

Q3

value	frequency
0	3
1	3
2	3
3	1

$$\lambda = E(x) = \frac{0 \times 3 + 1 \times 3 + 2 \times 3 + 3 \times 1}{10}$$

$$= 1.2$$

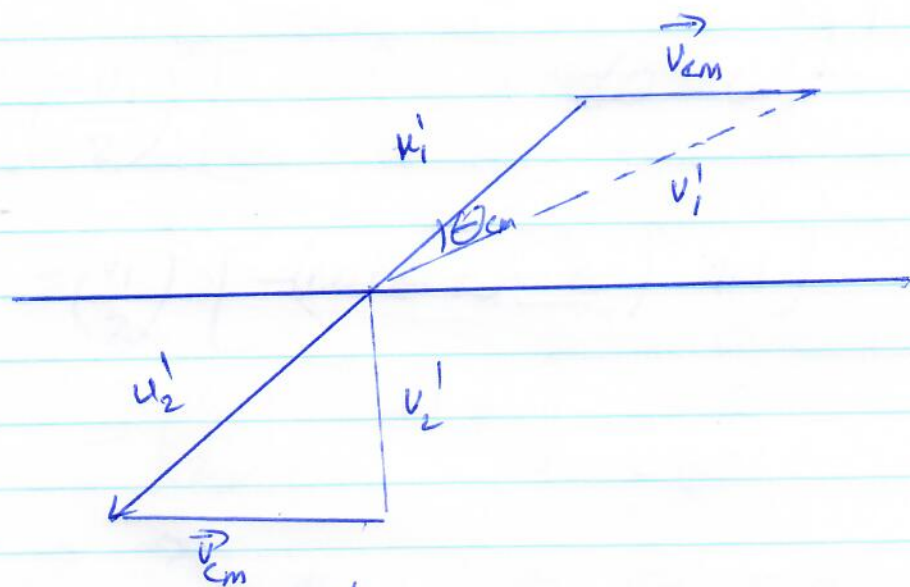
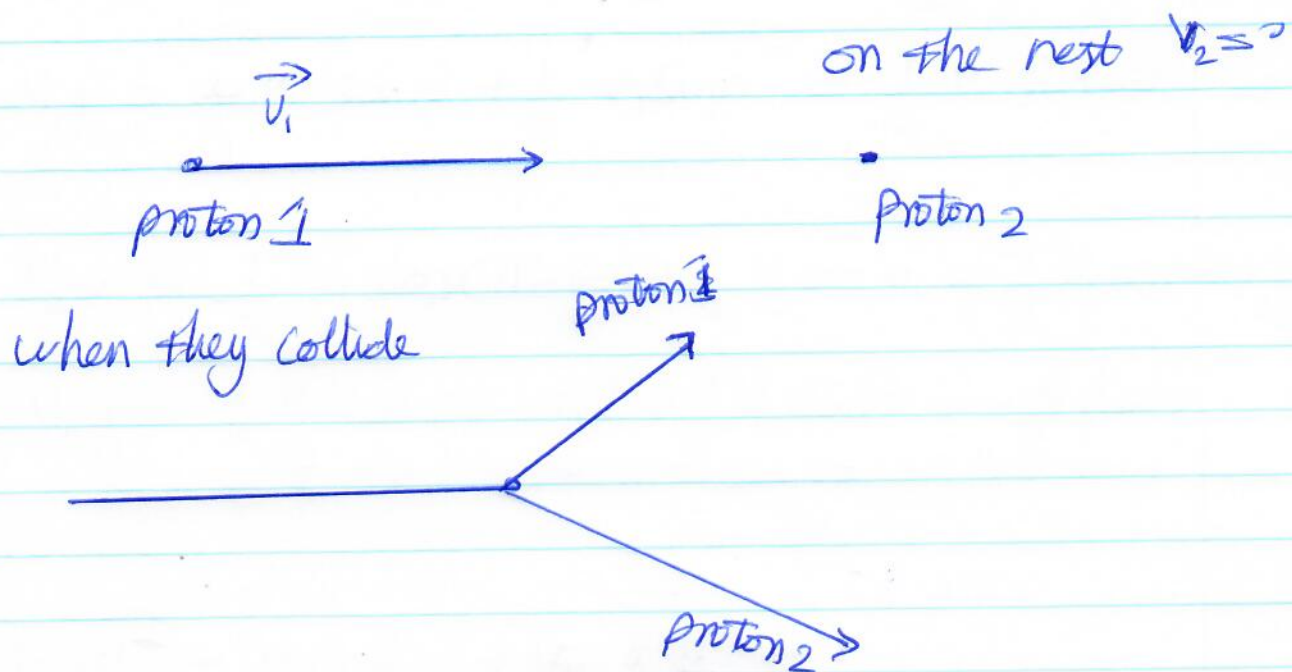
So the average counting rate is 1.2

→ probability the next counting is zero

$$P(X=0) = e^{-\lambda} \frac{\lambda^x}{x!} = e^{-1.2} \frac{(1.2)^0}{0!}$$

$$= 0.301$$

Q2



the protons ^{they} have the same masses $\Rightarrow m_1 = m_2$

$$v_{cm} = \frac{v_1 m_1 + v_2 m_2}{m_1 + m_2} = \frac{v_1 m_1}{2 m_1} = \frac{v_1}{2}$$

when need to prove that $\vec{v}_1 \cdot \vec{v}_2 = 0$

$$\vec{v}_1 \cdot \vec{v}_2 = v_{1x} v_{2x} + v_{1y} v_{2y}$$

$$V_{1x} = \frac{1}{2} V_1 \cos \theta + \frac{1}{2} V_1 \cos 0 = \frac{1}{2} V_1 \cos \theta + \frac{1}{2} V_1$$

$$V_{1y} = \frac{1}{2} V_1 \sin \theta + \frac{1}{2} V_1 \sin 0 = \frac{1}{2} V_1 \sin \theta$$

$$V_{2x} = \frac{1}{2} V_1 \cos(\pi - \theta) + \frac{1}{2} V_2 \cos 0 = -\frac{1}{2} V_1 \cos \theta + \frac{1}{2} V_1$$

$$V_{2y} = \frac{1}{2} V_1 \sin(\pi - \theta) + \frac{1}{2} V_1 \sin 0 = -\frac{1}{2} V_1 \sin \theta$$

So $\vec{V}_1 \cdot \vec{V}_2 = V_{1x} V_{2x} + V_{1y} V_{2y} =$

$$\left(\frac{V_1}{2}\right)^2 \left[-\cos^2 \theta + \cancel{\cos \theta} - \cancel{\cos \theta} + \sin^2 \theta \right]$$

$$= \left(\frac{V_1}{2}\right)^2 \left[-(\cos^2 \theta + \sin^2 \theta) + 1 \right]$$

$$= \left(\frac{V_1}{2}\right)^2 \left[-1 + 1 \right] = 0$$

$$\vec{V}_1 \cdot \vec{V}_2 = 0 \quad \Rightarrow \quad \theta = \frac{\pi}{2}$$