

Twin Permutations - Hackerearth

Sunday, February 23, 2020 9:23 AM

Also known as "Ambiguous Permutations"

The Problem:

Define a permutation of length N as a sequence of N numbers, consisting of all the numbers from 1 to N in any order.

An inverse permutation of a permutation (let say P) is a sequence of numbers in which the i^{th} number is the position of number i in the original permutation (*permutation P*), $1 \leq i \leq N$.

For example -

For a permutation $2\ 5\ 1\ 4\ 3$, inverse permutation is $3\ 1\ 5\ 4\ 2$.

Given a number N , find the number of *distinct permutations* of length N which can not be distinguished from their inverse permutation.

PS : Large I/O.

Input:

First line consists of a single integer T , the number of test cases.

Next T lines consist of a single integer each, representing value of N for that test case.

Constraints:

$$1 \leq T \leq 10^6$$

$$1 \leq N \leq 10^6$$

Output:

For each testcase, output the desired answer *modulo* 10^9+7 in a separate line.

Sample Input:

1
3

Sample Output:

4

Explanation

There are 6 permutations of length 3. They are written along with their inverse permutation below.

Permutation	Inverse Permutation
1 2 3	1 2 3
1 3 2	1 3 2
2 1 3	2 1 3
2 3 1	3 1 2
3 1 2	2 3 1
3 2 1	3 2 1

Clearly, there are 4 such permutations that can not be distinguished from their inverse permutation.

The Code:

```
#include <stdio.h>
#define MOD 1000000007
#define M 1000000

int main(){
    int caseCount, N;
    long int permutations[M];
    scanf("%d", &caseCount);

    permutations[0] = 1;
    permutations[1] = 2;
    for(int i=2; i<=M; i++){
        permutations[i] = ( permutations[i-1] + permutations[i-2] * 1LL * (i) ) % MOD;
    }

    while(caseCount > 0){
        scanf("%d", &N);
        printf("%ld\n", permutations[N-1]);
        caseCount--;
    }
}
```

The Stats:

Score
30.0

Time (sec)
0.30824

Memory (KiB)
8008

Language
C