Gaussian Mixture Model

Distribution

$$p(s|x) = \sum_{k=1}^{K} \pi(a^k|x) \prod_{t=1}^{T} \phi(s_t|a^k,x)$$

$$y = [s_1, s_2, ..., s_T]$$

$$p(\mathbf{s}|\mathbf{x}) = \sum_{k=1}^{K} \pi(\mathbf{a}^{k}|\mathbf{x})\phi(\mathbf{s}|\mathbf{a}^{k},\mathbf{x})$$

Negative Log-Likelihood

Loss

Data:
$$\{(\mathbf{x}^m, \hat{\mathbf{s}}^m)\}_{m=1}^M$$
 $\hat{\mathbf{s}}^m = [s_1^m, s_2^m, ..., s_T^m]$

$$l(\theta) = -\sum_{m=1}^{M} \sum_{k=1}^{K} \mathbf{1}(k = \hat{k}^m) \left[\log \pi(\mathbf{a}^k | \mathbf{x}^m; \theta) + \sum_{t=1}^{T} \log \mathcal{N}(\mathbf{s}_t^m | \mathbf{a}_t^k + \mu_t^k, \Sigma_t^k; \mathbf{x}^m; \theta) \right]$$

$$\boldsymbol{\mu^k} = [\mu_1^k, \mu_2^k, ..., \mu_T^k]$$
$$\boldsymbol{\Sigma^k} = [\Sigma_1^k, \Sigma_2^k, ..., \Sigma_T^k]$$

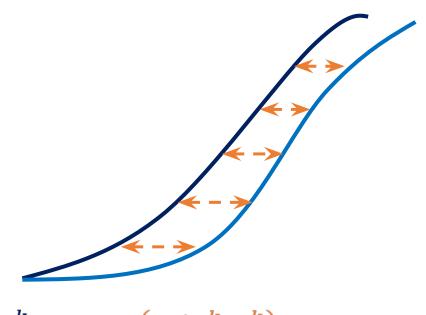
Data:
$$\{(\mathbf{x}^m, \mathbf{y}^m)\}_{m=1}^M$$
 $\mathbf{y}^m = [y_1^m, y_2^m, ..., y_T^m]$

$$l(\theta) = -\sum_{m=1}^{M} \sum_{k=1}^{K} \mathbf{1}(k = \hat{k}^m) \left[\log \pi(\mathbf{a}^k | \mathbf{x}^m; \theta) + \log \mathcal{N}(\mathbf{y}^m | \mathbf{a}^k + \boldsymbol{\mu}^k, \boldsymbol{\Sigma}^k; \mathbf{x}^m; \theta) \right]$$

Data:
$$\{(x^m, y^m)\}_{m=1}^M$$

$$p(y|x) = \sum_{k=1}^{K} \pi(a^k|x)\phi(y|a^k,x)$$

$$l(\theta) = -\sum_{m=1}^{M} \sum_{k=1}^{K} \mathbf{1}(k = \hat{k}^m) \left[\log \pi(\mathbf{a}^k | \mathbf{x}; \theta) + \log \mathcal{N}(\mathbf{y}^m | \mathbf{a}^k + \boldsymbol{\mu}^k, \boldsymbol{\Sigma}^k; \mathbf{x}^m; \theta) \right]$$



$$a^k + \mathcal{N}(\Delta s | \mu^k, \Sigma^k) = y$$

