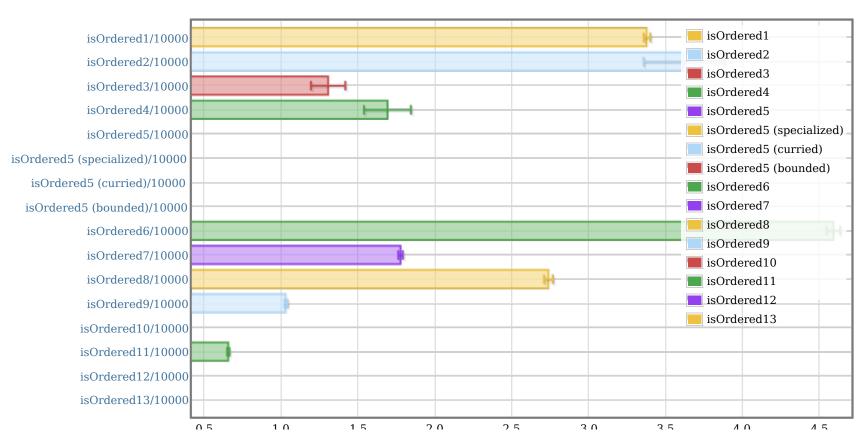
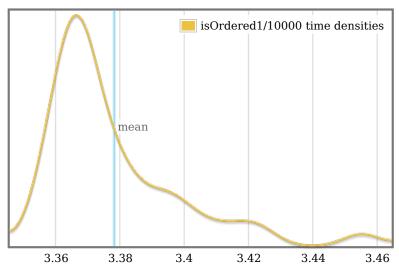
# criterion performance measurements overview

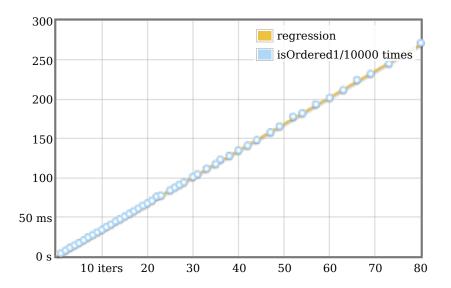
want to understand this report?



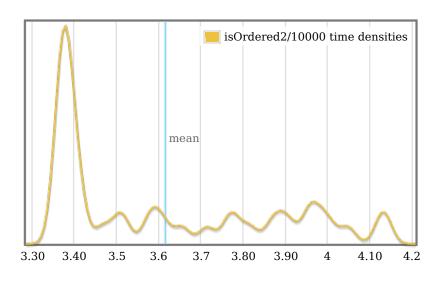
## isOrdered1/10000

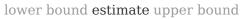


lower bound estimate upper bound

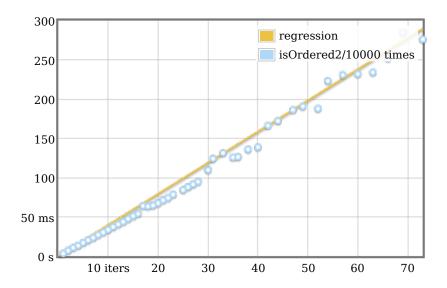


## isOrdered2/10000

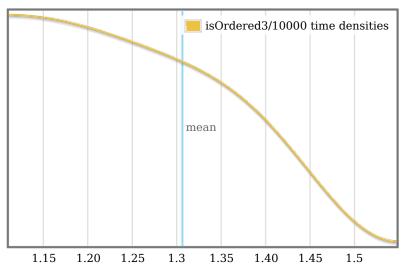




OLS regression	3.85 ms	3.96  ms	4.09 ms
R <sup>2</sup> goodness-of-fit	0.989	0.992	0.996
Mean execution time	3.54 ms	$3.62 \; \text{ms}$	3.70 ms
Standard deviation	225 µs	261 µs	304 µs



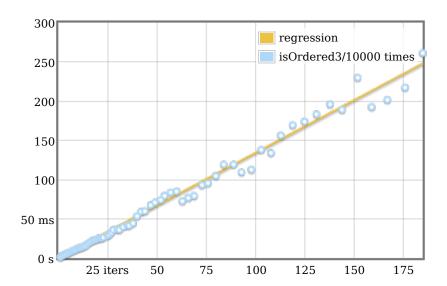
## isOrdered3/10000



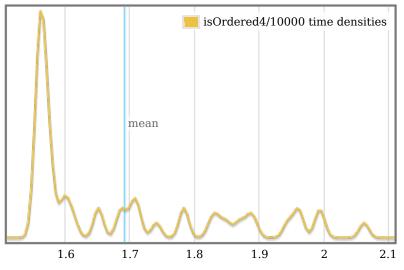
lower bound estimate upper bound

OLS regression 1.28 ms 1.  $R^2$  goodness-of-fit 0.981 0. Mean execution time 1.27 ms 1. Standard deviation 101  $\mu$ s 11

1.34 ms 1.40 ms 0.986 0.992 1.31 ms 1.34 ms 112 µs 128 µs



## isOrdered4/10000



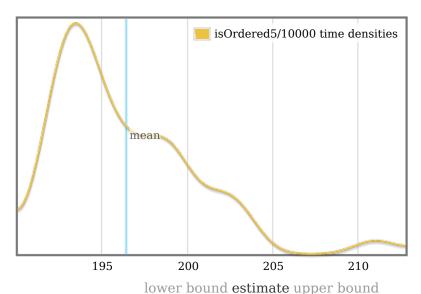
lower bound estimate upper bound

OLS regression 1.51 ms  $R^2$  goodness-of-fit 0.993 Mean execution time 1.65 ms Standard deviation 130  $\mu s$ 

1.53 ms 1.54 ms 0.996 0.998 1.69 ms 1.74 ms 153 µs 181 µs

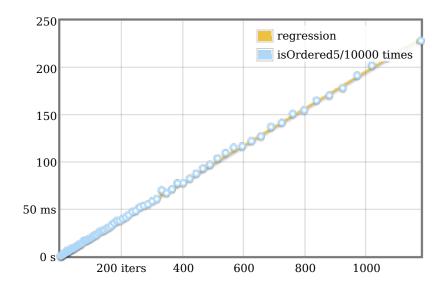


## isOrdered5/10000

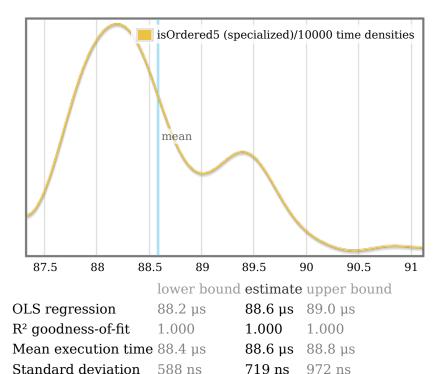


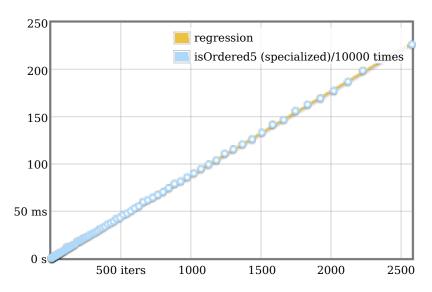
OLS regression 195  $\mu s$  196  $\mu s$  197  $\mu s$  R<sup>2</sup> goodness-of-fit 0.999 1.000 1.000 Mean execution time 195  $\mu s$  196  $\mu s$  198  $\mu s$ 

Standard deviation  $3.15~\mu s$   $4.00~\mu s$   $5.86~\mu s$ 

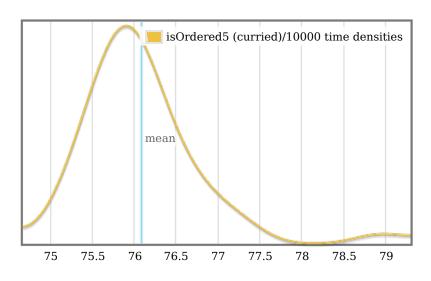


## isOrdered5 (specialized)/10000



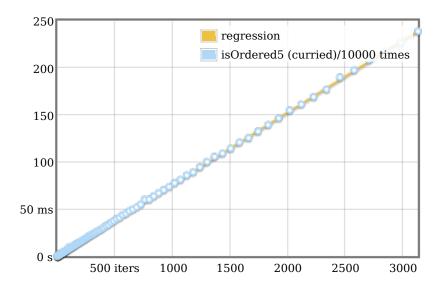


# isOrdered5 (curried)/10000

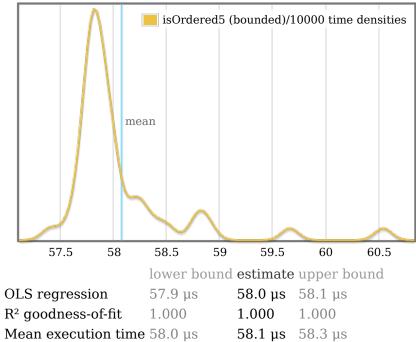


lower bound estimate upper bound

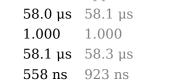
OLS regression	76.0 μs	76.2 μs	76.5 μs
R <sup>2</sup> goodness-of-fit	1.000	1.000	1.000
Mean execution time	75.9 μs	$76.1~\mu s$	76.3 µs
Standard deviation	474 ns	669 ns	1.14 us

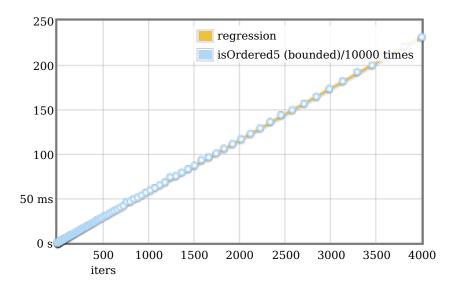


## isOrdered5 (bounded)/10000

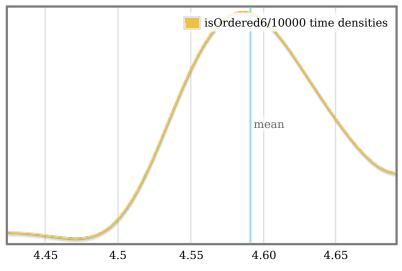


Standard deviation 340 ns



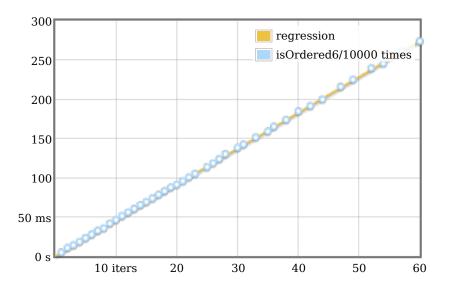


## isOrdered6/10000

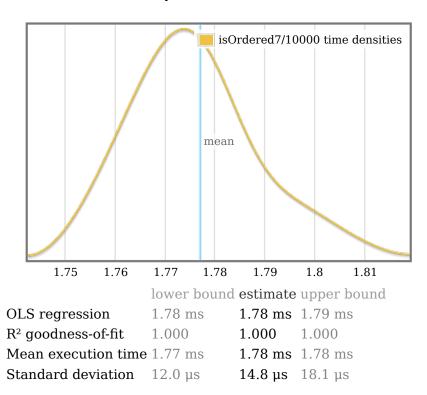


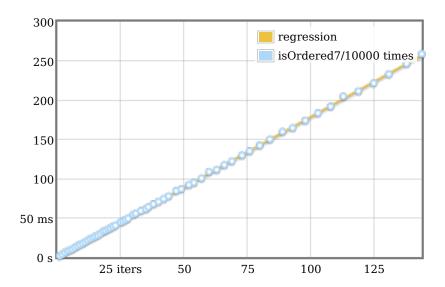
lower bound estimate upper bound

OLS regression 4.54 ms 4.56 ms 4.58 ms  $R^2$  goodness-of-fit 1.000 1.000 1.000 Mean execution time 4.57 ms 4.59 ms 4.60 ms Standard deviation 35.9  $\mu$ s 45.0  $\mu$ s 65.9  $\mu$ s

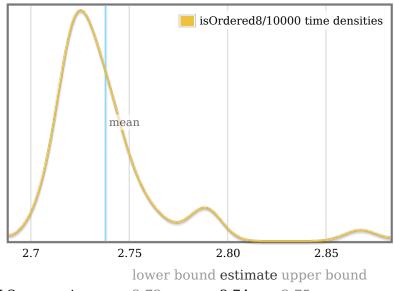


## isOrdered7/10000





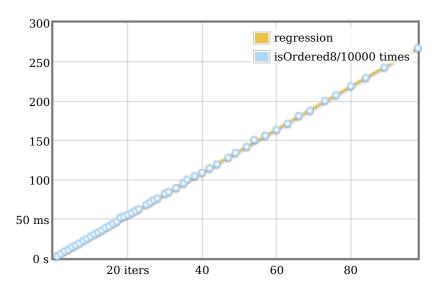
## isOrdered8/10000



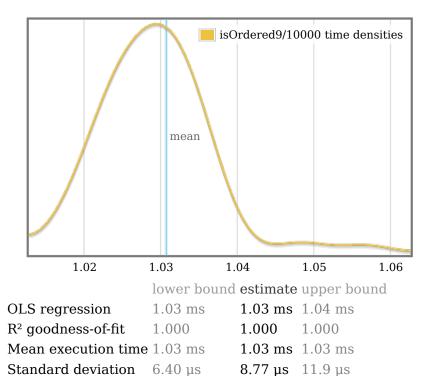
**OLS** regression 2.73 ms 2.74 ms 2.75 ms

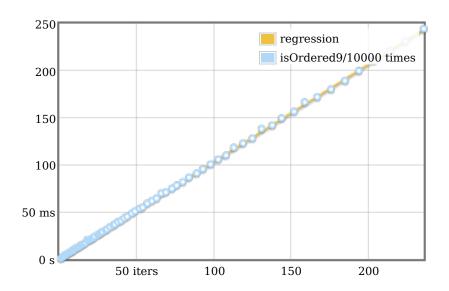
R<sup>2</sup> goodness-of-fit 1.000 1.000 1.000 Mean execution time 2.73 ms

2.74 ms 2.75 ms Standard deviation 18.8 µs **28.5 μs** 45.2 μs



## isOrdered9/10000

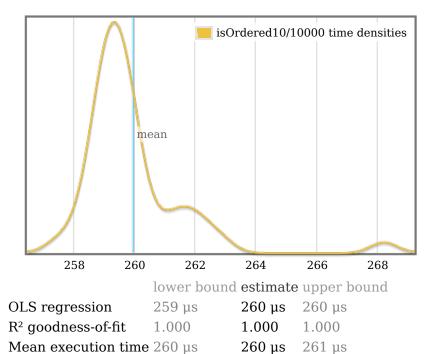


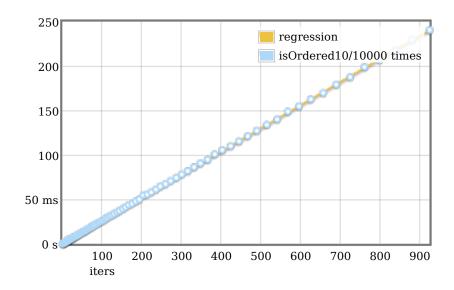


1.72 μs 3.00 μs

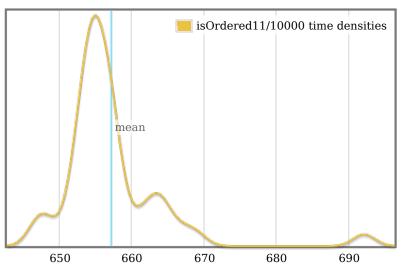
## isOrdered10/10000

Standard deviation  $1.05 \mu s$ 



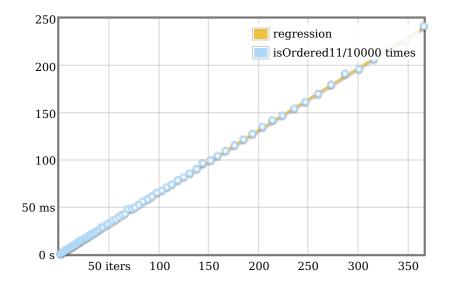


## isOrdered11/10000

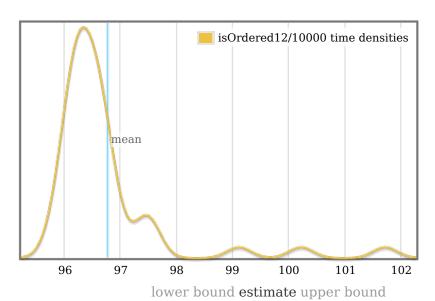


lower bound estimate upper bound

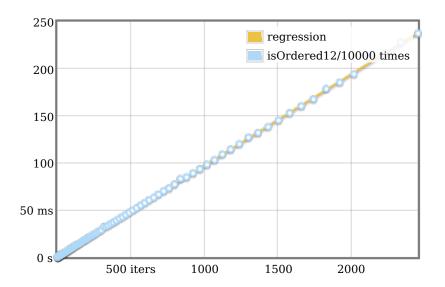
OLS regression	655 μs	658 µs	660 µs
R <sup>2</sup> goodness-of-fit	1.000	1.000	1.000
Mean execution time	656 μs	657 µs	660 µs
Standard deviation	4.27 μs	7.14 µs	13.3 µs



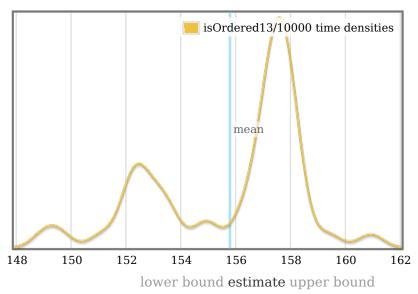
## isOrdered12/10000



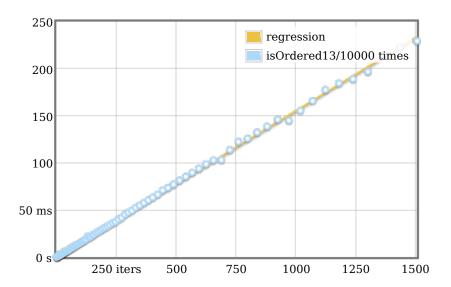
OLS regression 96.5  $\mu$ s 97.0  $\mu$ s 97.6  $\mu$ s R<sup>2</sup> goodness-of-fit 1.000 1.000 1.000 Mean execution time 96.5  $\mu$ s 96.8  $\mu$ s 97.2  $\mu$ s Standard deviation 601 ns 1.10  $\mu$ s 1.89  $\mu$ s



## isOrdered13/10000



OLS regression 154  $\mu s$  155  $\mu s$  156  $\mu s$  R<sup>2</sup> goodness-of-fit 0.999 0.999 1.000 Mean execution time 155  $\mu s$  156  $\mu s$  157  $\mu s$  Standard deviation 2.28  $\mu s$  2.76  $\mu s$  3.36  $\mu s$ 



#### understanding this report

In this report, each function benchmarked by criterion is assigned a section of its own. The charts in each section are active; if you hover your mouse over data points and annotations, you will see more details.

- The chart on the left is a kernel density estimate (also known as a KDE) of time measurements. This graphs the probability of any given time measurement occurring. A spike indicates that a measurement of a particular time occurred; its height indicates how often that measurement was repeated.
- The chart on the right is the raw data from which the kernel density estimate is built. The x axis indicates the number of loop iterations, while the y axis shows measured execution time for the given number of loop iterations. The line behind the values is the linear regression prediction of execution time for a given number of iterations. Ideally, all measurements will be on (or very near) this line.

Under the charts is a small table. The first two rows are the results of a linear regression run on the measurements displayed in the right-hand chart.

- *OLS regression* indicates the time estimated for a single loop iteration using an ordinary least-squares regression model. This number is more accurate than the *mean* estimate below it, as it more effectively eliminates measurement overhead and other constant factors.
- *R*<sup>2</sup> *goodness-of-fit* is a measure of how accurately the linear regression model fits the observed measurements. If the measurements are not too noisy, R<sup>2</sup> should lie between 0.99 and 1, indicating an excellent fit. If the number is below 0.99, something is confounding the accuracy of the linear model.
- Mean execution time and standard deviation are statistics calculated from execution time divided by number of iterations.

We use a statistical technique called the bootstrap to provide confidence intervals on our estimates. The bootstrap-derived upper and lower bounds on estimates let you see how accurate we believe those estimates to be. (Hover the mouse over the table headers to see the confidence levels.)

A noisy benchmarking environment can cause some or many measurements to fall far from the mean. These outlying measurements can have a significant inflationary effect on the estimate of the standard deviation. We calculate and display an estimate of the extent to which the standard deviation has been inflated by outliers.

# colophon

This report was created using the  $\underline{\text{criterion}}$  benchmark execution and performance analysis tool.

Criterion is developed and maintained by Bryan O'Sullivan.