



Chapter 9: Virtual Memory

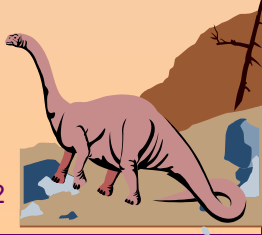
- Background
- Demand Paging
- Process Creation
- Page Replacement
- Allocation of Frames
- Thrashing
- Operating System Examples



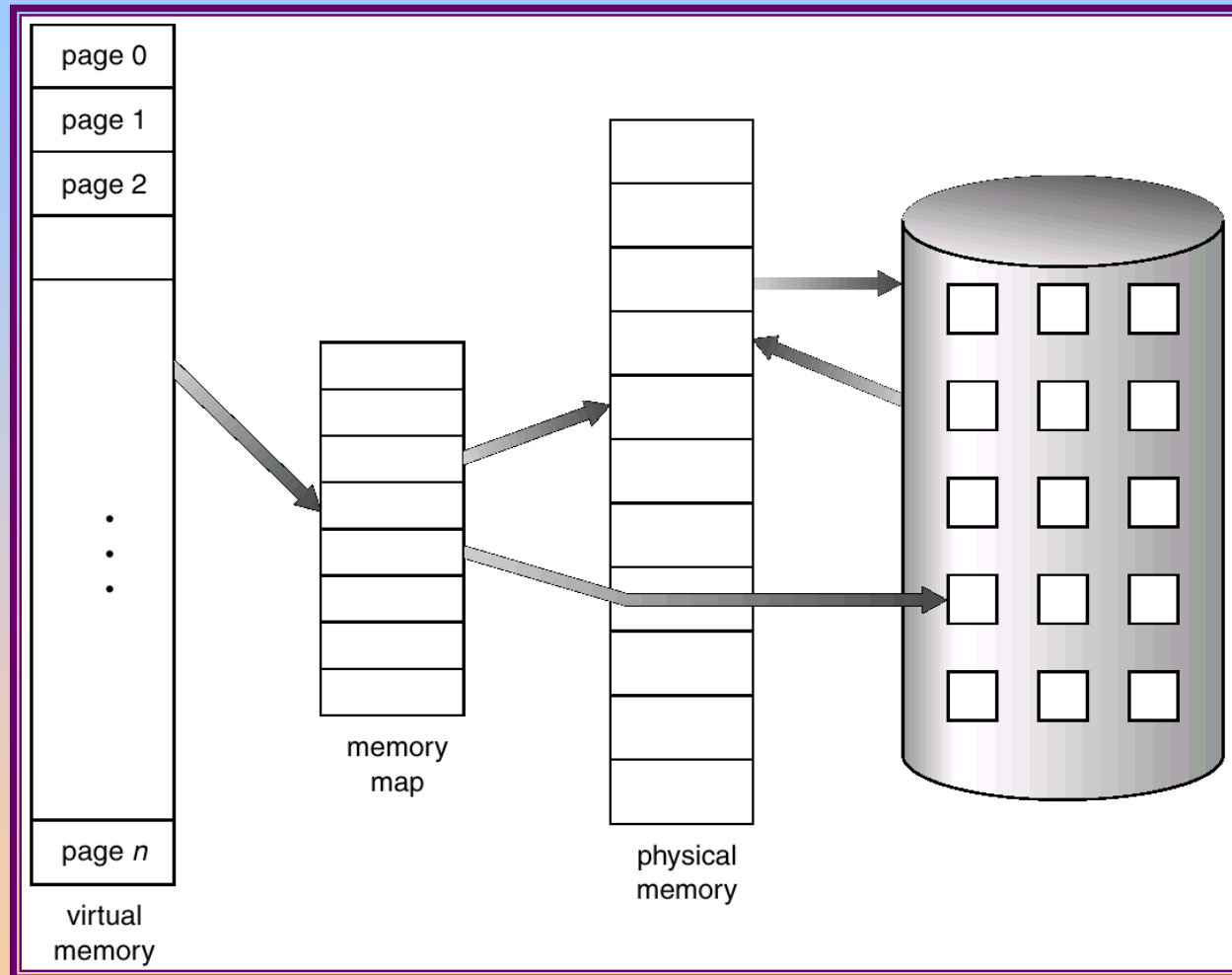


Background

- **Virtual memory** – separation of user logical memory from physical memory.
 - Only part of the program needs to be in memory for execution.
 - Logical address space can therefore be much larger than physical address space.
 - Allows address spaces to be shared by several processes.
 - Allows for more efficient process creation.
- Virtual memory can be implemented via:
 - Demand paging
 - Demand segmentation



Virtual Memory That is Larger Than Physical Memory





Demand Paging

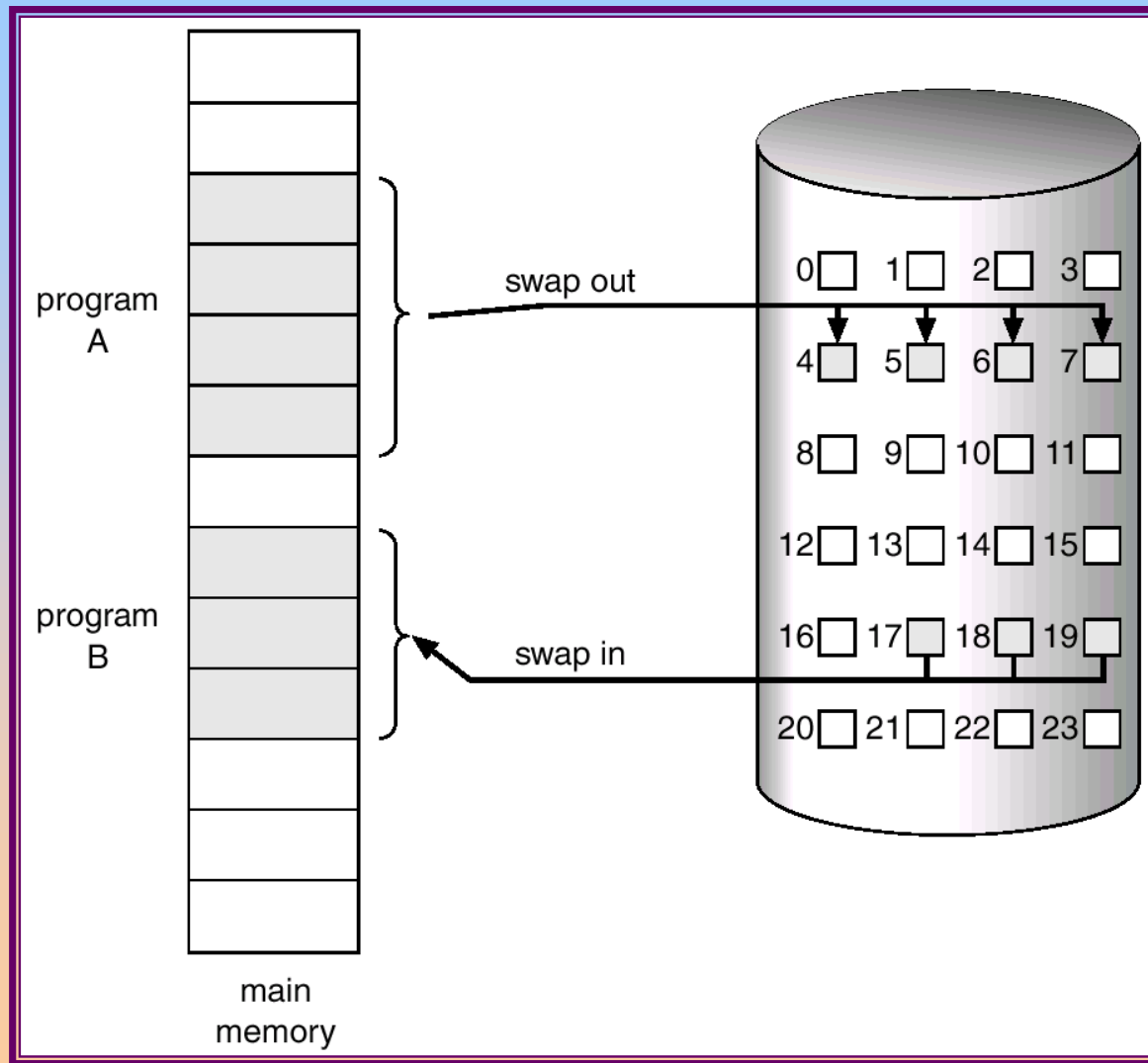
- Bring a page into memory only when it is needed.
 - Less I/O needed
 - Less memory needed
 - Faster response
 - More users

- Page is needed \Rightarrow reference to it
 - invalid reference \Rightarrow abort
 - not-in-memory \Rightarrow bring to memory





Transfer of a Paged Memory to Contiguous Disk Space





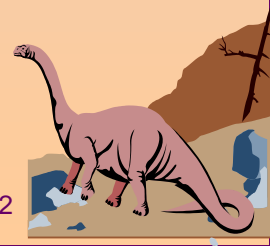
Valid-Invalid Bit

- With each page table entry a valid–invalid bit is associated
(1 \Rightarrow in-memory, 0 \Rightarrow not-in-memory)
- Initially valid–invalid but is set to 0 on all entries.
- Example of a page table snapshot.

Frame #	valid-invalid bit
	1
	1
	1
	1
	0
⋮	
	0
	0

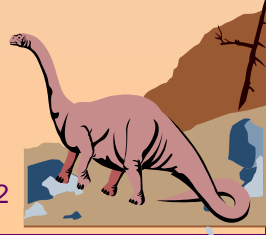
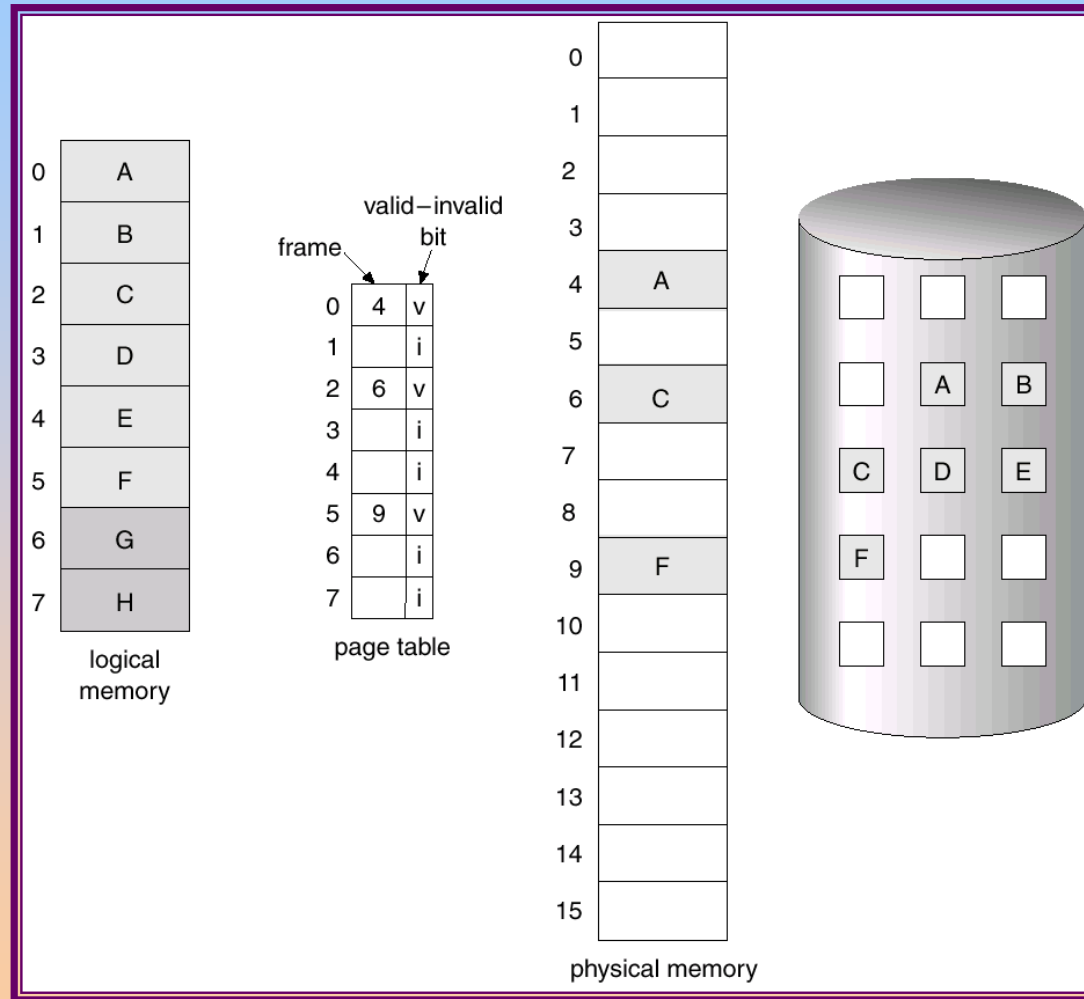
page table

- During address translation, if valid–invalid bit in page table entry is 0 \Rightarrow page fault.





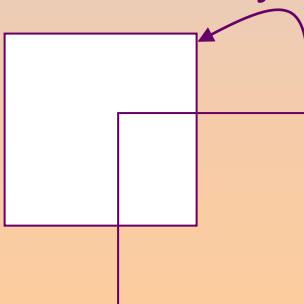
Page Table When Some Pages Are Not in Main Memory





Page Fault

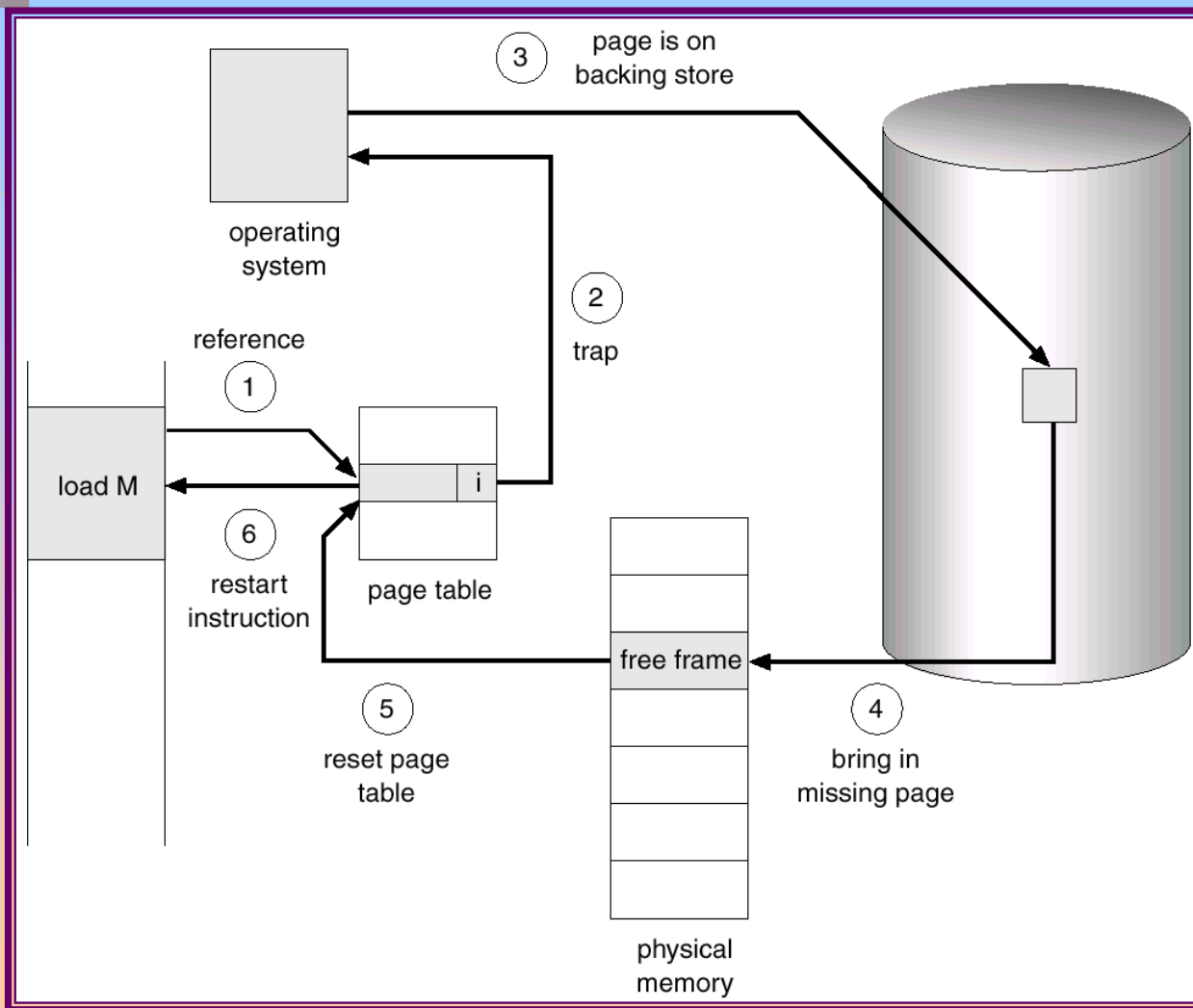
- ❑ If there is ever a reference to a page, first reference will trap to OS \Rightarrow page fault
- ❑ OS looks at another table to decide:
 - ❑ Invalid reference \Rightarrow abort.
 - ❑ Just not in memory.
- ❑ Get empty frame.
- ❑ Swap page into frame.
- ❑ Reset tables, validation bit = 1.
- ❑ Restart instruction: Least Recently Used
 - ❑ block move



- ❑ auto increment/decrement location



Steps in Handling a Page Fault





What happens if there is no free frame?

- Page replacement – find some page in memory, but not really in use, swap it out.
 - algorithm
 - performance – want an algorithm which will result in minimum number of page faults.
- Same page may be brought into memory several times.





Performance of Demand Paging

- Page Fault Rate $0 \leq p \leq 1.0$
 - if $p = 0$ no page faults
 - if $p = 1$, every reference is a fault

- Effective Access Time (EAT)

$$\begin{aligned} \text{EAT} = & (1 - p) \times \text{memory access} \\ & + p (\text{page fault overhead} \\ & + [\text{swap page out}] \\ & + \text{swap page in} \\ & + \text{restart overhead}) \end{aligned}$$





Demand Paging Example

- ❑ Memory access time = 1 microsecond
- ❑ 50% of the time the page that is being replaced has been modified and therefore needs to be swapped out.
- ❑ Swap Page Time = 10 msec = 10,000 msec

$$\begin{aligned} \text{EAT} &= (1 - p) \times 1 + p (15000) \\ &= 1 + 15000P \quad (\text{in msec}) \end{aligned}$$





Process Creation

- Virtual memory allows other benefits during process creation:
 - Copy-on-Write
 - Memory-Mapped Files



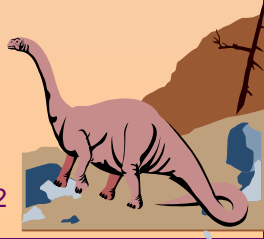


Copy-on-Write

- ❑ Copy-on-Write (COW) allows both parent and child processes to initially *share* the same pages in memory.

If either process modifies a shared page, only then is the page copied.

- ❑ COW allows more efficient process creation as only modified pages are copied.
- ❑ Free pages are allocated from a *pool* of zeroed-out pages.



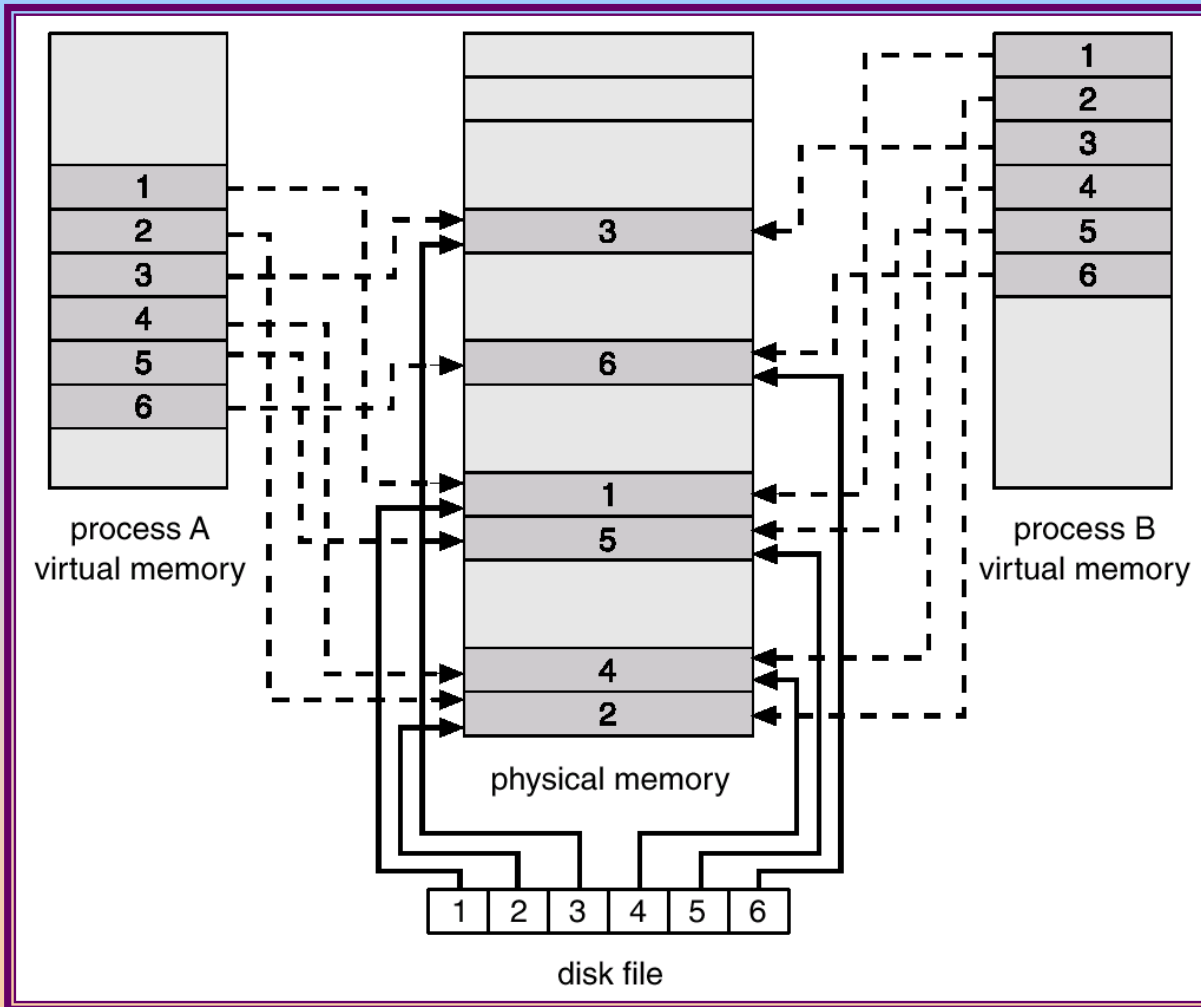


Memory-Mapped Files

- ❑ Memory-mapped file I/O allows file I/O to be treated as routine memory access by *mapping* a disk block to a page in memory.
- ❑ A file is initially read using demand paging. A page-sized portion of the file is read from the file system into a physical page. Subsequent reads/writes to/from the file are treated as ordinary memory accesses.
- ❑ Simplifies file access by treating file I/O through memory rather than **read()** **write()** system calls.
- ❑ Also allows several processes to map the same file allowing the pages in memory to be shared.



Memory Mapped Files



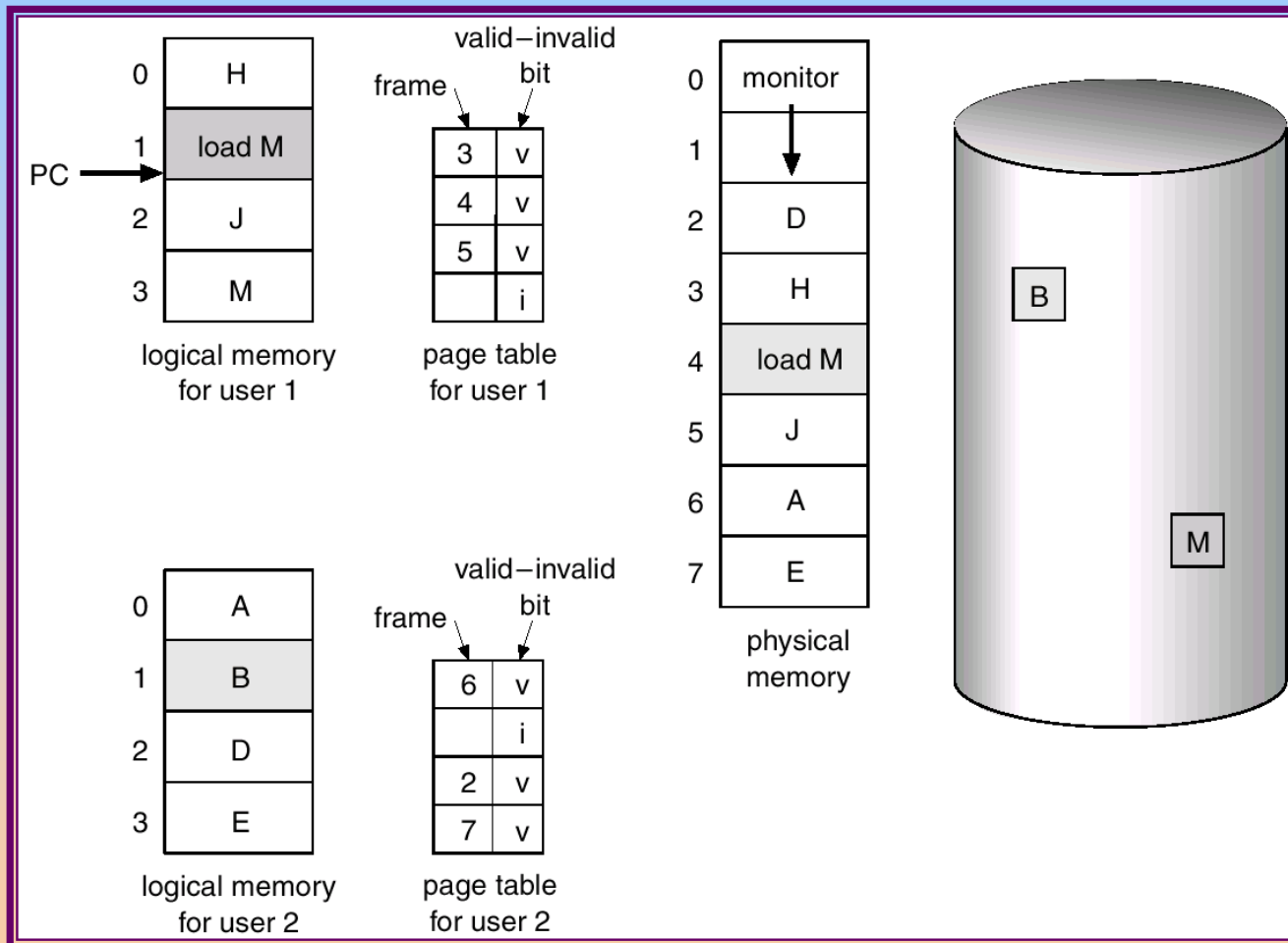


Page Replacement

- ❑ Prevent over-allocation of memory by modifying page-fault service routine to include page replacement.
- ❑ Use *modify (dirty) bit* to reduce overhead of page transfers – only modified pages are written to disk.
- ❑ Page replacement completes separation between logical memory and physical memory – large virtual memory can be provided on a smaller physical memory.



Need For Page Replacement



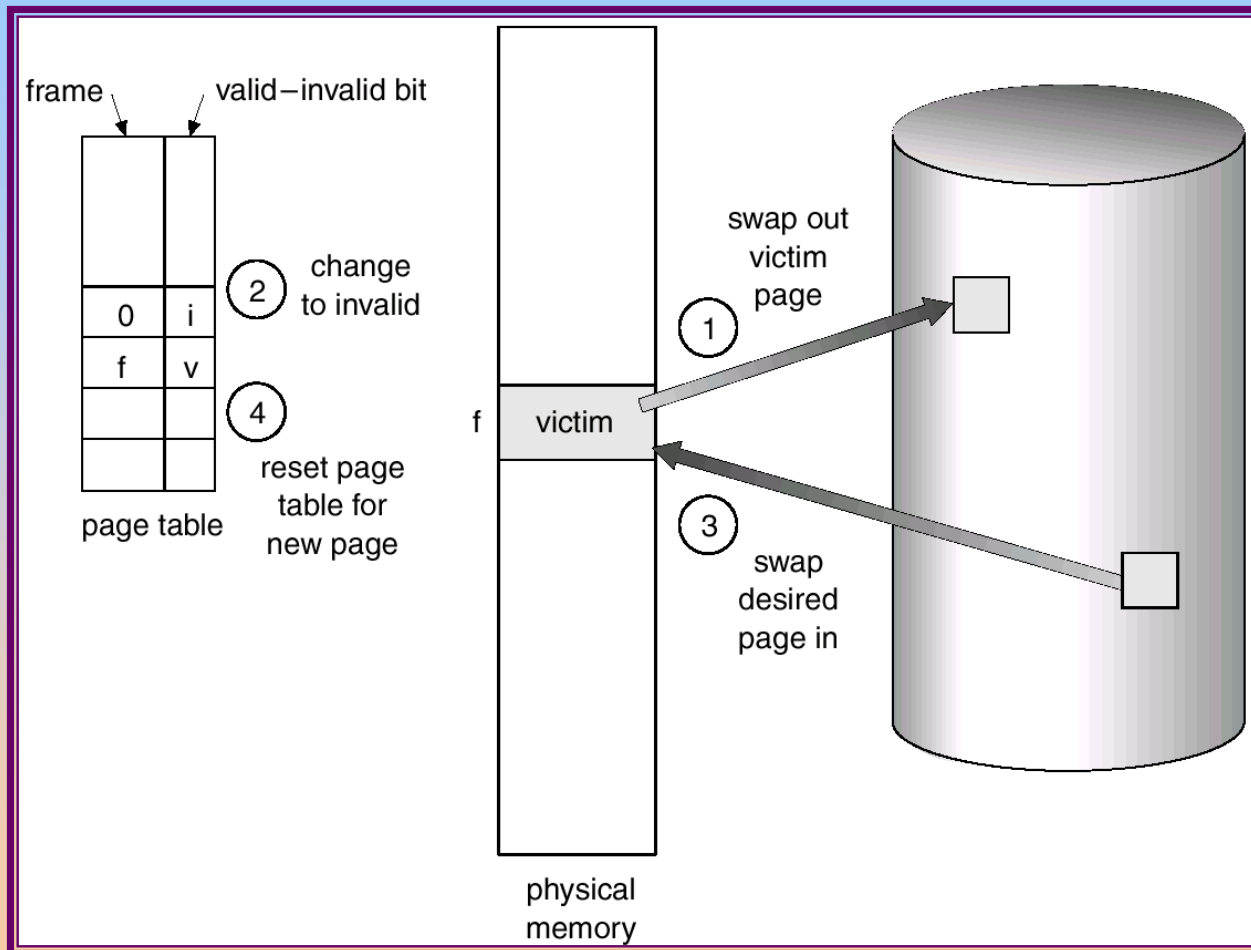


Basic Page Replacement

1. Find the location of the desired page on disk.
2. Find a free frame:
 - If there is a free frame, use it.
 - If there is no free frame, use a page replacement algorithm to select a *victim* frame.
3. Read the desired page into the (newly) free frame.
Update the page and frame tables.
4. Restart the process.



Page Replacement





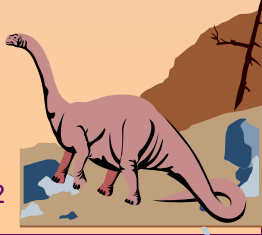
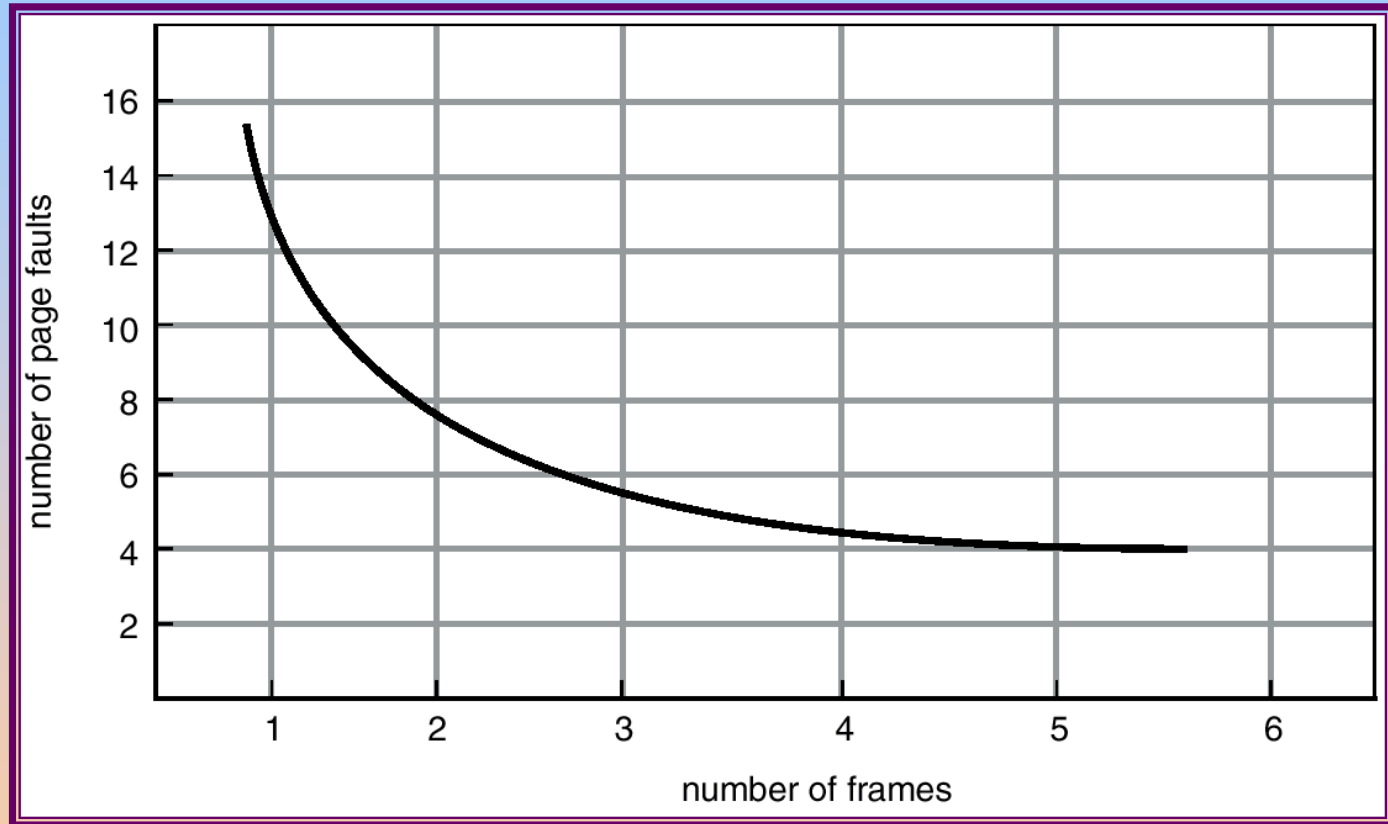
Page Replacement Algorithms

- Want lowest page-fault rate.
- Evaluate algorithm by running it on a particular string of memory references (reference string) and computing the number of page faults on that string.
- In all our examples, the reference string is
1, 2, 3, 4, 1, 2, 5, 1, 2, 3, 4, 5.





Graph of Page Faults Versus The Number of Frames





First-In-First-Out (FIFO) Algorithm

- Reference string: 1, 2, 3, 4, 1, 2, 5, 1, 2, 3, 4, 5
- 3 frames (3 pages can be in memory at a time per process)

1	1	4	5
2	2	1	3
3	3	2	4

9 page faults

- 4 frames

1	1	5	4
2	2	1	5
3	3	2	
4	4	3	

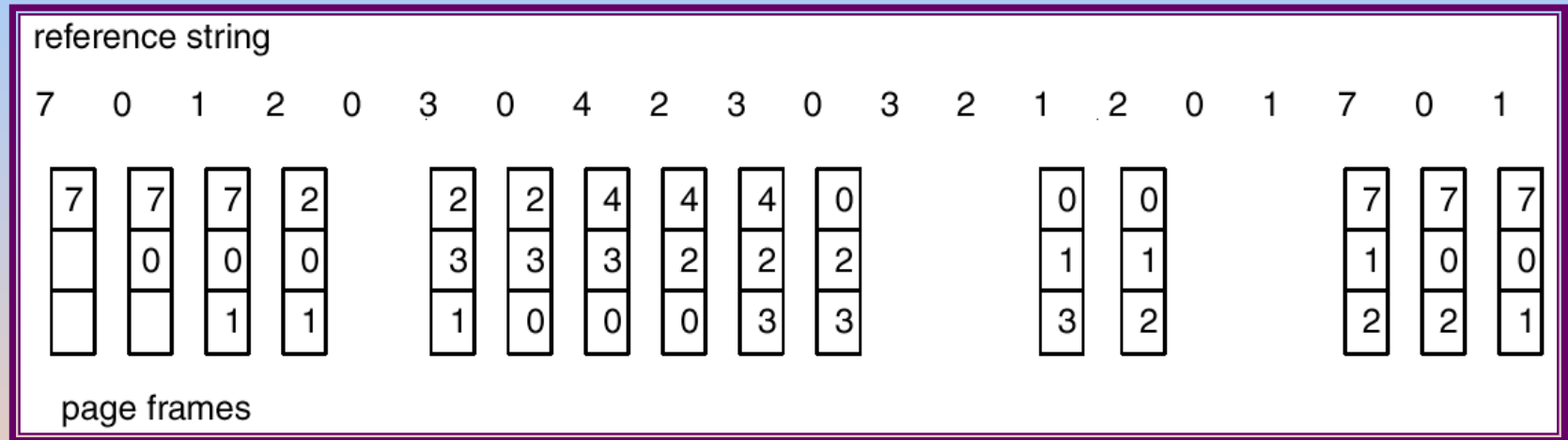
10 page faults

- FIFO Replacement – Belady’s Anomaly
 - more frames \Rightarrow less page faults



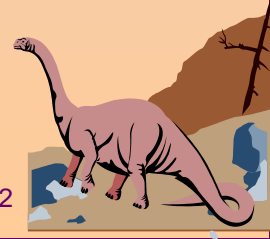


FIFO Page Replacement





FIFO Illustrating Belady's Anamoly





Optimal Algorithm

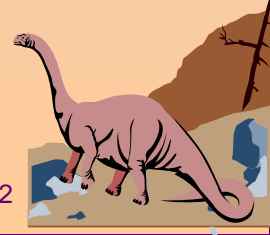
- ❑ Replace page that will not be used for longest period of time.
- ❑ 4 frames example

1, 2, 3, 4, 1, 2, 5, 1, 2, 3, 4, 5

1	4
2	
3	
4	5

6 page faults

- ❑ How do you know this?
- ❑ Used for measuring how well your algorithm performs.





Optimal Page Replacement

reference string

7 0 1 2 0 3 0 4 2 3 0 3 2 1 2 0 1 7 0 1

7	7	7	2		2		2		2		2						7		
	0	0	0		0		4		0		0						0		
		1	1		3		3		3		1						1		

page frames





Least Recently Used (LRU) Algorithm

- Reference string: 1, 2, 3, 4, 1, 2, 5, 1, 2, 3, 4, 5

1	5	
2		
3	5	4
4	3	

- Counter implementation
 - Every page entry has a counter; every time page is referenced through this entry, copy the clock into the counter.
 - When a page needs to be changed, look at the counters to determine which are to change.





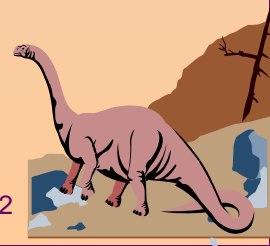
LRU Page Replacement

reference string

7 0 1 2 0 3 0 4 2 3 0 3 2 1 2 0 1 7 0 1

7	7	7	2		2		4	4	4	0			1		1		1		
	0	0	0		0		0	0	3	3			3		0		0		
		1	1		3		3	2	2	2			2		2		7		

page frames





LRU Algorithm (Cont.)

- Stack implementation – keep a stack of page numbers in a double link form:
 - Page referenced:
 - move it to the top
 - requires 6 pointers to be changed
 - No search for replacement





Use Of A Stack To Record The Most Recent Page References

reference string

4 7 0 7 1 0 1 2 1 2 7 1 2

↑
a

↑
b

2
1
0
7
4

stack before a

7
2
1
0
4

stack after b





LRU Approximation Algorithms

□ Reference bit

- With each page associate a bit, initially = 0
- When page is referenced bit set to 1.
- Replace the one which is 0 (if one exists). We do not know the order, however.

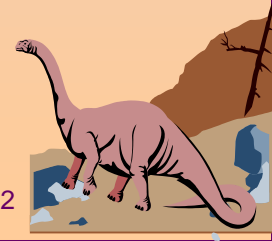
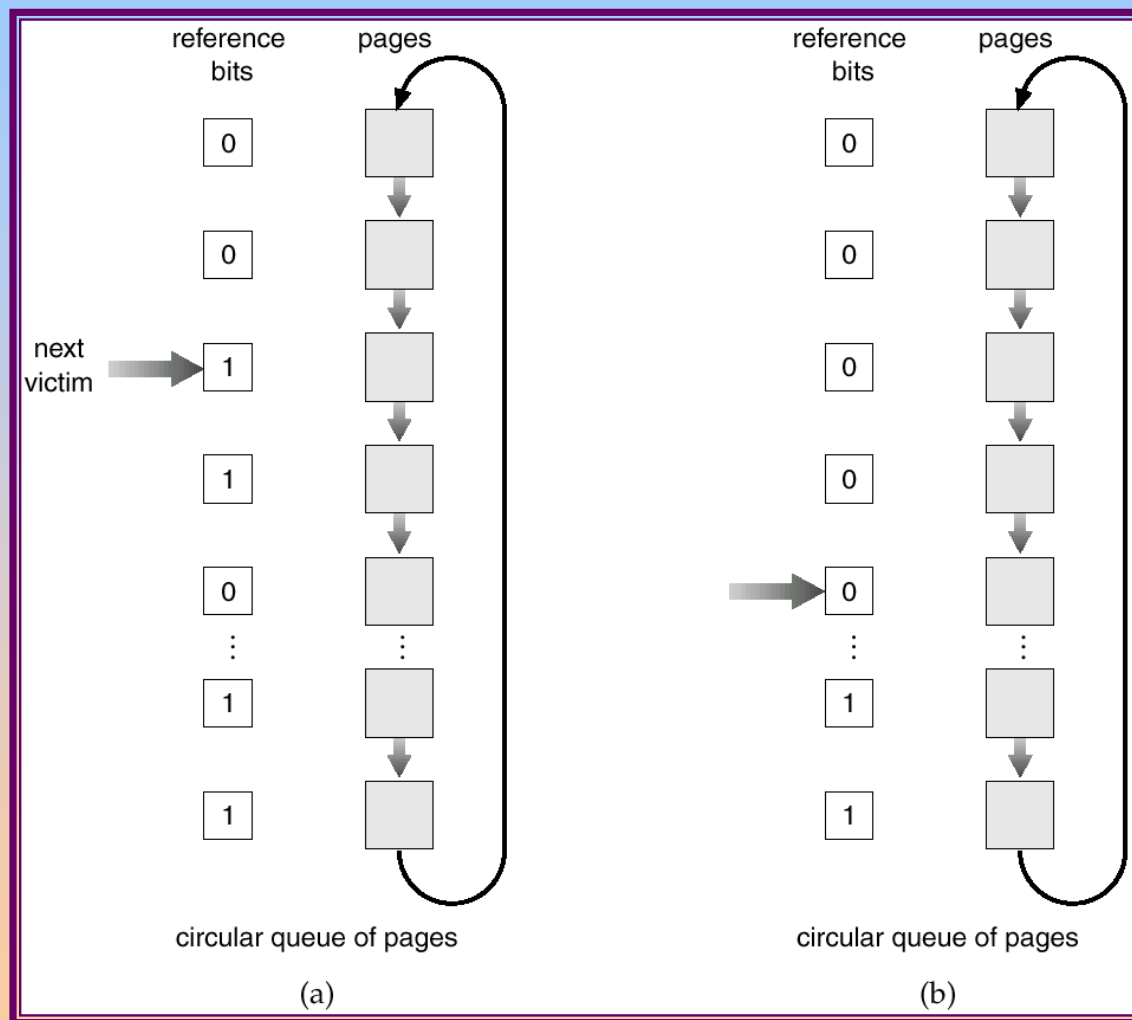
□ Second chance

- Need reference bit.
- Clock replacement.
- If page to be replaced (in clock order) has reference bit = 1. then:
 - set reference bit 0.
 - leave page in memory.
 - replace next page (in clock order), subject to same rules.





Second-Chance (clock) Page-Replacement Algorithm





Counting Algorithms

- ❑ Keep a counter of the number of references that have been made to each page.
- ❑ LFU Algorithm: replaces page with smallest count.
- ❑ MFU Algorithm: based on the argument that the page with the smallest count was probably just brought in and has yet to be used.





Allocation of Frames

- ❑ Each process needs **minimum** number of pages.
- ❑ Example: IBM 370 – 6 pages to handle SS MOVE instruction:
 - ❑ instruction is 6 bytes, might span 2 pages.
 - ❑ 2 pages to handle **from**.
 - ❑ 2 pages to handle **to**.
- ❑ Two major allocation schemes.
 - ❑ fixed allocation
 - ❑ priority allocation





Fixed Allocation

- Equal allocation – e.g., if 100 frames and 5 processes, give each 20 pages.
- Proportional allocation – Allocate according to the size of process.

– s_i = size of process p_i

– $S = \sum s_i$

– m = total number of frames

– a_i = allocation for $p_i = \frac{s_i}{S} \times m$

$$m = 64$$

$$s_1 = 10$$

$$s_2 = 127$$

$$a_1 = \frac{10}{137} \times 64 \approx 5$$

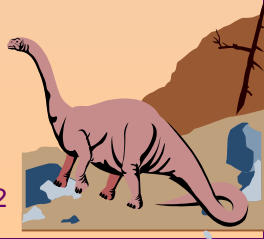
$$a_2 = \frac{127}{137} \times 64 \approx 59$$





Priority Allocation

- Use a proportional allocation scheme using priorities rather than size.
- If process P_i generates a page fault,
 - select for replacement one of its frames.
 - select for replacement a frame from a process with lower priority number.





Global vs. Local Allocation

- ❑ **Global** replacement – process selects a replacement frame from the set of all frames; one process can take a frame from another.
- ❑ **Local** replacement – each process selects from only its own set of allocated frames.





Thrashing

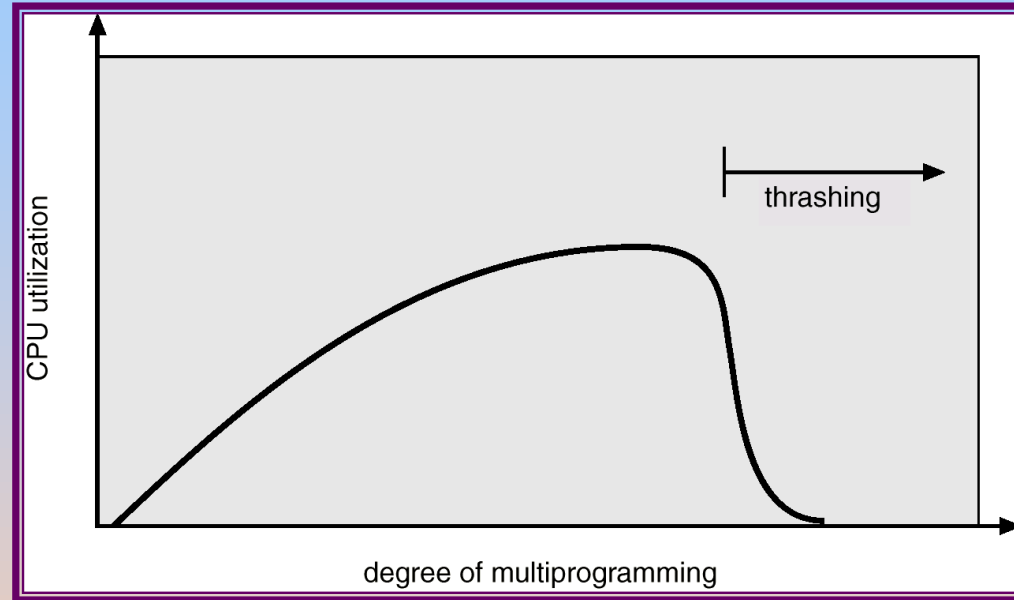
- If a process does not have “enough” pages, the page-fault rate is very high. This leads to:
 - low CPU utilization.
 - operating system thinks that it needs to increase the degree of multiprogramming.
 - another process added to the system.

- **Thrashing** \equiv a process is busy swapping pages in and out.

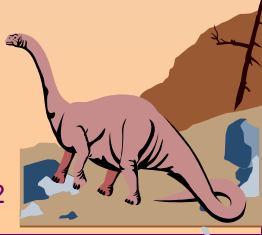




Thrashing

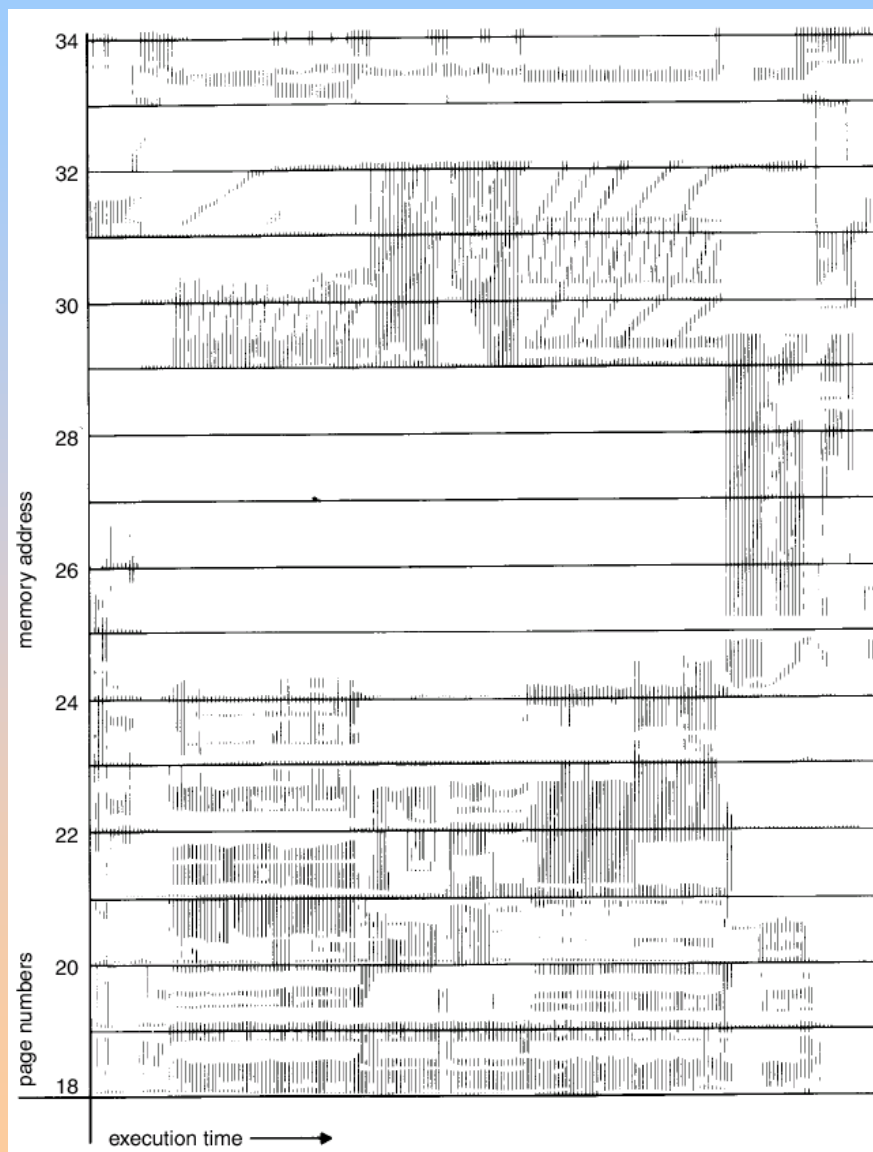


- ❑ Why does paging work?
Locality model
 - ❑ Process migrates from one locality to another.
 - ❑ Localities may overlap.
- ❑ Why does thrashing occur?
 Σ size of locality > total memory size





Locality In A Memory-Reference Pattern





Working-Set Model

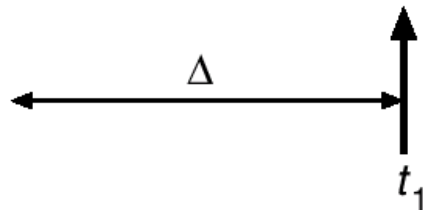
- $\Delta \equiv$ working-set window \equiv a fixed number of page references
Example: 10,000 instruction
- WSS_i (working set of Process P_i) =
total number of pages referenced in the most recent Δ
(varies in time)
 - if Δ too small will not encompass entire locality.
 - if Δ too large will encompass several localities.
 - if $\Delta = \infty \Rightarrow$ will encompass entire program.
- $D = \sum WSS_i \equiv$ total demand frames
- if $D > m \Rightarrow$ Thrashing
- Policy if $D > m$, then suspend one of the processes.



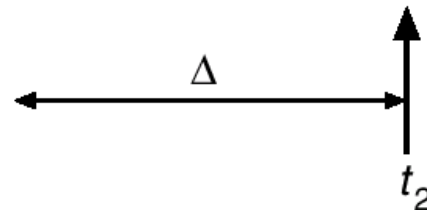
Working-set model

page reference table

... 2 6 1 5 7 7 7 7 5 1 6 2 3 4 1 2 3 4 4 4 3 4 3 4 4 4 1 3 2 3 4 4 4 3 4 4 4 ...



$$WS(t_1) = \{1, 2, 5, 6, 7\}$$



$$WS(t_2) = \{3, 4\}$$



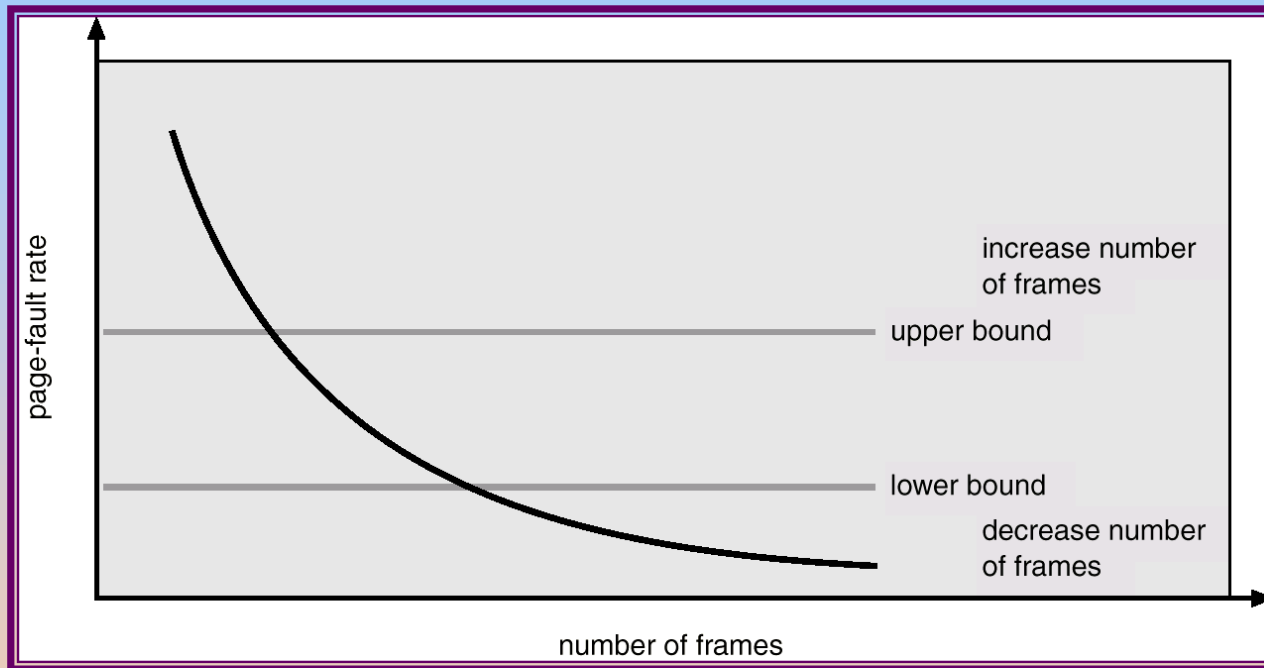
Keeping Track of the Working Set

- Approximate with interval timer + a reference bit
- Example: $\Delta = 10,000$
 - Timer interrupts after every 5000 time units.
 - Keep in memory 2 bits for each page.
 - Whenever a timer interrupts copy and sets the values of all reference bits to 0.
 - If one of the bits in memory = 1 \Rightarrow page in working set.
- Why is this not completely accurate?
- Improvement = 10 bits and interrupt every 1000 time units.





Page-Fault Frequency Scheme



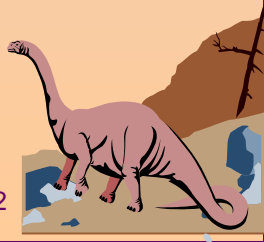
- Establish “acceptable” page-fault rate.
 - If actual rate too low, process loses frame.
 - If actual rate too high, process gains frame.





Other Considerations

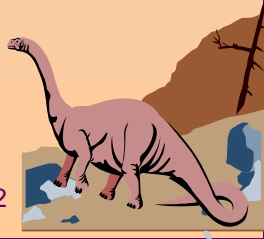
- Prepaging
- Page size selection
 - fragmentation
 - table size
 - I/O overhead
 - locality





Other Considerations (Cont.)

- ❑ **TLB Reach** - The amount of memory accessible from the TLB.
- ❑ $\text{TLB Reach} = (\text{TLB Size}) \times (\text{Page Size})$
- ❑ Ideally, the working set of each process is stored in the TLB. Otherwise there is a high degree of page faults.





Increasing the Size of the TLB

- ❑ **Increase the Page Size.** This may lead to an increase in fragmentation as not all applications require a large page size.
- ❑ **Provide Multiple Page Sizes.** This allows applications that require larger page sizes the opportunity to use them without an increase in fragmentation.





Other Considerations (Cont.)

□ Program structure

- `int A[][] = new int[1024][1024];`

- Each row is stored in one page

- Program 1

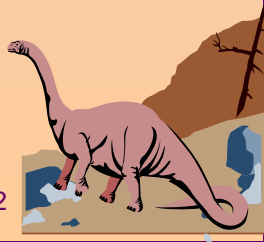
```
for (j = 0; j < A.length; j++)  
  for (i = 0; i < A.length; i++)  
    A[i,j] = 0;
```

1024 x 1024 page faults

- Program 2

```
for (i = 0; i < A.length; i++)  
  for (j = 0; j < A.length; j++)  
    A[i,j] = 0;
```

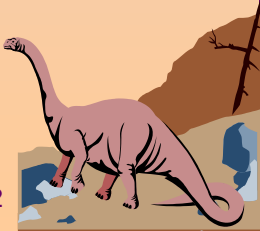
1024 page faults





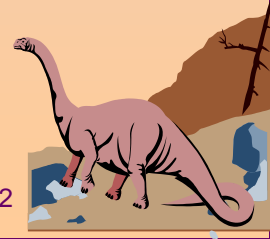
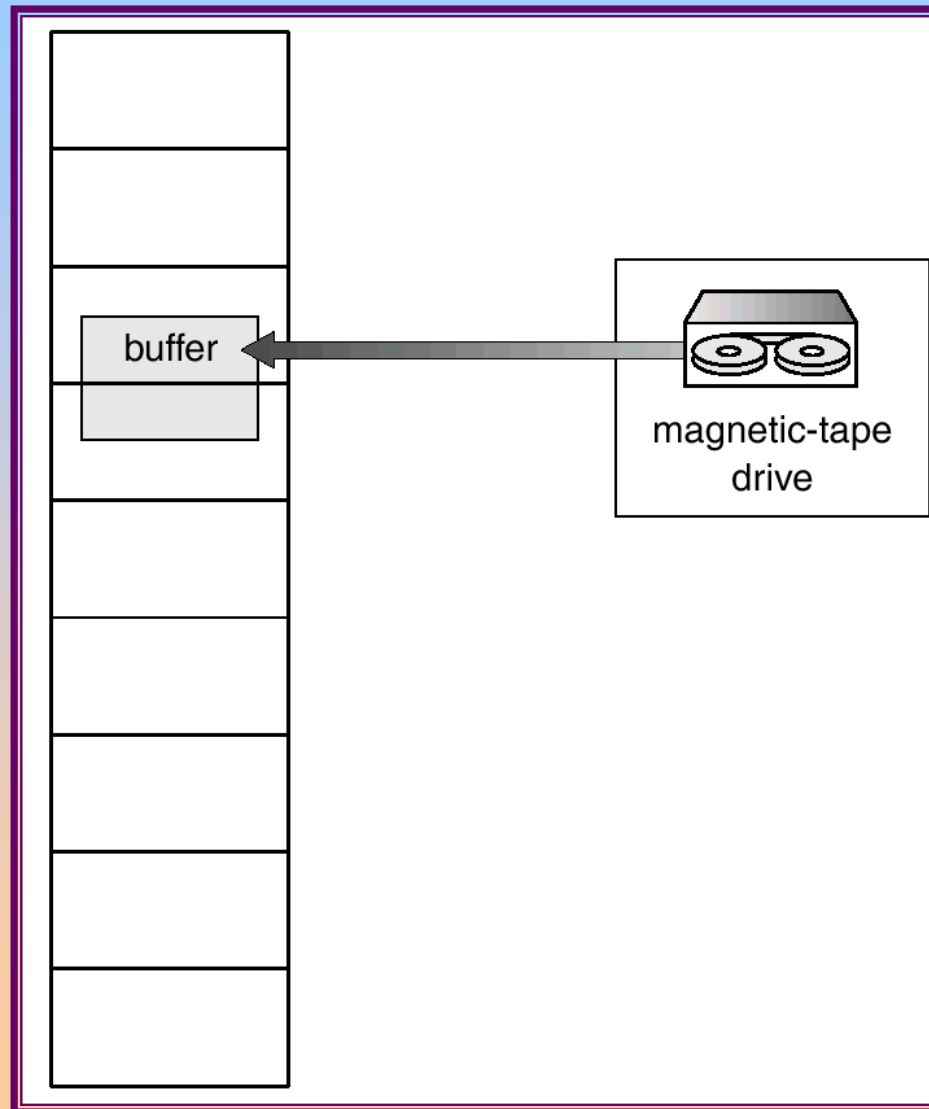
Other Considerations (Cont.)

- ❑ **I/O Interlock** – Pages must sometimes be locked into memory.
- ❑ Consider I/O. Pages that are used for copying a file from a device must be locked from being selected for eviction by a page replacement algorithm.





Reason Why Frames Used For I/O Must Be In Memory





Operating System Examples

□ Windows NT

□ Solaris 2





Windows NT

- ❑ Uses demand paging with **clustering**. Clustering brings in pages surrounding the faulting page.
- ❑ Processes are assigned **working set minimum** and **working set maximum**.
- ❑ Working set minimum is the minimum number of pages the process is guaranteed to have in memory.
- ❑ A process may be assigned as many pages up to its working set maximum.
- ❑ When the amount of free memory in the system falls below a threshold, **automatic working set trimming** is performed to restore the amount of free memory.
- ❑ Working set trimming removes pages from processes that have pages in excess of their working set minimum.





Solaris 2

- ❑ Maintains a list of free pages to assign faulting processes.
- ❑ **Lotsfree** – threshold parameter to begin paging.
- ❑ Paging is performed by *pageout* process.
- ❑ Pageout scans pages using modified clock algorithm.
- ❑ **Scanrate** is the rate at which pages are scanned. This ranged from **slowscan** to **fastscan**.
- ❑ Pageout is called more frequently depending upon the amount of free memory available.



Solar Page Scanner

