

DPP: 2

Subject: Mathematics **Topic:** Inequalities

1.
$$\frac{x-1}{x} - \frac{x+1}{x-1} < 2$$
.

3.
$$\frac{1}{x-2} + \frac{1}{x-1} > \frac{1}{x}$$

5.
$$\frac{2(x-4)}{(x-1)(x-7)} \le \frac{1}{x-2}$$
.

7.
$$\frac{7}{(x-2)(x-3)} + \frac{9}{x-3} + 1 < 0$$

9.
$$\frac{1}{x+1} - \frac{2}{x^2 - x + 1} < \frac{1-2x}{x^3 + 1}$$
.

11.
$$x^4 - 5x^2 + 4 < 0$$

13.
$$\frac{(x-2)(x-4)(x-7)}{(x+2)(x+4)(x+3)} > 1$$

15.
$$\frac{x^2-36}{x^2-9x+18} < 0$$
.

17.
$$(x+1)(x-3)^2(x-5)(x-4)^2(x-2) < 0$$
.

19.
$$(x+3)^{553}(3x-2)^{5555}(7-x)^{343}(5x+8)^{10^{10}}$$

21.
$$\frac{(x+8)^{3351}(1-x)^{3^{8^5}}}{(x+5)^{103}(x-2)^{4^{4^4}}} \ge 0$$

23.
$$\frac{x^2 + 4x + 4}{2x^2 - x - 1} > 0$$
. **NEET** 24. $\frac{x^2 + 8x + 7}{4x^2 - 4x + 1} < 0$. undation

25.
$$\frac{x^2 - 6x + 9}{5 - 4x - x^2} \ge 0.$$

27.
$$\frac{(x+2)(x^2-2x+1)}{4+3x-x^2} \ge 0$$
.

29.
$$1 + \frac{12}{x^2} < \frac{7}{x}$$

2.
$$\frac{2(x-3)}{x(x-6)} \le \frac{1}{x-1}$$
.

4.
$$\frac{2x}{x^2-9} \le \frac{1}{x+2}$$
.

6.
$$\frac{1}{x-2} + \frac{1}{x-1} \ge \frac{1}{x}$$

8.
$$\frac{20}{(x-3)(x-4)} + \frac{10}{x-4} + 1 > 0.$$

10.
$$\frac{x+4}{x^2-9} - \frac{2}{x+3} < \frac{4x}{3x+x^2}$$
.

12.
$$x^4 - 2x^2 - 63 \le 0$$
.

14.
$$\frac{(x-1)(x-2)(x-3)}{(x+1)(x+2)(x+3)} > 1$$

16.
$$(x-1)(3-x)(x-2)^2 > 0$$
.

18.
$$(x-1)^2 (x+1)^3 (x-4) < 0$$
.

19.
$$(x+3)^{553}(3x-2)^{5555}(7-x)^{343}(5x+8)^{10^{10}} < 0$$
 20. $\frac{(x-1)^2(x+1)^3}{x^4(x-2)} \le 0$.

22.
$$\frac{(x-1)(x+2)^2}{-1-x} < 0.$$

24.
$$\frac{x^2-8x+7}{4x^2-4x+1} < 0$$
 undation

26.
$$\frac{x^4 - 3x^3 + 2x^2}{x^2 - x - 30} > 0.$$

28.
$$\frac{(2-x^2)(x-3)^3}{(x+1)(x^2-3x-4)} \ge 0.$$

30.
$$\frac{x+1}{(x-1)^2} < 1$$
.

31.
$$\frac{(x+7)^{N^{4^5}}(x-5)^3}{(x+11)^{7853}(x+4)(3-x)(x-6)^{N+1982}} \ge 0$$
, where N is odd number

- 32. $\frac{x^{10^{10}}(x+2)^{N!}(x+1)^{N!^{N!}}}{(x+6)^{3}(x-3)^{451}(x+3)^{N!-1}(2-x)} \ge 0, \text{ where N is natural number } \ge 2.$
- 33. $\frac{x^{t}(x-1)^{T+3^{9^{7}}}}{(x+7)^{T}(10-x)^{1999+t1}} \le 0$, where t, T are primes satisfying, $T^{2}-2t^{2}=1$.
- 34. $\frac{(x+8)^{U\{1!+2!+3!+...+1997\}}(x+4)(8-x)^{5555^{333^{779}}}}{(x-4)^5(x+5)^2} \le 0, \text{ where } u\{n\} \text{ denotes unit digit of } n.$
- 35. $\frac{(x+2)^{44^{55}}(-3-x)^{58}}{(1+x)^{333^{444}}(2x-4)(x-3)^{T}} \le 0$ where T satisfies the relation (3!) (5!) (7!) = T!...

Answer kev

1.
$$(-\infty, -1) \cup (0, 1/2) \cup (1, +\infty)$$
 2. $(-\infty, 0) \cup (1, 6)$

2.
$$(-\infty,0) \cup (1,6)$$

3.
$$(-\sqrt{2},0) \cup (1,\sqrt{2}) \cup (2,+\infty)$$

4.
$$(-\infty, -3) \cup (-2, 3)$$

5.
$$(-\infty, -1)U(2,7)$$

6.
$$x \in [-\sqrt{2}, 0] \cup [1, \sqrt{2}] \cup [2, \infty]$$

7.
$$x \in (-5, 1) \cup (2, 3)$$

8.
$$(-\infty, -2) \cup (-1, 3) \cup (4, +\infty)$$

9.
$$(-\infty, 2) - \{1\}$$

10.
$$(-3,0)U(0,3)U\left(\frac{22}{5},\infty\right)$$
 11. $(-2,-1)\cup(1,2)$.

13.
$$(-\infty, -7) \cup (-4, -2)$$

14.
$$(-\infty, -3) \cup (-2, -1)$$

16.
$$(1,2) \cup (2,3)$$

17.
$$(-\infty, -1)U(2,5) - \{3,4\}$$

19.
$$x \in (-3, -8/5) \cup (-8/5, 2/3) \cup (7, \infty)$$

20.
$$[-1,0) \cup (0,2)$$
.

21.
$$x \in \{-\infty\} \cup (-5, 1]$$

22.
$$(-\infty, -2) \cup (-2, -1) \cup (1, +\infty)$$
 23. $(-\infty, -2) \cup (-2, -1/2) \cup (1, +\infty)$

23.
$$(-\infty, -2) \cup (-2, -1/2) \cup (1, +1/2) \cup (1, +1/2)$$

25.
$$(-5,1) \cup \{3\}$$

26.
$$(-\infty, -5) \cup 1, 2) \cup (6, +\infty)$$

27.
$$(-\infty, -2) \cup (-1, 4)$$

28.
$$[-\sqrt{2},-1)U(-1,\sqrt{2})U[3,4)$$
 29. (3,4)

30.
$$(-\infty, 0) \cup (3, +\infty)$$

31.
$$x \in (-1, -7] \cup (-4, 3) \cup [5, 6)$$
 32. $(-6, -3)U(2, 3)U\{-2, -1, 0\}$

32.
$$(-6,-3)U(2,3)U\{-2,-1,0\}$$

33.
$$x \in (-\infty, -7) \cup \{0, 1\} \cup (10, \infty)$$
 34. $x \in (-\infty, 8) \cup [-4, 4) \cup [8, \infty)$ **35.** $x \in (-1, 2)$

34.
$$x \in (-\infty, 8) \cup [-4, 4) \cup [8, \infty)$$

35.
$$x \in (-1, 2)$$

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Answer key (DPP 1)

2.
$$(-2/3,3)$$

1.
$$[1,4/3/]$$
. **2.** $(-2/3,3)$ **3.** $(-\infty,-1) \cup (15,+\infty)$. **4.** $[-2,1]$

5.
$$(-\infty, -3)U(2,3)$$
 6. $(-1/4, 5/6)$ **7.** $(-\infty, 3/2) \cup (7/3, +\infty)$

6.
$$(-1/4, 5/6)$$

7.
$$(-\infty; 3/2) \cup (7/3, +\infty)$$

8.
$$\phi$$

9.
$$(-\infty, +\infty)$$
 10. $(2,3)$

11.
$$(-3,1)$$

12.
$$x \in (-\infty, -1) \cup (5, \infty)$$

13.
$$(-\infty,3) \cup (4,+\infty)$$
 14. $(5/2,8)$

15.
$$(-\infty, -1) \cup (5, +\infty)$$

15.
$$(-\infty, -1) \cup (5, +\infty)$$
 16. $(-\infty, -1) \cup (1/3, +\infty)$

17.
$$(-1/2,2)$$

18.
$$(-1,0) \cup (4,+\infty)$$

17.
$$(-1/2,2)$$
 18. $(-1,0) \cup (4,+\infty)$ **19.** $(-5,-2) \cup (-2/3,+\infty)$

20.
$$\left(-\infty, \left(2-\sqrt{22}\right)/3\right) \cup \left(\left(2+\sqrt{22}\right)/3, 5/2\right)$$

21.
$$(-17/2, -3) \cup (1, +\infty)$$

22.
$$(-\infty, -3) \cup (3, +\infty)$$

22.
$$(-\infty, -3) \cup (3, +\infty)$$
 23. $(-\infty, -6)U[-2, 0)U[3, \infty)$

24. (2,3)
$$\cup$$
 (5,6)

24.
$$(2,3) \cup (5,6)$$
 25. $(-\infty,-3) \cup (-2,+\infty)$ **26.** $(-\infty,-3) \cup [1,4)$

27.
$$(-\infty + \infty)$$
 28. ϕ

29.
$$x \in (-3, 1)$$

30.
$$[1,3] \cup (5,+\infty)$$

29.
$$x \in (-3, 1)$$
 30. $[1,3] \cup (5,+\infty)$ **31.** $(-\infty,-1/\sqrt[3]{2}) \cup (0,+\infty)$ **32.** $(-1,1) \cup (4,6)$

32.
$$(-1,1) \cup (4,6)$$

33.
$$(-\infty, -7)U(-5, 3)$$
 34. $(-2, -1] \cup (0, 2]$. **35.** $(0, 3)$

36.
$$(-1, +\infty)$$

37.
$$(-9/2,-2) \cup (3,+\infty)$$
 38. $(-\infty,5/2) \cup (33/8,+\infty)$.

40.
$$\left(-\infty, \frac{16}{7}\right) U(4, \infty)$$
 41. $\left(-7, -3\right)$. **42.** $\left(-17/25, -3/8\right)$

43.
$$(-\infty, -5) \cup (5, +\infty)$$

44.
$$(-\infty,2) \cup (5,+\infty)$$
 45. $(-\infty,2) \cup (5,+\infty)$

44.
$$(-\infty,2) \cup (5,+\infty)$$
 45. $(-\infty,1)U[\frac{3}{2},\infty)$ **46.** $(-\infty,0) \cup (1,+\infty)$. **47.** $(-\infty,-5/2) \cup (-2,8)$

47.
$$(-\infty, -5/2) \cup (-2, 8)$$

48.
$$(3/4,1) \cup (7,+\infty)$$
 49. $(-1,0) \cup (0,1)$.

51.
$$(-\infty, -4) \cup (-3, 3) \cup (6, +\infty)$$

52.
$$(-\infty, -\sqrt{7}) \cup (-2, \sqrt{7}) \cup [8/3, +\infty)$$

52.
$$(-\infty, -\sqrt{7}) \cup (-2, \sqrt{7}) \cup [8/3, +\infty)$$
 53. $(-\infty, -\frac{\sqrt{63}}{2}) \cup (-3, \frac{\sqrt{63}}{2}) \cup (4, +\infty)$ **54.** $[1,2) \cup (3,4]$

55.
$$\left(-\infty, -\sqrt{7}/2\right) \cup \left(-1, \sqrt{7}/2\right) \cup \left(4/3, +\infty\right)$$
 56. $\left(-\left(11+\sqrt{737}\right)/28, 4/7\right) \cup \left(\left(\sqrt{737}-11\right)/28, 1\right)$

59.
$$(-2, +\infty)$$
 60. $(-\infty, +\infty)$ **61.** $(-\infty, -20) \cup (23, +\infty)$

57.
$$(-\infty, 1) \cup (4, +\infty)$$
 58. \emptyset 59. $(-2, +\infty)$ 60. $(-\infty, +\infty)$ 61. $(-\infty, -2)$ 62. $(-(1+\sqrt{21})/2, (\sqrt{21}-1)/2)$ 63. $(1/2, 3)$ 64. $(-\infty, -1) \cup (4, +\infty)$

57. $(-\infty, 1) \cup (4, +\infty)$ **58.** ϕ

64.
$$(-\infty, -1)(\sqrt{4}, +\infty)$$

65.
$$(-\infty, -\sqrt{10}) \cup (-1/2, 2/5) \cup (\sqrt{10}, +\infty)$$
 66. $(-\infty, -1) \cup (1, +\infty)$ **67.** $(-\infty, 0) \cup (1, \infty)$

66.
$$(-\infty,-1) \cup (1,+\infty)$$
 67. $(-\infty,0) U(1,\infty)$

68.
$$(-\infty,0) \cup (1,2) \cup (3,+\infty)$$

69.
$$(-2,-1) \cup (2,+\infty)$$

68.
$$(-\infty,0) \cup (1,2) \cup (3,+\infty)$$
 69. $(-2,-1) \cup (2,+\infty)$ **70.** $(-\infty,-1]U(5,6]$ **71.** $[-3,0) \cup [20,+\infty)$

72.
$$(-\infty, -1.4] \cup (2, 2.6]$$

73.
$$(-\infty,-1) \cup (1,3)$$

72.
$$(-\infty, -1.4] \cup (2, 2.6]$$
 73. $(-\infty, -1) \cup (1, 3)$ 74. $(-2, (3 - \sqrt{17})/2] \cup (0, 2) \cup [(3 + \sqrt{17})/2, +\infty)$