15)

$$\tilde{z}_t = \sum_i f(y_t; \chi_i) \omega_i \tag{16}$$

알고리즘

```
In [4]: init_v = 0.520073999999999 # best for titanic
        theta_t_m = np.array([0.] \star (D)) # mean of thetas at t
        theta_t_v = np.array([init_v] * (D)) # variance of thetas at t
        n = np.array([0.] * D)
        f = open(c_fi.file_path)
        for t, row in enumerate (DictReader (f, fieldnames=c_fi.l_header_names, delir
            if t == 0:
                continue
            del row['PassengerId']
            y = 1. if row[c_fi.ylab] == '1' else 0.
            del row[c_fi.ylab]
            x = get_x_mmh3(row, D)
            \# Predictive distribution for s_t \sim N(s_t_mold, s_t_vold)
            s_t_m_old = sum(theta_t_m[x])
            s_t_v_old = sum(theta_t_v[x])
            # Posterior distribution for s_t
            s_t_m, s_t_v = get_s_t_new(y, s_t_m_old, s_t_v_old)
            # Changes in s_t
            delta_m = s_t_m - s_t_m_old
            delta_v = s_t_v - s_t_v_old
            # Updating theta
            update_theta_cat(x, theta_t_m, theta_t_v, delta_m, delta_v, t, n)
            \#p = get\_p\_cat(x, theta\_t\_m)
        f.close()
```

\_\_\_\_\_

```
NameError
                                                Traceback (most recent call last)
       <ipython-input-4-f1169350cd7b> in <module>()
         ----> 3 theta_t_m = np.array([0.] \star (D)) # mean of thetas at t
         4 theta_t_v = np.array([init_v] \star (D)) # variance of thetas at t
         5 n = np.array([0.] * D)
       NameError: name 'np' is not defined
In [5]: # s_t_m_old and s_t_v_old must be numpy ndarray
       def get_s_t_new(y, s_t_m_old, s_t_v_old):
           wi = wwi / np.sqrt(np.pi)
           xi = xxi * np.sqrt(2) * np.sqrt(s_t_v_old) + s_t_m_old
           fw = 0.
           if (y==1):
               fw = (1. / (1. + np.exp(-xi))) * wi
           else:
               fw = ((np.exp(-xi)) / (1. + np.exp(-xi))) * wi
           z t = sum(fw)
           s_t_m_new = 1. / z_t * sum(xi * fw)
           s_t_v_new = 1. / z_t * sum((xi**2) * fw) - s_t_m_new**2
           return (s_t_m_new, s_t_v_new)
In [6]: def update_theta_cat(x, theta_t_m, theta_t_v, delta_m, delta_v, n_iter, n):
           a_i = get_a_i_cat(x, theta_t_v)
```

theta\_t\_m[x] += (a\_i \* delta\_m)

theta\_t\_v[x] += 
$$((a_i**2) * delta_v)$$
  
n[x] += 1.

In [7]: # theta\_t\_v must be numpy ndarray

return theta\_t\_v[x] / sum(theta\_t\_v[x])

# 1.5 4. 실험

# 1.5.1 4.1. 실험(타이타닉 데이터)

개요

- 소규모 데이터를 이용한 실험을 위해 891건의 타이타닉 생존자 데이터를 이용
- 데이터는 생존여부(0,1)를 나타내는 'Survived'와 탑승자의 특성을 나타내는 8가지 변수로 구성됨.
- 초기 800건을 훈련 데이터, 나머지 91건을 테스트 데이터로 사용

#### 최적 초기값

SGD는 step size의 초기값 $(\alpha_{init})$ 에, ADF는 회귀 계수 분포의 초기 분산값 $(V_{init})$ 에 큰 영향을 받음.

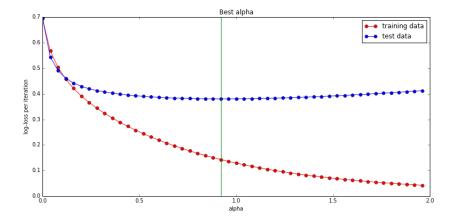
주어진 데이터에 최적인  $\alpha_{init}$ 과  $V_{init}$ 를 찾기 위해 각 값을 변화시키면서, 훈련 데이터와 데스트 데이터에 대한  $\log$ -loss를 관찰함

$$logloss = -\frac{1}{N} \sum_{i=1}^{N} (y_i \log(p_i) + (1 - y_i) \log(1 - p_i))$$

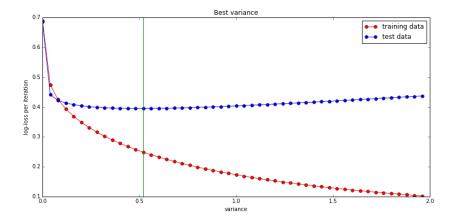
#### **Stochastic Gadient Descent**

# **Assumed Density Filtering**

$$\frac{ \text{Index} \ \ \alpha}{\text{AUC} \ \ \, 13 \ \ \, 0.5200739999999999993}$$



Local image

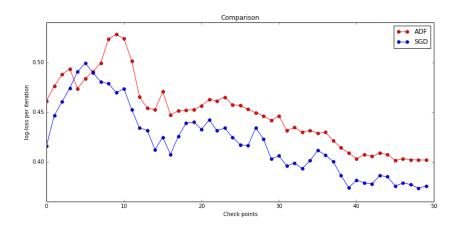


Local image

테스트 데이터에 최소 log-loss를 갖는 분산값은 0.5200739999999993

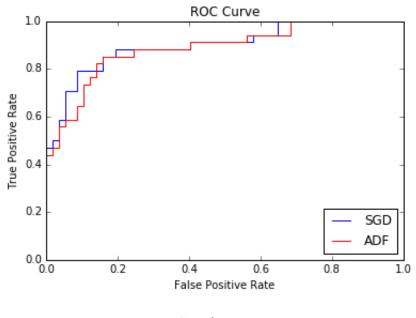
훈련 데이터 크기에 따른 log-loss 비교

16건의 훈련 데이터를 더 사용할 때마다 그때의 회귀 계수 벡터를 이용하여 91건의 테스트 데이터에 대한 log-loss 추이를 두 방법론(SGD, ADF)에 대해 비교한다.



Local image

전반적으로 ADF에 비해 SGD의 log-loss가 낮음.



Local image

SGD ADF

AUC 0.90041279669762642 0.88802889576883381

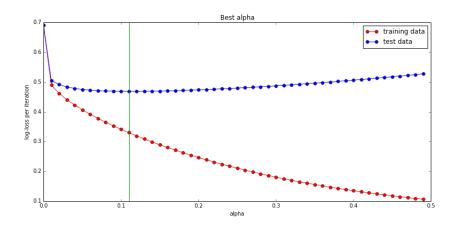
# 1.5.2 4.2. 실험(온라인 광고 데이터)

개요

Criteo에서 'Kaggle 대회'를 위해 공개한 4천 5백만건 상당의 온라인 광고 데이터를 사용하였다. 데이터는 웹사이트 방문자가 해당 광고를 클릭 했으냐 혹은 하지 않았느냐를 나타내는 이항 반응변수 Label과 39개의 설명변수로 구성되어 있다. 그리고 각 설명변수는 범주형으로서 범주는 500개 이상으로 실제 데이터의 경우 훈련 데이터에 없던 범주가 새롭게 등장 할 수도 있는 특성을 갖는다. 이러한 데이터를 일괄처리(batch) 방식으로 처리한다면 대략 19,500 × 45,000,000 크기의 매트릭스 연산을 수행해야 한다.

# 최적 초기값

#### **Stochastic Gadient Descent**



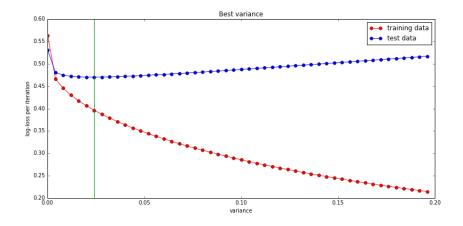
Local image

# **Assumed Density Filtering**

훈련 데이터 크기에 따른 log-loss 비교

SGD ADF

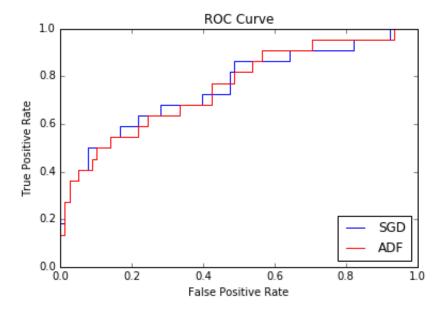
AUC 0.75874125874125875 0.75699300699300698



Local image



Local image



Local image

```
1.6 5. 맺음말
In [ ]:
In [ ]:
제 2 절 [부록-구현]
2.0.1 Simulation SGD for titanic data
In [8]: from datetime import datetime
        from csv import DictReader
        from math import exp, log, sqrt
        import numpy as np
        import mmh3
        import time
        from spooky import hash128, hash64, hash32
        from sklearn.metrics import roc_curve, auc
        import scipy.stats as stats
        import matplotlib.pyplot as plt
        import matplotlib as mpl
        %matplotlib inline
  Parameters
In [9]: D = 2 ** 20
        rand\_seed = 1004
        num_poly = 10
        xxi, wwi = np.polynomial.hermite.hermgauss(num_poly)
In [10]: class DataSize:
             def __init__(self
                          , num_metric_check_point
                           , num_status_check_point
                           , num_train_data_start
                           , num_train_data_size
```

```
, num_test_data_size):
                                             self.num metric check point = num metric check point
                                             self.num_status_check_point = num_status_check_point
                                             self.num_train_data_start = num_train_data_start
                                             self.num_train_data_end = self.num_train_data_start + num_train_data_start + num_train_data_start
                                             self.num_test_data_start = num_test_data_start
                                              self.num_test_data_end = self.num_test_data_start + num_test_data_
                                   def display(self):
                                             print("num_metric_check_point: %s" %(self.num_metric_check_point))
                                             print("num_status_check_point: %s" %(self.num_status_check_point))
                                             print("num_train_data_start : %s" %(self.num_train_data_start))
                                             print("num_train_data_end : %s" %(self.num_train_data_end))
                                             print("num_train_data_size : %s" %(self.num_train_data_end - self.num_train_data_end - self
                                             print ("num_test_data_start
                                                                                                                         : %s" %(self.num_test_data_start))
                                             print("num_test_data_end : %s" %(self.num_test_data_end))
                                             print("num test data size
                                                                                                                         : %s" %(self.num_test_data_end - self
In [11]: class FileInfo:
                                   def __init__(self
                                                                   , _file_path
                                                                   , _f_having_header
                                                                   , _l_header_names
                                                                   , _seperator
                                                                   , _l_skip_columns
                                                                   , _ylab):
                                             self.file_path = _file_path
                                             self.f_having_header = _f_having_header
                                             self.l_header_names = _l_header_names
                                             self.seperator = _seperator
                                             self.l_skip_columns = _l_skip_columns
                                             self.ylab = \_ylab
```

, num\_test\_data\_start

```
r'C:/My/Playground/Git/2016_Thesis/100_Simulation/data/tra
                         , True # _f_having_header
                         , ['PassengerId', 'Survived', 'Pclass', 'Name', 'Sex'
                            , 'Age', 'SibSp', 'Parch', 'Ticket', 'Fare', 'Cabin',
                         , ',' # _seperator
                         , ['PassengerId']# _l_skip_columns
                         , 'Survived'# _ylab
         fi_criteo = FileInfo(
                         r'C:\Temp\dac.tar\train.txt' # _file_path
                         , False # _f_having_header
                         , ['Label'] + [ 'I' + str(i) for i in list(range(1,14))] -
                         , '\t' # _seperator
                         , [] # _1_skip_columns
                         , 'Label'# _ylab
  Functions
In [13]: # csv_row must be dict
         def get_x_mmh3(csv_row, D):
             x = [0]
             for key, value in csv_row.items():
                 index = mmh3.hash128(str(key) + str(value), seed=rand_seed, x64ard
                 x.append(index)
             return x
In [14]: # csv_row must be dict
         def get_x_spooky(csv_row, D):
             x = [0]
             for key, value in csv_row.items():
                 index = hash32(str(key) + str(value)) % D
                 x.append(index)
             return x
```

In [12]: fi\_titanic = FileInfo(

```
In [15]: def get_p(x, w):
             v = v = 0.
             for i in x: # do wTx
                 wTx += w[i] * 1. # w[i] * x[i], but if i in x we got x[i] = 1.
             return 1. / (1. + exp(-max(min(wTx, 20.), -20.))) # bounded sigmoid
In [16]: # w must be numpy ndarray
         def get_p_cat(x, w):
             wTx = sum(w[x])
             return 1. / (1. + exp(-max(min(wTx, 20.), -20.))) # bounded sigmoid
In [17]: def logloss(p, y):
             p = max(min(p, 1. - 10e-12), 10e-12)
             return -\log(p) if y == 1. else -\log(1. - p)
In [18]: def get_validation_metrics(c_fi,start, end, wlen, w, f_debug):
             log_loss = 0.
             arr_y = []
             arr_p = []
             f = open(c fi.file path)
             for t, row in enumerate(DictReader(f, fieldnames=c_fi.l_header_names,
                 if t == 0:
                     continue # just for titanic
                 if t < start: # fixed</pre>
                     continue;
                 y = 1. if row[c_fi.ylab] == '1' else 0.
                 del row[c_fi.ylab]
                 arr_y.append(y)
                 if(len(c_fi.l_skip_columns) > 0):
                     for i in range(len(c_fi.l_skip_columns)):
                         del row[(c_fi.l_skip_columns)[i]] # for titanic
```

```
p = 0
                                                                   if(isinstance(w, list)):
                                                                                  p = get_p(x, w)
                                                                   else:
                                                                                  p = get_p_cat(x, w)
                                                                   arr_p.append(p)
                                                                   log_loss += logloss(p, y)
                                                                   if f_debug:
                                                                                   if t >= 1: # fixed
                                                                                                  print(' [get_validation_metrics] %s\tencountered: %d\t y=9
                                                                                                                   datetime.now(), (t), y, p, log_loss/t))
                                                                   # End of ...
                                                                   if t >= end: # fixed
                                                                                  break;
                                                    f.close()
                                                    return(log_loss, arr_y, arr_p)
                                    #fn = ['Label'] + [ 'I' + str(i) for i in list(range(1,14))] + [ 'C' + str
                                    #get_validation_metrics(train, fn, '\t', 'Label', num_test_data_start, n
In [19]: def plot_log_loss(arr_log_loss):
                                                  plt.figure(num=None, figsize=(13, 6), dpi=80, facecolor='w', edgecolor
                                                   x = range(len(arr_log_loss))
                                                   plt.plot(x, arr_log_loss, label='log_loss', marker='o')
제 3 절 SGD
```

 $x = get_x_mmh3(row, wlen)$ 

# Functions

```
In [20]: def update_w_withn(w, n, x, p, y, alpha):
             for i in x:
                 w[i] = (p - y) * alpha / (sqrt(n[i]) + 1.)
                 n[i] += 1.
             return w, n
In [21]: def update_w(w, n, x, p, y, alpha):
             for i in x:
                 w[i] -= (p - y) * alpha
                 n[i] += 1.
             return w, n
  Training function
In [22]: def sgd_training(alpha, D, f_debug, f_step_validation, f_validation, c_ds,
             w = [0.] * D # weights
             n = np.array([0.] * (D))
             start_time = time.time()
             log_loss_sgd_training = 0.
             arr_log_loss_sqd_test = []
             f = open(c_fi.file_path)
             fn = c_fi.l_header_names
             for t, row in enumerate (DictReader (f, fieldnames=fn, delimiter=c_fi.se
                 if len(c_fi.l_skip_columns) > 0 :
                     for i in range(len(c_fi.l_skip_columns)):
                          del row[(c_fi.l_skip_columns)[i]] # for titanic
                 if t == 0 & c_fi.f_having_header:
                     continue
                 if t < c_ds.num_train_data_start:</pre>
                     continue
```

```
# Start of ...
   y = 1. if row[c_fi.ylab] == '1' else 0.
   del row[c_fi.ylab]
   x = get_x_mmh3(row, D)
   p = get_p(x, w)
   w, n = update_w_withn(w, n, x, p, y, alpha)
   p = get_p(x, w)
    log_loss_sgd_training += logloss(p, y)
    if f_debug:
        if t % c_ds.num_status_check_point == 0 and t >= 1: # for tit
            print('%s\tencountered: %d\t y=%d: %f, loss:%f' % (
                datetime.now(), (t), y, p, log_loss_sgd_training/t))
    if f_step_validation:
        if t % c_ds.num_metric_check_point == 0 and t > 1:
            rt_log_loss, arr_y, arr_p = get_validation_metrics(
                    c_fi
                    , c_ds.num_test_data_start
                    , c_ds.num_test_data_end
                    , W
                    , f_debug)
            arr_log_loss_sgd_test.append(rt_log_loss / (c_ds.num_test_
    if t >= c_ds.num_train_data_end:
        break
f.close()
if f_debug:
   print("---Total execution time: %s seconds ---" % (time.time() - s
# Return different variables as mode selected.
```

# 제4절 ADF

#### **Functions**

```
In [23]: # s_t_m_old and s_t_v_old must be numpy ndarray
    def get_s_t_new(y, s_t_m_old, s_t_v_old):

        wi = wwi / np.sqrt(np.pi)
        xi = xxi * np.sqrt(2) * np.sqrt(s_t_v_old) + s_t_m_old

        fw = 0.
        if(y==1):
            fw = (1. / (1. + np.exp(-xi))) * wi
        else:
            fw = ((np.exp(-xi)) / (1. + np.exp(-xi))) * wi

        z_t = sum(fw)
        s_t_m_new = 1. / z_t * sum(xi * fw)
```

```
return (s_t_m_new, s_t_v_new)
In [24]: # theta_t_v must be numpy ndarray
         def get_a_i_cat(x, theta_t_v):
             return theta_t_v[x] / sum(theta_t_v[x])
In [25]: def update_theta_cat(x, theta_t_m, theta_t_v, delta_m, delta_v, n_iter, n)
             a_i = get_a_i_cat(x, theta_t_v)
             theta_t_m[x] += (a_i \star delta_m)
             theta_t_v[x] += ((a_i**2) * delta_v)
             \#theta_t_v[x] += ((a_i**2) * delta_v) + abs(theta_t_m[x])/min((n_iter-
             \#theta_t_v[x] += ((a_i**2) * delta_v) + abs(theta_t_m[x])/(n_iter+1.)
             \#theta_t_v[x] += ((a_i**2) * delta_v / np.sqrt(n[x] + 1.))
             \#theta_t_v[x] += ((a_i**2) * delta_v) + 1. / np.sqrt(n[x] + 1.)
             \#theta_t_v[x] += ((a_i**2) * delta_v) + abs(theta_t_m[x])/np.sqrt(n[x])
             n[x] += 1.
  Trainning function
In [26]: def adf_training(variance, D, f_debug, f_step_validation, f_validation, c_
             theta_t_m = np.array([0.] * (D)) # mean of thetas at t
             theta_t_v = np.array([variance] * (D)) # variance of thetas at t
             n = np.array([0.] * D)
             start time = time.time()
             log_loss_adf_training = 0.
             arr_log_loss_adf_test = []
             f = open(c_fi.file_path)
             fn = c_fi.l_header_names
             for t, row in enumerate (DictReader (f, fieldnames=fn, delimiter=c_fi.se
                 if len(c_fi.l_skip_columns) > 0 :
                     for i in range(len(c_fi.l_skip_columns)):
```

 $s_t_v_new = 1. / z_t * sum((xi**2) * fw) - s_t_m_new**2$ 

```
del row[(c_fi.l_skip_columns)[i]] # for titanic
if t == 0 & c_fi.f_having_header:
    continue
if t < c_ds.num_train_data_start:</pre>
    continue
# Start of ...
y = 1. if row[c_fi.ylab] == '1' else 0.
del row[c_fi.ylab]
x = qet_x_mmh3 (row, D)
\# Predictive distribution for s_t ~ N(s_t_m_old, s_t_v_old)
s_t_m_old = sum(theta_t_m[x])
s_t_v_old = sum(theta_t_v[x])
# Posterior distribution for s_t
s_t_m, s_t_v = get_s_t_new(v, s_t_m_old, s_t_v_old)
# Changes in s_t
delta_m = s_t_m - s_t_m_old
delta_v = s_t_v - s_t_v_old
# Updating theta
update_theta_cat(x, theta_t_m, theta_t_v, delta_m, delta_v, t, n)
p = get_p_cat(x, theta_t_m)
log_loss_adf_training += logloss(p, y)
if f_debug:
    if y == 1.:
        print('%s\tencountered: %d\t y=%d: %f, loss:%f' % (
```

```
if t % c_ds.num_status_check_point == 0 and t > 1:
            print('%s\tencountered: %d\t y=%d: %f, loss:%f' % (
                datetime.now(), (t), y, p, log_loss_adf_training/t))
    if f_step_validation:
        if t % c_ds.num_metric_check_point == 0 and t > 1:
            rt_log_loss, arr_y, arr_p = get_validation_metrics(
                    c_fi
                    , c_ds.num_test_data_start
                    , c_ds.num_test_data_end
                    , D
                    , theta_t_m
                    , f_debug)
            arr_log_loss_adf_test.append(rt_log_loss / (c_ds.num_test_
    # End of ...
    if t >= c_ds.num_train_data_end:
        break
f.close()
if f_debug:
    print("---Total execution time: %s seconds ---" % (time.time() - s
if f_step_validation:
    return(arr_log_loss_adf_test)
if f validation:
    rt_log_loss_adf_training = log_loss_adf_training / (c_ds.num_train
    rt_log_loss_adf_test, arr_y, arr_p = get_validation_metrics(
                    c fi
                    , c_ds.num_test_data_start
                    , c_ds.num_test_data_end
                    , D
```

datetime.now(), (t), y, p, log\_loss\_adf\_training/t))

```
, theta_t_m
                               , f_debug)
                rt_log_loss_adf_test = rt_log_loss_adf_test / (c_ds.num_test_data_
                return((theta_t_m, arr_y, arr_p, rt_log_loss_adf_training, rt_log_
  Choose Data-set to simulate
In [27]: TEST_DATA = 'C'
제 5 절 Validation
제 6 절 Let's find best parameters.(validation)
In [28]: ds_best_param_titanic = DataSize(10 # num_metric_check_point
                                , 1 # num_status_check_point
                                , 1, 700
                                              #train_start, train_size
                                , 701, 191) #test_start, test_size
        ds_best_param_criteo = DataSize(10 # num_metric_check_point
                                , 1  # num_status_check_point
                                , 1, 3000
                                               #train_start, train_size
                                , 3001, 1000) #test_start, test_size
        ds_best_param_criteo = DataSize(10 # num_metric_check_point
                                , 1 # num_status_check_point
                                , 1, 10000 #train_start, train_size
                                , 10001, 5000) #test_start, test_size
  SGD: alpha
In [29]: start_time = time.time()
```

arr\_alpha = list(np.linspace(.00001, 2., 50, endpoint=False))

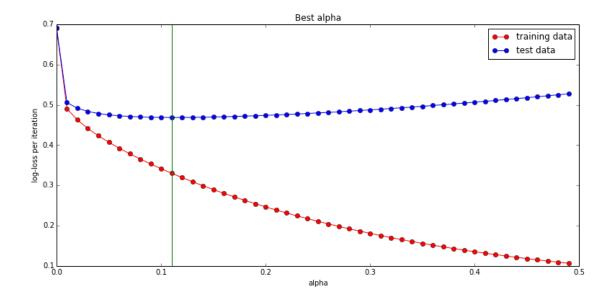
arr\_log\_loss\_sqd\_train\_best\_alpha = [0] \*len(arr\_alpha)

if(TEST DATA == 'T'):

```
arr_log_loss_sgd_test_best_alpha = [0]*len(arr_alpha)
    for i in range(0,len(arr_alpha)):
        param, arr_y, arr_p, arr_log_loss_sgd_train_best_alpha[i], arr_log
                 arr_alpha[i]
                 D = 2 * * 20
                 , f_debug = False
                 , f_step_validation = False
                 , f_validation = True
                 , c_ds = ds_best_param_titanic
                 , c_fi = fi_titanic)
        print('%s, i:%s, param:%s, log-loss(tr:%s, te:%s)' %(datetime.now
                                                           , arr_log_loss_sc
                                                           , arr_log_loss_sc
elif(TEST DATA == 'C'):
    arr_alpha = list(np.linspace(.00001, .5, 50, endpoint=False))
    arr_log_loss_sqd_train_best_alpha = [0] *len(arr_alpha)
    arr_log_loss_sgd_test_best_alpha = [0] *len(arr_alpha)
    for i in range(0,len(arr_alpha)):
        param, arr_y, arr_p, arr_log_loss_sgd_train_best_alpha[i], arr_log
                 arr_alpha[i]
                 D = 2 * * 20
                 , f_debug = False
                 , f_step_validation = False
                 , f_validation = True
                 , c_ds = ds_best_param_criteo
                 , c_fi = fi_criteo)
        print('%s, i:%s, param:%s, log-loss(tr:%s, te:%s)' %(datetime.now
                                                           , arr_log_loss_so
                                                           , arr_log_loss_sc
print("---Total execution time: %s seconds ---" % (time.time() - start_tir
```

```
2016-05-15 19:18:15.851399, i:0, param:1e-05, log-loss(tr:0.6918403588996792, te:0
2016-05-15 19:18:18.494041, i:1, param:0.0100098, log-loss(tr:0.49044689711343914,
2016-05-15 19:18:21.112887, i:2, param:0.0200096, log-loss(tr:0.4625502985876282, t
2016-05-15 19:18:23.712671, i:3, param:0.0300094, log-loss(tr:0.44138048512224426,
2016-05-15 19:18:26.382024, i:4, param:0.0400092, log-loss(tr:0.4233142604535997, t
2016-05-15 19:18:29.044417, i:5, param:0.050009, log-loss(tr:0.40717346369673746, t
2016-05-15 19:18:31.566666, i:6, param:0.0600088, log-loss(tr:0.3923736244975191, t
2016-05-15 19:18:34.133071, i:7, param:0.0700086, log-loss(tr:0.3785815800374904, t
2016-05-15 19:18:36.640006, i:8, param:0.0800084, log-loss(tr:0.36559179485708765,
2016-05-15 19:18:39.157443, i:9, param:0.0900082, log-loss(tr:0.3532698982022108, t
2016-05-15 19:18:41.673066, i:10, param:0.100008, log-loss(tr:0.3415237640053782, t
2016-05-15 19:18:44.171208, i:11, param:0.1100078, log-loss(tr:0.330287578703691, t
2016-05-15 19:18:46.674601, i:12, param:0.1200076, log-loss(tr:0.3195125758479837,
2016-05-15 19:18:49.184297, i:13, param:0.1300074, log-loss(tr:0.3091614062033541,
2016-05-15 19:18:51.701074, i:14, param:0.1400072, log-loss(tr:0.2992045875913354,
2016-05-15 19:18:54.194337, i:15, param:0.150007, log-loss(tr:0.2896181932169808, t
2016-05-15 19:18:56.748217, i:16, param:0.1600068, log-loss(tr:0.28038230352815396,
2016-05-15 19:18:59.237173, i:17, param:0.1700066, log-loss(tr:0.2714799433760288,
2016-05-15 19:19:01.713008, i:18, param:0.1800064, log-loss(tr:0.2628963361706617,
2016-05-15 19:19:04.186371, i:19, param:0.1900062, log-loss(tr:0.2546183703151998,
2016-05-15 19:19:06.672514, i:20, param:0.200006, log-loss(tr:0.24663421112116876,
2016-05-15 19:19:09.145519, i:21, param:0.2100058, log-loss(tr:0.23893301462408548,
2016-05-15 19:19:11.612134, i:22, param:0.2200056, log-loss(tr:0.23150471426198582,
2016-05-15 19:19:14.094299, i:23, param:0.2300054, log-loss(tr:0.22433986067117703,
2016-05-15 19:19:16.612013, i:24, param:0.2400052, log-loss(tr:0.21742950089289978,
2016-05-15 19:19:19:17585, i:25, param:0.250005, log-loss(tr:0.21076508727172683,
2016-05-15 19:19:21.650227, i:26, param:0.2600048, log-loss(tr:0.20433840899850772,
2016-05-15 19:19:24.138814, i:27, param:0.2700046, log-loss(tr:0.19814154107014398,
2016-05-15 19:19:26.622807, i:28, param:0.2800044, log-loss(tr:0.19216680670073683,
2016-05-15 19:19:29.069105, i:29, param:0.2900042, log-loss(tr:0.1864067501148142,
2016-05-15 19:19:31.536516, i:30, param:0.300004, log-loss(tr:0.18085411730767686,
2016-05-15 19:19:33.996924, i:31, param:0.3100038, log-loss(tr:0.17550184285153478,
2016-05-15 19:19:36.498372, i:32, param:0.3200036, log-loss(tr:0.17034304121095803,
2016-05-15 19:19:38.983521, i:33, param:0.3300034, log-loss(tr:0.16537100134042287,
2016-05-15 19:19:41.460634, i:34, param:0.3400032, log-loss(tr:0.16057918359063408,
2016-05-15 19:19:43.913118, i:35, param:0.350003, log-loss(tr:0.15596121816132288,
```

```
2016-05-15 19:19:46.395698, i:36, param:0.3600028, log-loss(tr:0.15151090451377108,
2016-05-15 19:19:48.901747, i:37, param:0.3700026, log-loss(tr:0.14722221130140406,
2016-05-15 19:19:51.453383, i:38, param:0.3800024, log-loss(tr:0.14308927649482833,
2016-05-15 19:19:53.949050, i:39, param:0.3900022, log-loss(tr:0.1391064074719948,
2016-05-15 19:19:56.593939, i:40, param:0.400002, log-loss(tr:0.13526808091785408,
2016-05-15 19:19:59.208022, i:41, param:0.4100018, log-loss(tr:0.13156894243392878,
2016-05-15 19:20:01.845362, i:42, param:0.4200016, log-loss(tr:0.12800380580008303,
2016-05-15 19:20:04.499336, i:43, param:0.4300014, log-loss(tr:0.12456765186107348,
2016-05-15 19:20:07.128090, i:44, param:0.4400012, log-loss(tr:0.12125562703205937,
2016-05-15 19:20:09.839833, i:45, param:0.450001, log-loss(tr:0.11806304143224787,
2016-05-15 19:20:12.373601, i:46, param:0.4600008, log-loss(tr:0.11498536666598914,
2016-05-15 19:20:14.901587, i:47, param:0.4700006, log-loss(tr:0.11201823327733958,
2016-05-15 19:20:17.388313, i:48, param:0.4800004, log-loss(tr:0.10915742790822434,
2016-05-15 19:20:20.357713, i:49, param:0.4900002, log-loss(tr:0.10639889019269375,
---Total execution time: 127.17217421531677 seconds ---
In [30]: plt.figure(num=None, figsize=(13, 6), dpi=80, facecolor='w', edgecolor='k
         plt.plot(arr_alpha, arr_log_loss_sqd_train_best_alpha, marker='o', color='
         plt.plot(arr_alpha, arr_log_loss_sgd_test_best_alpha, marker='o', color='b
        plt.legend(loc="upper right")
        plt.xlabel('alpha')
         plt.ylabel('log-loss per iteration')
        plt.title('Best alpha')
         ndarr_test = np.array(arr_log_loss_sqd_test_best_alpha)
         print((ndarr_test.argmin(), arr_alpha[ndarr_test.argmin()], arr_log_loss_s
         plt.axvline(arr_alpha[ndarr_test.argmin()], color = 'g')
         if(TEST_DATA == 'T'):
             plt.savefig('./images/best_param_sqd_T.png')
         elif(TEST_DATA == 'C'):
             plt.savefig('./images/best_param_sgd_C.png')
(11, 0.11000779999999999, 0.46879230769345764)
```



#### ADF: variance

, arr\_log\_loss\_ac
, arr\_log\_loss\_ac

```
arr log loss adf test best var = [0] *len(arr var)
             for i in range(0,len(arr_var)):
                 param, arr_y, arr_log_loss_adf_train_best_var[i], arr_log_l
                          D = 2 * * 20
                          , f_debug = False
                          , f_step_validation = False
                          , f_validation = True
                          , c_ds = ds_best_param_criteo
                          , c_fi = fi_criteo)
                 print('%s, i:%s, param:%s, log-loss(tr:%s, te:%s)' %(datetime.now
                                                                   , arr_log_loss_ad
                                                                   , arr_log_loss_ad
        print("---Total execution time: %s seconds ---" % (time.time() - start_tir
2016-05-15 19:20:24.258864, i:0, param:0.0001, log-loss(tr:0.5637217661946521, te:0
2016-05-15 19:20:27.771373, i:1, param:0.004098, log-loss(tr:0.46689164684935613, t
2016-05-15 19:20:31.266933, i:2, param:0.008096, log-loss(tr:0.445533737645424, te
2016-05-15 19:20:34.740558, i:3, param:0.012094, log-loss(tr:0.4301030735201744, te
2016-05-15 19:20:38.226082, i:4, param:0.016092, log-loss(tr:0.4173842836044793, te
2016-05-15 19:20:41.699137, i:5, param:0.02009, log-loss(tr:0.40631207028069116, te
2016-05-15 19:20:45.188574, i:6, param:0.024088, log-loss(tr:0.39638550121913496, t
2016-05-15 19:20:48.678943, i:7, param:0.028086, log-loss(tr:0.3873222840303443, te
2016-05-15 19:20:52.170037, i:8, param:0.032084, log-loss(tr:0.37894435757683514, t
2016-05-15 19:20:55.626155, i:9, param:0.036082, log-loss(tr:0.3711303974374177, te
2016-05-15 19:20:59.111580, i:10, param:0.04008, log-loss(tr:0.3637929745511456, te
2016-05-15 19:21:02.556638, i:11, param:0.044078, log-loss(tr:0.3568663589052846, t
2016-05-15 19:21:06.040187, i:12, param:0.048076, log-loss(tr:0.35029947395238337,
2016-05-15 19:21:09.504786, i:13, param:0.052074, log-loss(tr:0.3440515680937664, t
2016-05-15 19:21:12.971294, i:14, param:0.056072, log-loss(tr:0.33808942041398166,
2016-05-15 19:21:16.437357, i:15, param:0.06007, log-loss(tr:0.33238546190535784, t
2016-05-15 19:21:19.905849, i:16, param:0.064068, log-loss(tr:0.3269164684984574, t
```

arr\_var = list(np.linspace(.0001, .2, 50, endpoint=False))

arr\_log\_loss\_adf\_train\_best\_var = [0] \*len(arr\_var)

elif(TEST\_DATA == 'C'):

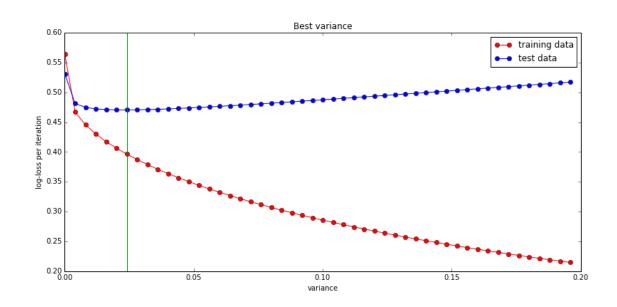
```
2016-05-15 19:21:23.455439, i:17, param:0.068066, log-loss(tr:0.3216626252400433, t
2016-05-15 19:21:26.963486, i:18, param:0.072064, log-loss(tr:0.3166068394155937, t
2016-05-15 19:21:30.410144, i:19, param:0.076062, log-loss(tr:0.31173422545066, te
2016-05-15 19:21:33.853347, i:20, param:0.08006, log-loss(tr:0.3070317113106935, te
2016-05-15 19:21:37.342972, i:21, param:0.084058, log-loss(tr:0.30248773272404456,
2016-05-15 19:21:40.828997, i:22, param:0.088056, log-loss(tr:0.2980919921202278, t
2016-05-15 19:21:44.277501, i:23, param:0.092054, log-loss(tr:0.29383526608085425,
2016-05-15 19:21:47.733888, i:24, param:0.096052, log-loss(tr:0.2897092497211826, t
2016-05-15 19:21:51.218437, i:25, param:0.10005, log-loss(tr:0.2857064295777301, te
2016-05-15 19:21:54.667410, i:26, param:0.104048, log-loss(tr:0.28181997877732956,
2016-05-15 19:21:58.138656, i:27, param:0.108046, log-loss(tr:0.27804366982226636,
2016-05-15 19:22:01.614402, i:28, param:0.112044, log-loss(tr:0.27437180144884316,
2016-05-15 19:22:05.076941, i:29, param:0.116042, log-loss(tr:0.2707991368372623, t
2016-05-15 19:22:08.539569, i:30, param:0.12004, log-loss(tr:0.2673208510578796, te
2016-05-15 19:22:12.013810, i:31, param:0.124038, log-loss(tr:0.26393248609418846,
2016-05-15 19:22:15.489362, i:32, param:0.128036, log-loss(tr:0.2606299121278021, t
2016-05-15 19:22:18.951238, i:33, param:0.132034, log-loss(tr:0.25740929403499346,
2016-05-15 19:22:22.428446, i:34, param:0.136032, log-loss(tr:0.25426706224865464,
2016-05-15 19:22:25.966940, i:35, param:0.14003, log-loss(tr:0.2511998872990525, te
2016-05-15 19:22:29.449886, i:36, param:0.144028, log-loss(tr:0.24820465747223838,
2016-05-15 19:22:32.988042, i:37, param:0.148026, log-loss(tr:0.24527845912454577,
2016-05-15 19:22:36.485105, i:38, param:0.152024, log-loss(tr:0.24241855927113568,
2016-05-15 19:22:39.950072, i:39, param:0.156022, log-loss(tr:0.23962239013059247,
2016-05-15 19:22:43.440689, i:40, param:0.16002, log-loss(tr:0.2368875353594199, te
2016-05-15 19:22:46.909658, i:41, param:0.164018, log-loss(tr:0.2342117177525089, t
2016-05-15 19:22:50.398607, i:42, param:0.168016, log-loss(tr:0.23159278822034302,
2016-05-15 19:22:53.861929, i:43, param:0.172014, log-loss(tr:0.22902871588217408,
2016-05-15 19:22:57.316025, i:44, param:0.176012, log-loss(tr:0.22651757913813678,
2016-05-15 19:23:00.769991, i:45, param:0.18001, log-loss(tr:0.2240575576028691, te
2016-05-15 19:23:04.219845, i:46, param:0.184008, log-loss(tr:0.2216469247997548, t
2016-05-15 19:23:07.672859, i:47, param:0.188006, log-loss(tr:0.2192840415286861, t
2016-05-15 19:23:11.145391, i:48, param:0.192004, log-loss(tr:0.21696734983194516,
2016-05-15 19:23:14.601891, i:49, param:0.196002, log-loss(tr:0.21469536749268522,
---Total execution time: 173.89910197257996 seconds ---
```

```
In [32]: plt.figure(num=None, figsize=(13, 6), dpi=80, facecolor='w', edgecolor='k
    plt.plot(arr_var, arr_log_loss_adf_train_best_var, marker='o', color= 'r',
    plt.plot(arr_var, arr_log_loss_adf_test_best_var, marker='o', color= 'b',
    plt.legend(loc="upper right")
    plt.xlabel('variance')
    plt.ylabel('log-loss per iteration')
    plt.title('Best variance')

    ndarr_test = np.array(arr_log_loss_adf_test_best_var)
    print((ndarr_test.argmin(), arr_var[ndarr_test.argmin()], arr_log_loss_adf
    plt.axvline(arr_var[ndarr_test.argmin()], color = 'g')

    if(TEST_DATA == 'T'):
        plt.savefig('./images/best_param_adf_T.png')
    elif(TEST_DATA == 'C'):
        plt.savefig('./images/best_param_adf_C.png')

(6, 0.0240880000000000000, 0.470400456729436)
```



# 제 7 절 Tracing log-loss as the number of sample grows(step\_validation)

```
In [54]: ds_step_vali_titanic = DataSize(np.round(800/50) # num_metric_check_y
                             , 1 # num_status_check_point
                             , 1, 800 #train_start, train_size
                             , 801, 91) #test_start, test_size
       ds_step_vali_criteo = DataSize(np.round(1000/50) # num_metric_check_p
                             , 1 # num_status_check_point
                             ds_step_vali_criteo = DataSize(np.round(10000/50) # num_metric_check_
                             , 1 # num_status_check_point
                             , 1, 10000 #train_start, train_size
                             , 10001, 1000)
                                           #test_start, test_size
       ds_step_vali_criteo = DataSize(np.round(1000000/50) # num_metric_chec
                             , 1 # num_status_check_point
                             , 1, 10000000 #train_start, train_size
                             , 10000001, 100000) #test_start, test_size
       ds_step_vali_titanic.display()
       ds_step_vali_criteo.display()
num_metric_check_point: 16.0
num_status_check_point: 1
num_train_data_start : 1
num_train_data_end : 800
num_train_data_size : 800
num_test_data_start : 801
num_test_data_end : 891
num_test_data_size : 91
num_metric_check_point: 20000.0
num_status_check_point: 1
num_train_data_start : 1
```

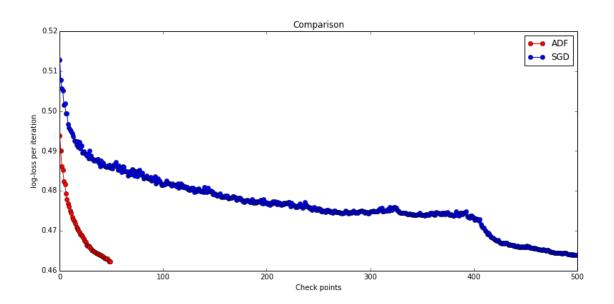
```
num_train_data_end : 10000000
num_train_data_size : 10000000
num_test_data_start : 10000001
num_test_data_end
                   : 10100000
num_test_data_size : 100000
  SGD
In [55]: start_time = time.time()
        if(TEST_DATA == 'T'):
            alpha = 0.9200053999999999 # best for titanic
            arr_log_loss_sqd_test = sqd_training(alpha = alpha
                                                     D = 2 * * 20
                                                     , f_debug = False
                                                     , f_step_validation = True
                                                     , f_validation = False
                                                     , c_ds = ds_step_vali_titanio
                                                     #, c_ds = ds_step_vali_crited
                                                     , c_fi = fi_titanic)
                                                     \#, c_fi = fi_criteo)
        elif(TEST_DATA == 'C'):
            alpha = 0.100008 # best for criteo
            arr_log_loss_sgd_test = sgd_training(alpha = alpha
                                                     D = 2 * * 20
                                                     , f_debug = False
                                                     , f_step_validation = True
                                                     , f_validation = False
                                                     #, c_ds = ds_step_vali_titans
                                                     , c_ds = ds_step_vali_criteo
                                                     \#, c_{fi} = fi_{titanic}
                                                     , c_fi = fi_criteo)
        print("---Total execution time: %s seconds ---" % (time.time() - start_tir
---Total execution time: 81738.79210209846 seconds ---
```

```
ndarr_log_loss_sgd_test = np.array(arr_log_loss_sgd_test)
       (ndarr_log_loss_sgd_test.argmin(), arr_log_loss_sgd_test[ndarr_log_loss_sgd_test]
       if(TEST_DATA == 'T'):
           plt.savefig('./images/step_vali_sgd_T.png')
       elif(TEST_DATA == 'C'):
           plt.savefig('./images/step_vali_sgd_C.png')
 0.52
 0.51
 0.50
 0.49
 0.48
 0.47
 0.46 L
ADF
```

In [56]: plot\_log\_loss(arr\_log\_loss\_sgd\_test)

```
, f_validation = False
                                                        , c_ds = ds_step_vali_titanio
                                                        #, c_ds = ds_step_vali_crited
                                                        , c_fi = fi_titanic)
                                                        \#, c_fi = fi_criteo)
         elif(TEST_DATA == 'C'):
             init_v = 0.024088000000000000 # best for criteo
             arr_log_loss_adf_test = adf_training(variance = init_v
                                                        D = 2 * * 20
                                                        , f_debug = False
                                                        , f_step_validation = True
                                                        , f_validation = False
                                                        \#, c_ds = ds_step_vali_titans
                                                        , c_ds = ds_step_vali_criteo
                                                        \#, c_{fi} = fi_{titanic}
                                                        , c_fi = fi_criteo)
         print("---Total execution time: %s seconds ---" % (time.time() - start_tir
---Total execution time: 1596.8921689987183 seconds ---
In [1]: plot_log_loss(arr_log_loss_adf_test)
        ndarr_log_loss_adf_test = np.array(arr_log_loss_adf_test)
        (ndarr_log_loss_adf_test.argmin(), arr_log_loss_adf_test[ndarr_log_loss_adf_
        if(TEST_DATA == 'T'):
            plt.savefig('./images/step_vali_adf_T.png')
        elif(TEST_DATA == 'C'):
            plt.savefig('./images/step_vali_adf_C.png')
        NameError
                                                   Traceback (most recent call last)
```

```
<ipython-input-1-a2984bd84b03> in <module>()
    ----> 1 plot_log_loss(arr_log_loss_adf_test)
          2
          3 ndarr_log_loss_adf_test = np.array(arr_log_loss_adf_test)
          4 (ndarr_log_loss_adf_test.argmin(), arr_log_loss_adf_test[ndarr_log_loss
        NameError: name 'plot_log_loss' is not defined
In [57]: plt.figure(num=None, figsize=(13, 6), dpi=80, facecolor='w', edgecolor='k
         x1 = range(len(arr_log_loss_adf_test))
        plt.plot(x1, arr_log_loss_adf_test, marker='o', color = 'r', label='ADF')
         x2 = range(len(arr_log_loss_sgd_test))
         plt.plot(x2, arr_log_loss_sqd_test, marker='o', color = 'b', label='SGD')
        plt.legend(loc="upper right")
         plt.xlabel('Check points')
        plt.ylabel('log-loss per iteration')
         plt.title('Comparison')
         if(TEST_DATA == 'T'):
             plt.savefig('./images/step_vali_comparison_T.png')
         elif(TEST_DATA == 'C'):
             plt.savefig('./images/step_vali_comparison_C.png')
```



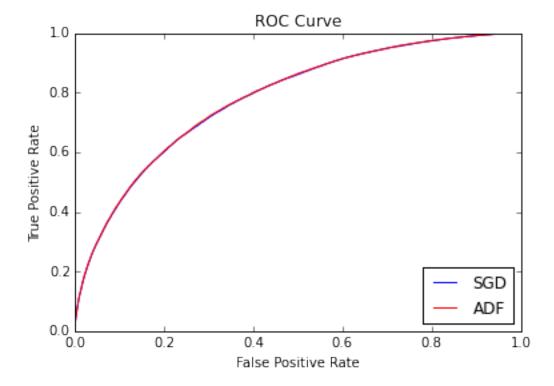
# 제 8 절 ?

```
if(TEST_DATA == 'T'):
             alpha = 0.92000539999999999 # best for titanic
             param_w, arr_sqd_y, arr_sqd_p, log_loss_sqd_train, log_loss_sqd_test =
                                                       D = 2 * * 20
                                                       , f_debug = False
                                                       , f_step_validation = False
                                                       , f_validation = True
                                                       , c_ds = ds_more_vali_titanic
                                                       , c_fi = fi_titanic)
         elif(TEST_DATA == 'C'):
             alpha = 0.100008 # best for criteo
             param_w, arr_sgd_y, arr_sgd_p, log_loss_sgd_train, log_loss_sgd_test =
                                                       D = 2 * * 20
                                                       , f_debug = False
                                                       , f_step_validation = False
                                                       , f_validation = True
                                                       , c_ds = ds_more_vali_criteo
                                                       , c_fi = fi_criteo)
         print("---Total execution time: %s seconds ---" % (time.time() - start tir
---Total execution time: 170.86889100074768 seconds ---
  ADF
In [51]: start_time = time.time()
         if(TEST_DATA == 'T'):
             init_v = 0.5200739999999999 # best for titanic
             #init_v = 0.00520073999999999 # best for titanic
             param_theta, arr_adf_y, arr_adf_p, log_loss_adf_train, log_loss_adf_te
                                                       D = 2 * * 20
                                                       , f_debug = False
                                                       , f_step_validation = False
                                                       , f_validation = True
```

```
, c_ds = ds_more_vali_titanic
                                                    , c_fi = fi_titanic)
        elif(TEST_DATA == 'C'):
            param_theta, arr_adf_y, arr_adf_p, log_loss_adf_train, log_loss_adf_te
                                                    D = 2 * * 20
                                                    , f_debug = False
                                                    , f_step_validation = False
                                                    , f_validation = True
                                                    , c_ds = ds_more_vali_criteo
                                                    , c_fi = fi_criteo)
        print("---Total execution time: %s seconds ---" % (time.time() - start_tir
---Total execution time: 276.404109954834 seconds ---
  Comparison
In [52]: #fpr_sgd = dict()
        #tpr_sqd = dict()
        #roc_auc_sqd = dict()
        fpr_sgd, tpr_sgd, _ = roc_curve(arr_sgd_y, arr_sgd_p)
        roc_auc_sqd = auc(fpr_sqd, tpr_sqd) #auc
        fpr_adf, tpr_adf, _ = roc_curve(arr_adf_y, arr_adf_p)
        roc_auc_adf = auc(fpr_adf, tpr_adf) #auc
        plt.figure()
        plt.plot(fpr_sgd, tpr_sgd, label='SGD', color='b')
        plt.plot(fpr_adf, tpr_adf, label='ADF', color='r')
        plt.xlabel('False Positive Rate')
        plt.ylabel('True Positive Rate')
```

```
plt.title('ROC Curve')
plt.legend(loc="lower right")
#plt.show() # or use command %matplotlib inline

if(TEST_DATA == 'T'):
    plt.savefig('./images/step_vali_roc_T.png')
elif(TEST_DATA == 'C'):
    plt.savefig('./images/step_vali_roc_C.png')
```



```
In [53]: (roc_auc_sgd, roc_auc_adf)
Out[53]: (0.78110714529429526, 0.78198942683050354)
In [ ]:
In [ ]:
In [ ]:
```

- In [ ]:
- In [ ]:
- In [ ]: