

# NAT LIST

2420010, RHE, Suyong

1-a. hd (0 | 1 | nil)



$x = 0 \quad L = (1 | nil)$

$\rightarrow hd((0 | (1 | nil))) \text{ by } (X | L)$   
 $= 0 \text{ by } (hd 2)$

$eq \quad hd (n : l) = errNat, \dots hd 1$   
 $eq \quad hd (X | L) = X, \dots hd 2$   
 $eq \quad tl (n : l) = nil, \dots tl 1$   
 $eq \quad tl (X | L) = L, \dots tl 2$   
 $eq \quad [X .. Y] = \text{if } x > y \text{ then } \{ nil \} \text{ else } \{ x | [x+1 .. Y] \} \dots nils$   
 $eq \quad \text{if true then } \{ L \} \text{ else } \{ L2 \} = L, \dots \text{if } 1$   
 $eq \quad \text{if false then } \{ L \} \text{ else } \{ L2 \} = L2, \dots \text{if } 2$

1-b. tl (0 | 1 | nil)



$x = 0 \quad L = (1 | nil)$

$\rightarrow tl((0 | (1 | nil))) \text{ by } (X | L)$   
 $= (1 | nil) \text{ by } (tl 2)$

$\rightarrow (2 | (3 | (4 | (5 | (\text{if } (6 > 5) \text{ then } \{ nil \} \text{ else } \{ 6 | [6+1 .. 5] \} \} \} \} \} \dots \text{by } (ls)$

$\rightarrow (2 | (3 | (4 | (5 | (\text{if true then } \{ \} \text{ else } \{ \} \} \} \} \dots \text{by } (>))$

$\rightarrow (2 | (3 | (4 | (5 | nil)))) \dots \text{by } (if 1)$

$= (2 | 3 | 4 | 5 | nil)$

1-c. [2 .. 5]

$\rightarrow (\text{if } (2 > 5) \text{ then } \{ nil \} \text{ else } \{ 2 | [2+1 .. 5] \}) \dots \text{by } (ls)$   
 $\rightarrow (\text{if false then } \{ \} \text{ else } \{ \} \dots \text{by } (>))$   
 $\rightarrow (2 | [2+1 .. 5]) \dots \text{by } (if 2) \rightarrow (2 | [3 .. 5]) \dots \text{by } (+)$   
 $\rightarrow (2 | (\text{if } (3 > 5) \text{ then } \{ nil \} \text{ else } \{ 3 | [3+1 .. 5] \})) \dots \text{by } (ls)$   
 $\rightarrow (2 | (\text{if false then } \{ \} \text{ else } \{ \} \dots \text{by } (>))$   
 $\rightarrow (2 | (3 | [3+1 .. 5])) \dots \text{by } (if 2) \rightarrow (2 | (3 | [4 .. 5])) \dots \text{by } (+)$   
 $\rightarrow (2 | (3 | (\text{if } (4 > 5) \text{ then } \{ nil \} \text{ else } \{ 4 | [4+1 .. 5] \}))) \dots \text{by } (ls)$   
 $\rightarrow (2 | (3 | (\text{if false then } \{ \} \text{ else } \{ \} \dots \text{by } (>))$   
 $\rightarrow (2 | (3 | (4 | [4+1 .. 5]))) \dots \text{by } (if 2) \rightarrow (2 | (3 | (4 | [5 .. 5]))) \dots \text{by } (+)$   
 $\rightarrow (2 | (3 | (4 | (\text{if } (5 > 5) \text{ then } \{ nil \} \text{ else } \{ 5 | [5+1 .. 5] \})))) \dots \text{by } (ls)$   
 $\rightarrow (2 | (3 | (4 | (\text{if false then } \{ \} \text{ else } \{ \} \dots \text{by } (>))$   
 $\rightarrow (2 | (3 | (4 | (5 | [5+1 .. 5])))) \dots \text{by } (if 2) \rightarrow (2 | (3 | (4 | (5 | [6 .. 5])))) \dots \text{by } (+)$