

## GCD

1. gcd(24, 36),

- gcd(36, (24 rem 36)) ... by (gcd 2)
- gcd(36, 24) ... by (remainder)
- gcd(24, (36 rem 24)) ... by (gcd 2)
- gcd(24, 12) ... by (rem)
- gcd(12, (24 rem 12)) ... by (gcd 2)
- gcd(12, 0) ... by (rem)
- 12 ... by (gcd 1)

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$$\begin{cases} \text{eg } \text{gcd}(x, 0) = x, \dots \text{gcd} 1 \\ \text{eg } \text{gcd}(x, N_2 Y) = \text{gcd}(N_2 Y, x \text{ rem } N_2 Y), \dots \text{gcd} 2 \end{cases}$$

$$*) m \text{ rem } n = (m - n) = \text{Remainder}$$

## FACT

1. fact(5),

- 5 · fact(p 5) ... by (f2)
  - 5 · fact(4) ... by (p)
  - 5 · 4 · fact(p 4) ... by (f2)
  - 5 · 4 · fact(3) ... by (p)
  - 5 · 4 · 3 · fact(p 3) ... by (f2)
  - 5 · 4 · 3 · fact(2) ... by (p)
  - 5 · 4 · 3 · 2 · fact(p 2) ... by (f2)
  - 5 · 4 · 3 · 2 · fact(1) ... by (p)
  - 5 · 4 · 3 · 2 · 1 · fact(p 1) ... by (f2)
  - 5 · 4 · 3 · 2 · 1 · fact(0) ... by (p)
  - 5 · 4 · 3 · 2 · 1 · 1 ... by (f1)
  - 5 · 4 · 3 · 2 · 1 → 120
  - 5 · 4 · 3 · 2 → 120
  - 5 · 4 · 6
  - 5 · 24
- all by (x)

$$\text{eg } \text{fact}(0) = 1, \dots f1$$

$$\text{eg } \text{fact}(N_2 X) = N_2 X \cdot \text{fact}(p N_2 X), \dots f2$$

$$*) p \text{ NN} = (-n - 1) = \text{Previous}$$

# OEDC-FACT

1. oedc-fact(5),

→ g(5, 1) ... by(2)

→ Cond(5 > 1, g(5, 2.1) · g(sd(5, 1), 2.1), 5)  
... by(g)

→ Cond(true, g(5, 2.1) · g(sd(5, 1), 2.1), 5)  
... by(>)

→ g(5, 2) · g(sd(5, 1), 2.1) ... by(Cond 1)

→ Cond(5 > 2, g(5, 2.2) · g(sd(5, 1), 2.2), 5)  
... by(g)

→ Cond(true, g(5, 2.2) · g(sd(5, 2), 2.2), 5) ... by(>)

→ g(5, 4) · g(sd(5, 2), 2.2) ... by(Cond 1)

→ Cond(5 > 4, g(5, 2.4) · g(sd(5, 4), 2.4), 5) ... by(g)

→ Cond(true, g(5, 2.4) · g(sd(5, 4), 2.4), 5) ... by(>)

→ g(5, 8) · g(sd(5, 4), 2.4) ... by(Cond 1)

→ Cond(5 > 8, g(5, 2.8) · g(sd(5, 8), 2.8), 5) ... by(g)

→ Cond(false, g(5, 2.8) · g(sd(5, 8), 2.8), 5) ... by(>)

→ 5 · g(sd(5, 4), 2.4) ... by(Cond 2)

→ g(1, 8) ... by(sd + (x)op)

→ Cond(1 > 8, g(1, 2.8) · g(sd(1, 8), 2.8), 1) ... by(g)

→ Cond(false, g(1, 2.8) · g(sd(1, 8), 2.8), 1) ... by(>)

→ 5 · 1 ... by(Cond 2)

→ 5 · g(sd(5, 2), 2.2) ... by((x)op)

→ g(3, 4) ... by(sd + (x)op)

→ Cond(3 > 4, g(3, 2.4) · g(sd(3, 4), 2.4), 3) ... by(g)

→ Cond(false, g(3, 2.4) · g(sd(3, 4), 2.4), 3) ... by(>)

$$eq \text{ oedc-fact}(0) = 1, \dots, 0 \neq 1$$

$$eq \text{ oedc-fact}(N_2 X) = g(N_2 X, 1), \dots, 0 \neq 2$$

$$eq g(X, Y) = \text{Cond}(X > Y, g(X, 2 \cdot Y) \cdot g(sd(X, Y), 2 \cdot Y), X), \dots, g$$

$$eq \text{ Cond}(\text{true}, X, Y) = X, \dots, \text{Cond 1}$$

$$eq \text{ Cond}(\text{false}, X, Y) = Y, \dots, \text{Cond 2}$$

→ 5.3 ... by (cond 2)  
 → 15.  $g(\text{sd}(5, 1), 2.1)$  ... by ( $\times$  op)  
 →  $g(4, 2)$  ... by ( $\text{sd} + \times$  op)  
 →  $\text{cond}(4 > 2, g(4, 2.2) \cdot g(\text{sd}(4, 2), 2.2), 4)$  ... by ( $g$ )  
 →  $\text{cond}(\text{true}, g(4, 2.2) \cdot g(\text{sd}(4, 2), 2.2), 4)$  ... by ( $>$ )  
 →  $g(4, 4)$  ... by ( $\text{sd}(4, 2), 2.2$ ) ... by (cond 1) + ( $\times$  op)  
 →  $\text{cond}(4 > 4, g(4, 2.4) \cdot g(\text{sd}(4, 4), 2.4), 4)$  ... by ( $g$ )  
 →  $\text{cond}(\text{false}, g(4, 2.4) \cdot g(\text{sd}(4, 4), 2.4), 4)$  ... by ( $>$ )  
 →  $4 \cdot g(\text{sd}(4, 2), 2.2)$  ... by (cond 2)  
 →  $g(2, 4)$  ... by ( $\text{sd} + \times$  op)  
 →  $\text{cond}(2 > 4, g(2, 2.4) \cdot g(\text{sd}(2, 4), 2.4), 2)$  ... by ( $g$ )  
 →  $\text{cond}(\text{false}, g(2, 2.4) \cdot g(\text{sd}(2, 4), 2.4), 2)$  ... by ( $>$ )  
 → 4.2 ... by (cond 2)  
 → 15.8 ... by ( $\times$  op)  
 → 120