



# Angular momentum imprints in the Multimessenger signals of Accretion Induced Collapse of White Dwarfs

**FAPESP**



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talk to  
NP3M collaboration  
19/10/2023

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James Webb Space Telescope's image

JOURNAL ARTICLE

# Multimessenger emission from the accretion-induced collapse of white dwarfs

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Check it for more details

# What is a White Dwarf (WD)?

## I. What are White Dwarfs?

- a. Final stage of low mass MS stars
- b. Did not burn all its fuel up to Fe
- c. Most commonly composed by C-O or O-Ne-Mg
- d. Main Features (order of magnitude):

Name	$M/M_{\odot}$	R (km)	$r_s$ (km)	$\bar{\rho}$ (g/cm <sup>3</sup> )
N.s.	2	10	6	$5 \times 10^{14}$
W.d.	1	5400	3	$3 \times 10^6$
Sun	1	$7 \times 10^5$	3	1.4
Jupiter	$10^{-3}$	$7 \times 10^4$	$3 \times 10^{-3}$	1.3
Earth	$3 \times 10^{-6}$	6000	$9 \times 10^{-6}$	5.5

Table reproduced from Gledenning's "Compact stars" book

## 2. What supports White Dwarfs?

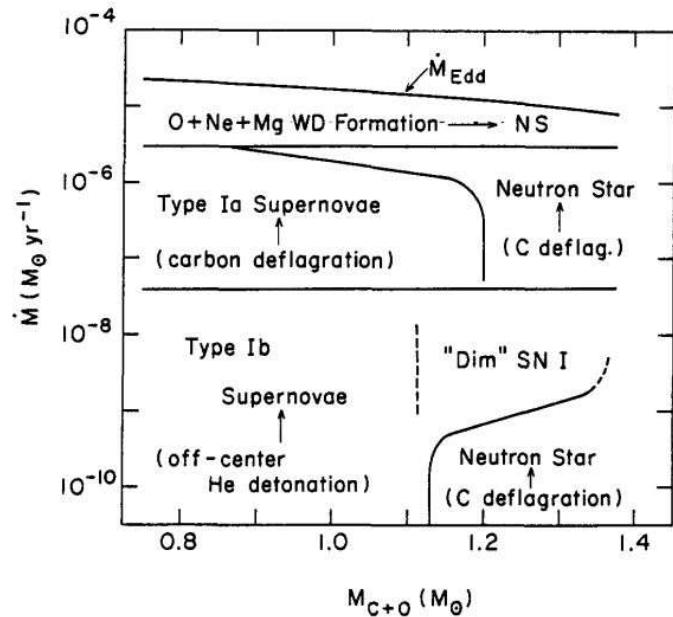
- a. No thermonuclear burning
- b. e<sup>-</sup>-degeneracy pressure
- c. Maximum mass:

$$M_{\max} \approx 5.87 \times Y_e^2 \times M_{\odot}, \quad \text{where} \quad Y_e \equiv \frac{n_e}{n_p + n_n}$$

## d. Main Assumptions / Caveats:

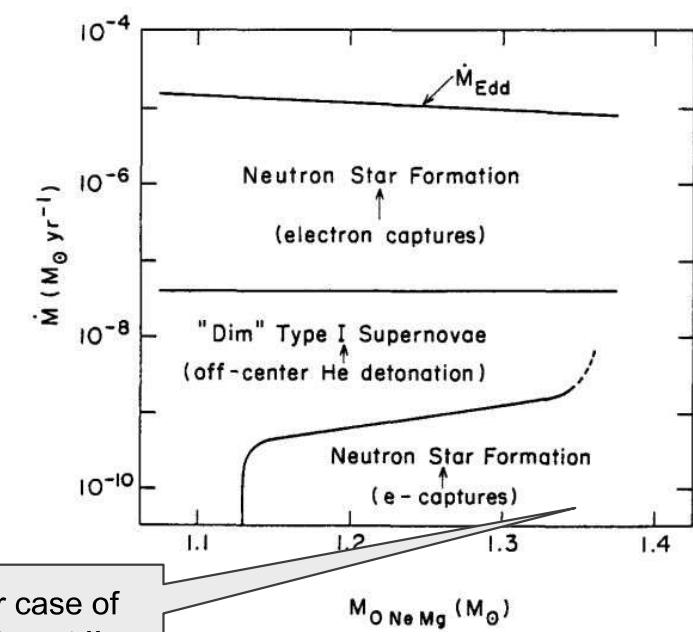
- I. Non-rotating WD – rotation is everywhere
- II. Cold WD -- mergers
- III. Isolated WD -- mergers

# What is an Accretion-induced Collapse (AIC)?



I.What is its fate?

- Unstable according to Chandrashekhar limit
- Collapse → Emits in 3 Bands of MMA
- Production of exotic isotopes as:  $^{62}\text{Ni}$ ,  $^{66}\text{Zn}$ ,  $^{68}\text{Zn}$ ,  $^{87}\text{Rb}$ ,  $^{88}\text{Sr}$
- Historically connected to: sGRB's, ms-pulsars



Our case of Interest !!

Images reproduced from Nomoto '86

# Can it happen? Possible Sources

## I. ZTF J1901+1458

Article | Published: 30 June 2021

### A highly magnetized and rapidly rotating white dwarf as small as the Moon

Ilaria Caiazzo Kevin B. Burdge, James Fuller, Jeremy Heyl, S. R. Kulkarni, Thomas A. Prince, Harvey B. Richer, Josiah Schwab, Igor Andreoni, Eric C. Bellm, Andrew Drake, Dmitry A. Duev, Matthew J. Graham, George Helou, Ashish A. Mahabal, Frank J. Masci, Roger Smith & Maayane T. Soumagnac

Nature 595, 39–42 (2021) | Cite this article

4766 Accesses | 28 Citations | 858 Altmetric | Metrics

## II. S Ophiuchi

### a. Red Giant

$$M = (0.7 - 0.8)M_{\odot} \quad (\text{E. Brandim et al.'09})$$

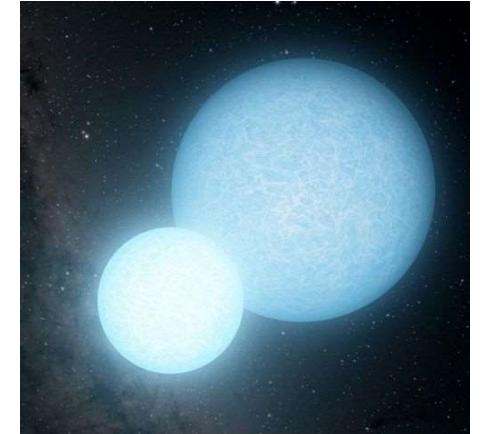
### b. WD

$$M = (1.2 - 1.4)M_{\odot} \quad (\text{E. Brandi et al.'09})$$

### c. Accretion

$$\dot{M} = ??$$

Image reproduced from astronomy.com  
Artistic comparison of a regular  
and a supermassive WD



## III. T Coronae Borealis

### a. Red Giant

$$M = (1.12 \pm 0.23)M_{\odot} \quad (\text{J.D. Linford et al.'19})$$

### b. WD

$$M = (1.37 \pm 0.13)M_{\odot} \quad (\text{J.D. Linford et al.'19})$$

### c. Accretion

$$\dot{M} = 6.7 \times 10^{-9} M_{\odot} \text{yr}^{-1} \quad (\text{G.J.M. Luna et al.'18})$$

# Numerical set-up & Initial data

Numerical details:

I. Hydrodynamics: WhiskyTHC

(Radice et al.'12 '13 '14 '16 '18 '21)

II. Neutrinos:

a. De-leptonization (Liebendörfer'05) & WhiskyTHC

III. Einstein Toolkit (Löffer et al. '12):

a. Initial data: RNDS thorn (Stergioulas & Friedman '95)

b. Spacetime evolution: CTGamma thorn

(Pollney et al. '11; Reisswig et al. '13),

c. AMR grid by CARPET thorn (Schnetter et al. '04)

IV. Novelties:

a. 3D (mirror symmetry on rotation axis)

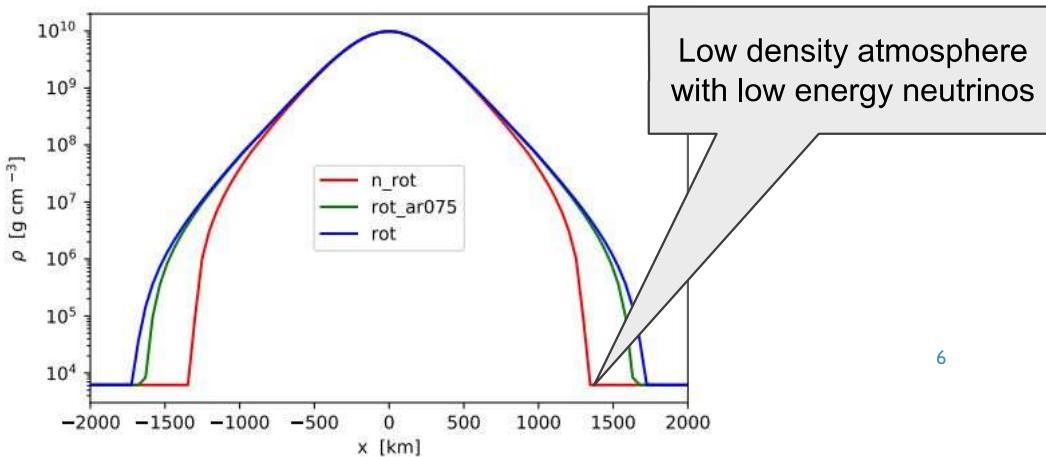
b. Full GR

VI. Previous models are either:

a. 2D simulations (Abdikamalov et al. '10)

b. Newtonian Gravity (Dessart et al. '06 '07)

Simulation	$\rho_0$ [g cm $^{-3}$ ]	Temp. [MeV]	$M$ [ $M_\odot$ ]	$M_{\text{bar.}}$ [ $M_\odot$ ]	$R$ [km]
rot	$9.95 \times 10^9$	0.01	1.52	1.53	$1.93 \times 10^3$
rot_ar075	$9.95 \times 10^9$	0.01	1.51	1.53	$1.71 \times 10^3$
nrot	$9.95 \times 10^9$	0.01	1.45	1.47	$1.33 \times 10^3$
Simulations	$J$ [g cm $^2$ s $^{-1}$ ]	$T/W$	$\Omega$ [Hz]	$\Omega_{\text{Kepler}}$ [Hz]	$a_r$
rot	$3.26 \times 10^{49}$	$1.49 \times 10^{-2}$	5.28	5.30	0.66
rot_ar075	$3.08 \times 10^{49}$	$1.37 \times 10^{-2}$	5.09	6.38	0.75
nrot	0	0	0	9.03	1.00



# Electron Fraction Dynamics

## I. De-leptonization of the core

a. Parameterized scheme by Liebendörfer'05:

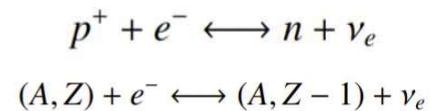
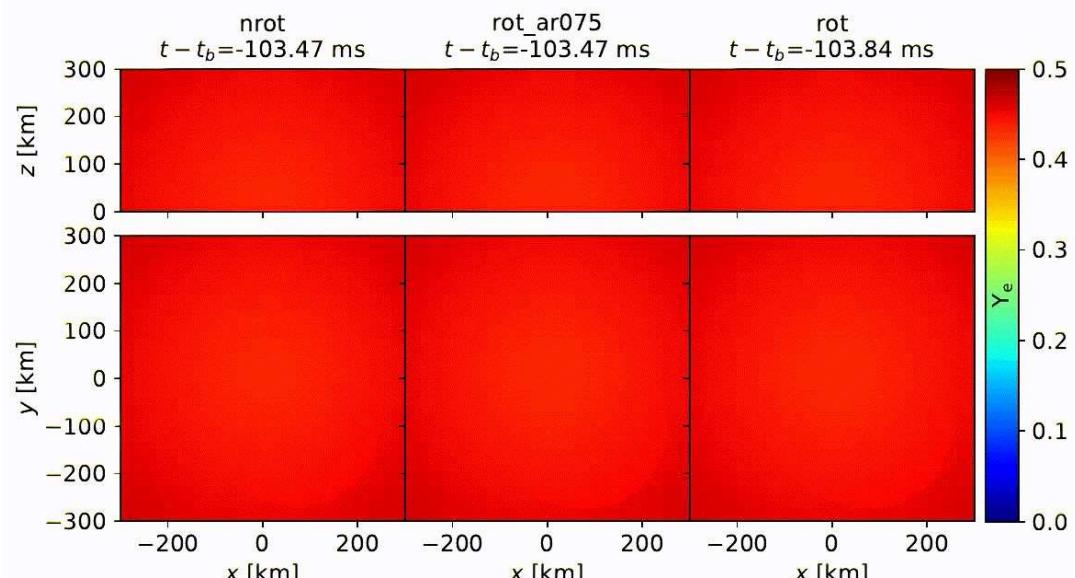
$$Y_e = Y_e(\rho)$$

b. Diminishing the  $e^-$  density diminishes the supporting pressure

From the theory of fermionic gases

$$\epsilon \rightarrow 3p \approx \frac{1}{4\pi^2} (3\pi^2 \rho)^{4/3} \quad (\text{high density, } k \gg m),$$

$$\rho = \frac{k^3}{3\pi^2}$$



# Mass Motion

I. Initial purely outgoing motion

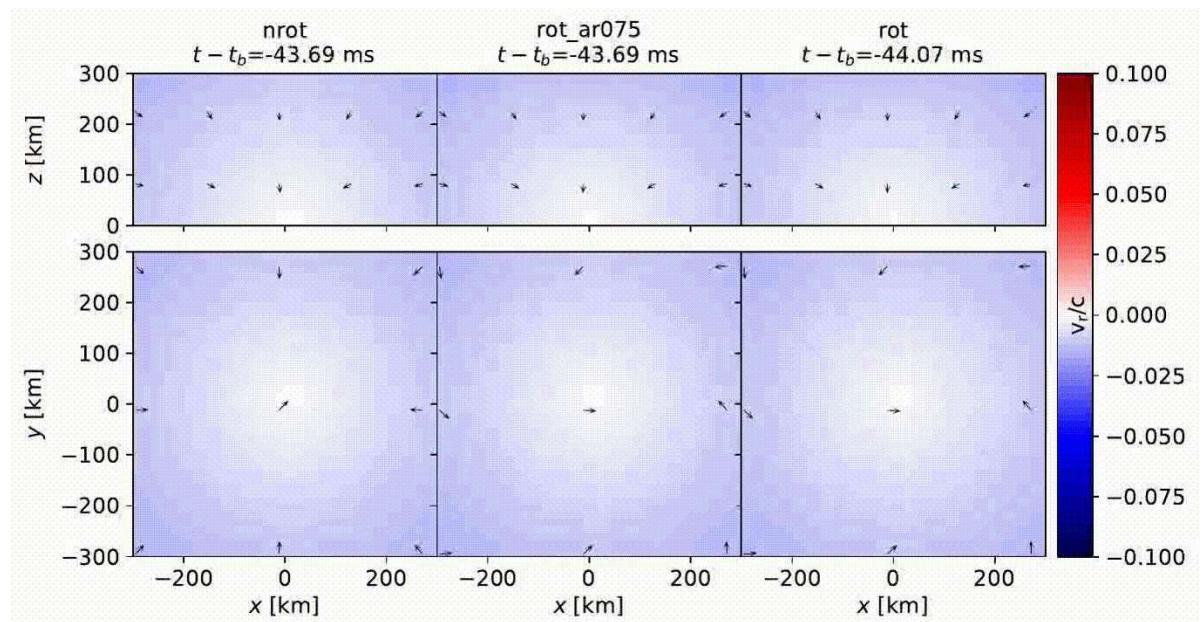
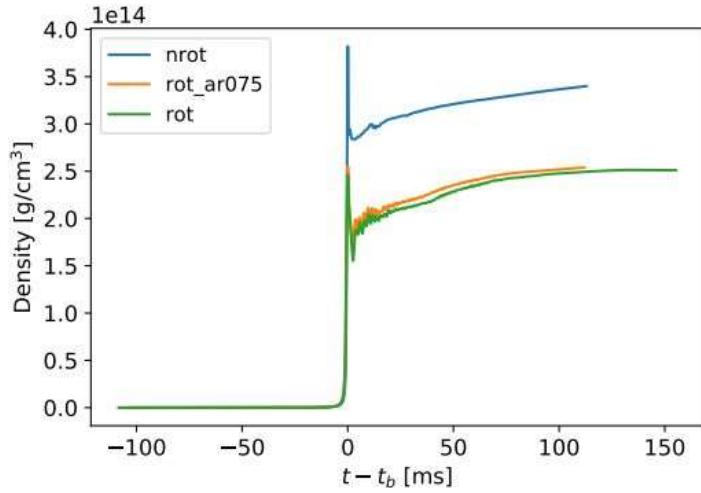
II. Core bounces:

a. Star central density approaches

$$\rho_{\text{nuc}} \approx 2.7 \times 10^{14} \text{ g cm}^{-3}$$

b. Core stiffens and bounce

c. Outward motion starts



# Mass Motion

I. Initial purely outgoing motion

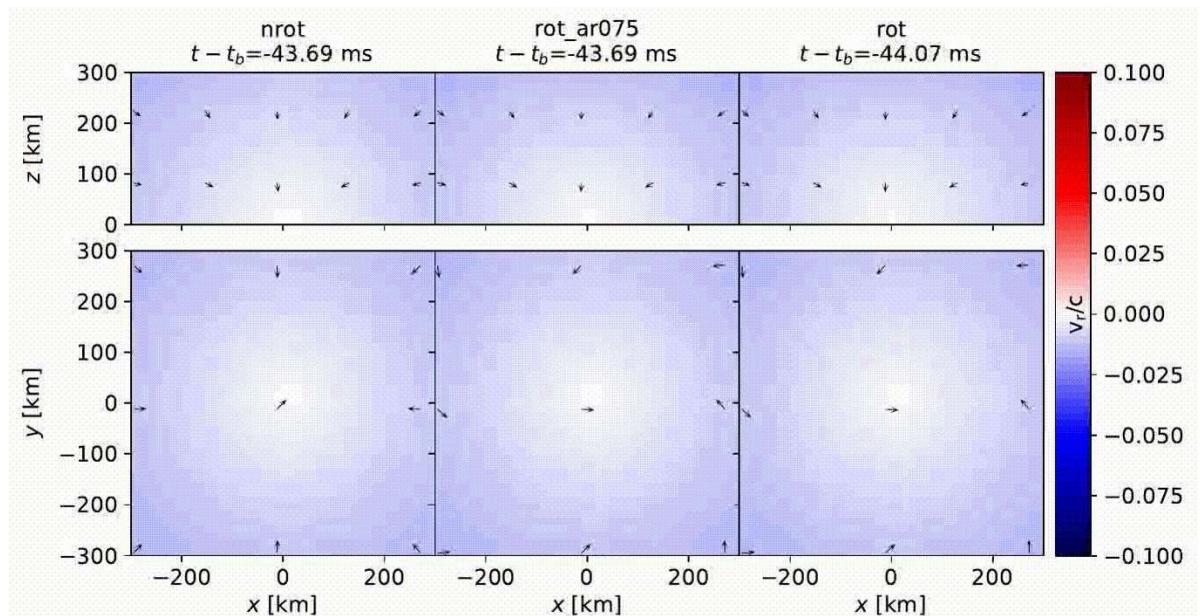
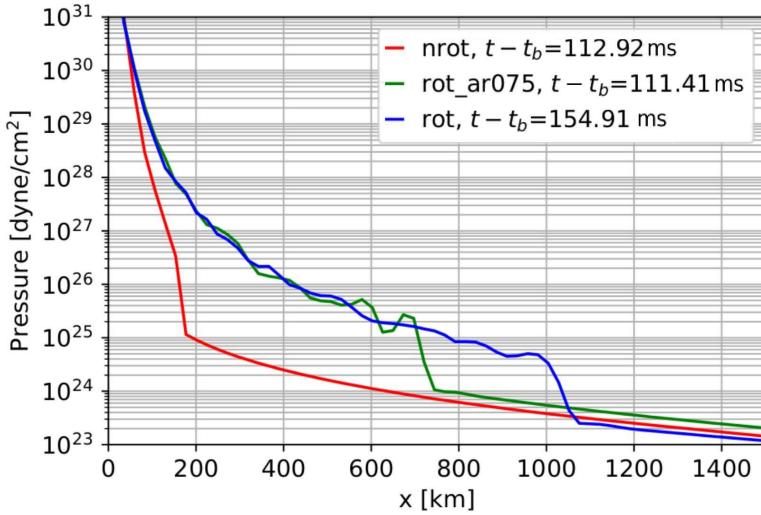
II. Core bounces:

a. Star central density approaches

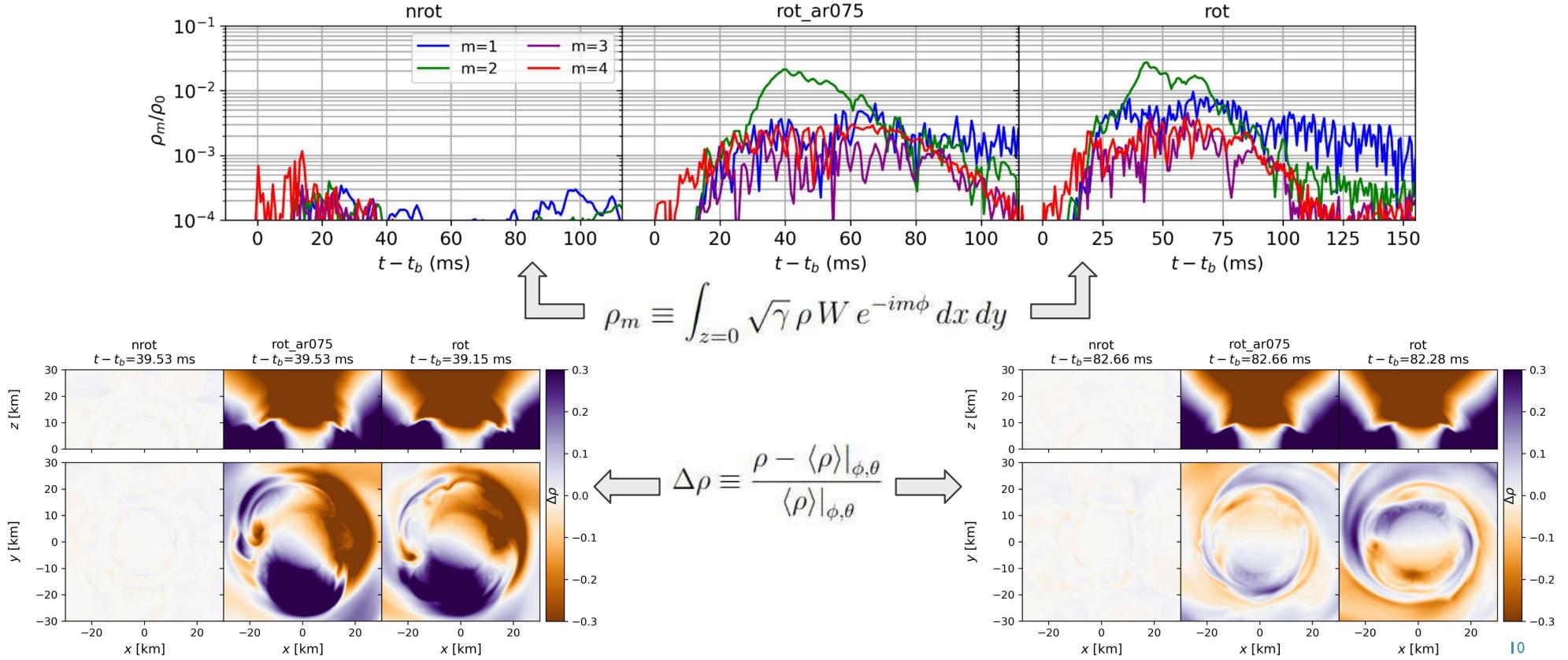
$$\rho_{\text{nuc}} \approx 2.7 \times 10^{14} \text{ g cm}^{-3}$$

b. Core stiffens and bounce

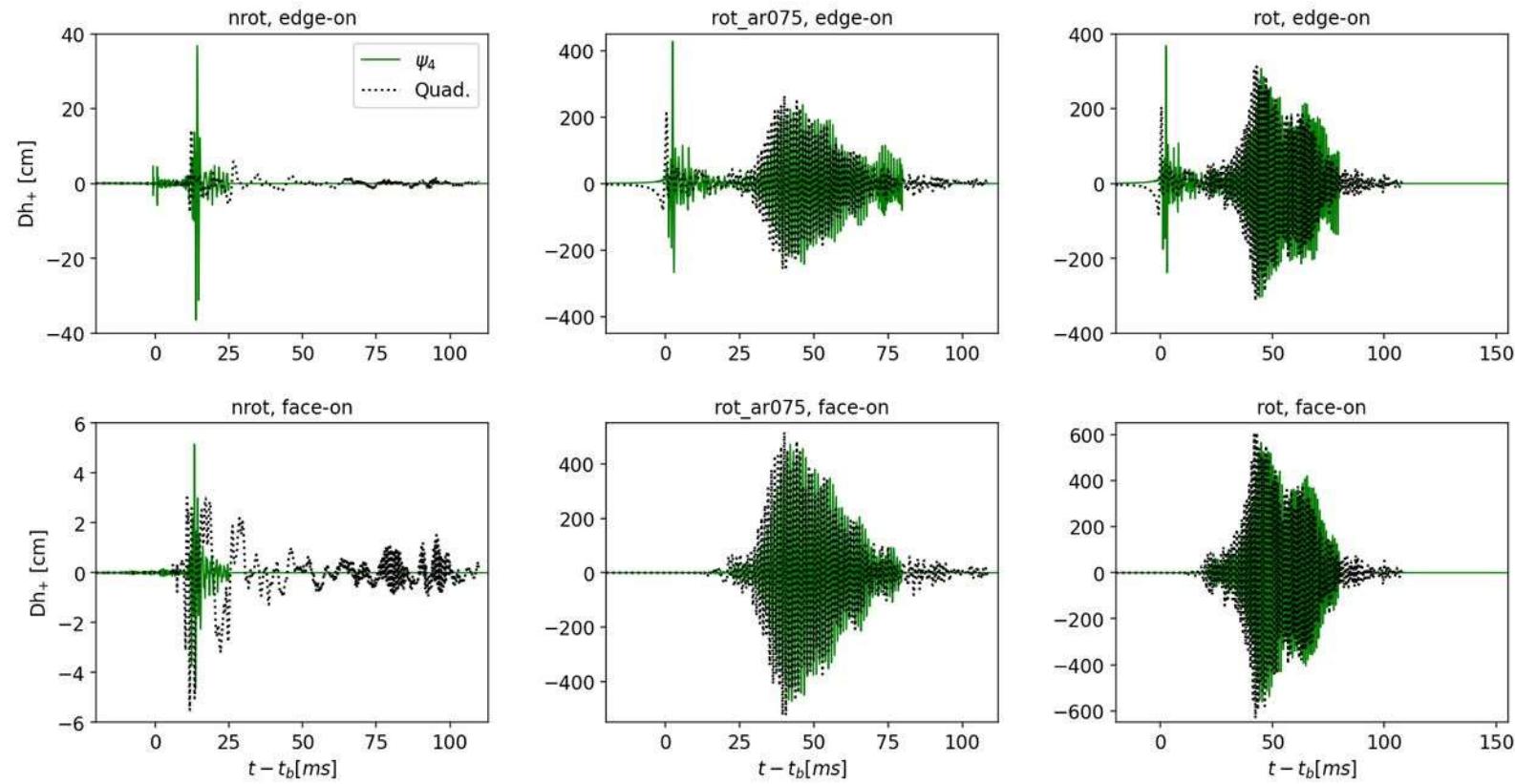
c. Outward motion starts



# Mass Distribution: m=1 Instability



# Gravitational Waves: Time domain



# Gravitational Waves: Polarization

What about polarization?

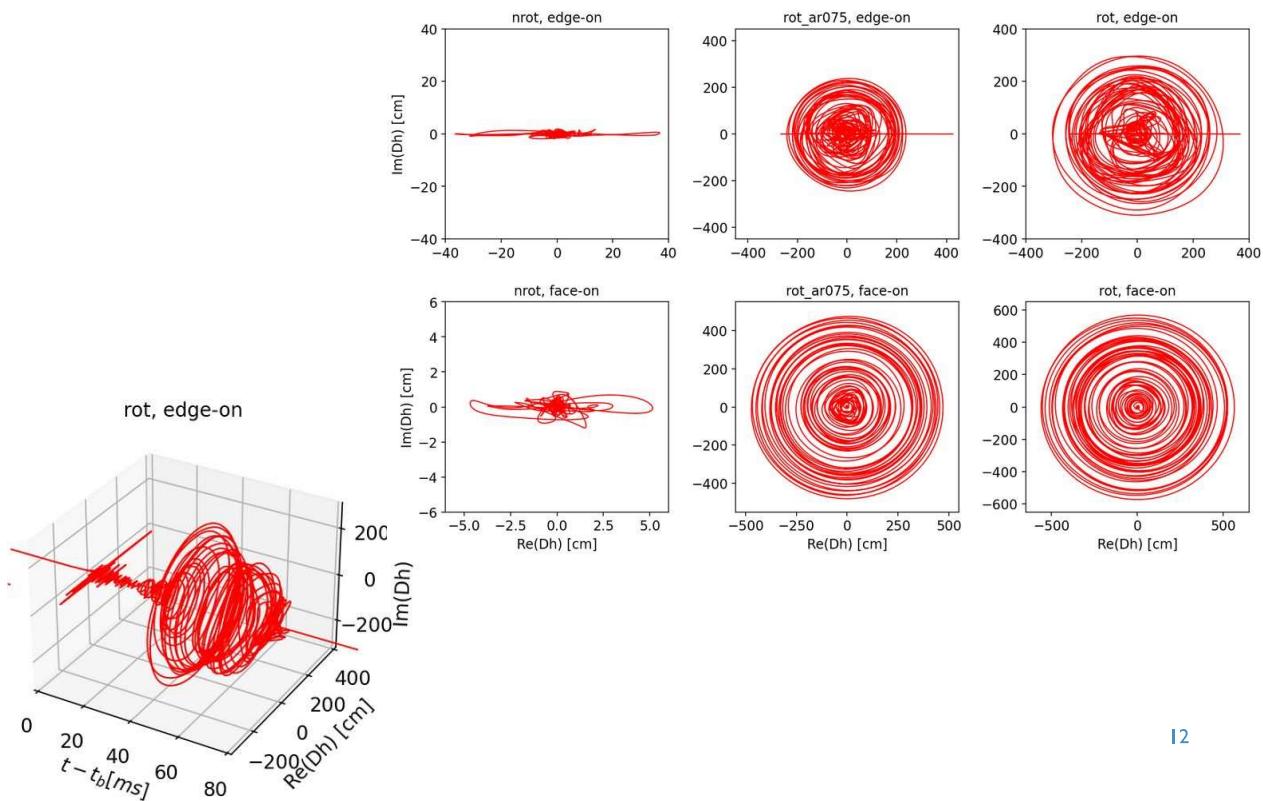
In K. Hayama et al.'18:

I. Polarization can tell us about :

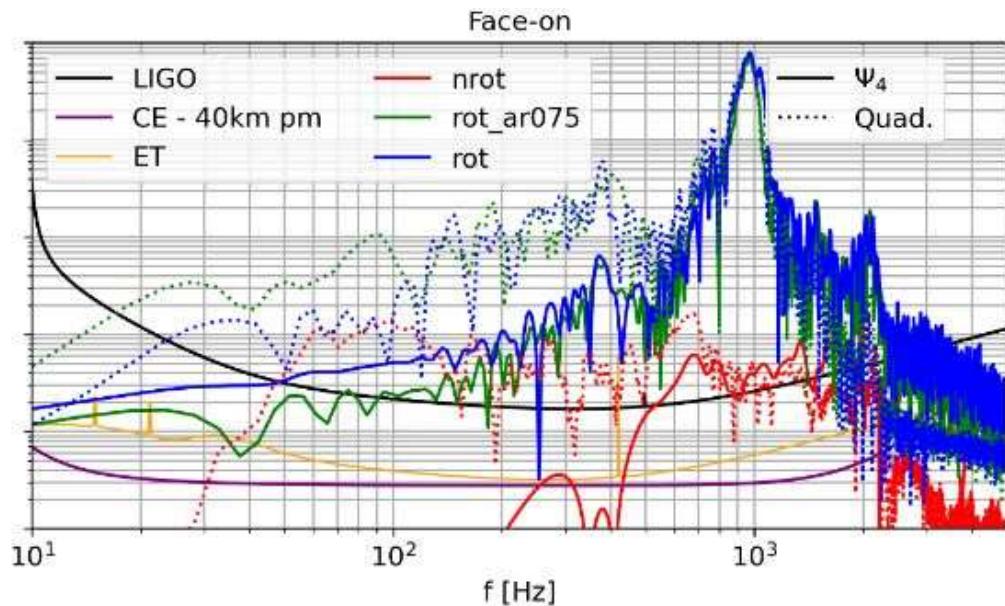
- a. EOS
- b. Presence of SASI instability

In our models:

- a.m=0: linear polarization
- b. m=2: Circular polarization
- c. No sign flip of the (m=2) polarization
- d. No evidence for SASI



# Gravitational Waves: Dectectability at 10kpc

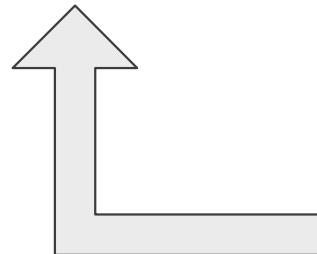


Model	LIGO	CE	ET
nrot ( $\Psi_4$ edge-on)	$1.7 \times 10^1$	$1.5 \times 10^2$	$7.6 \times 10^1$
nrot (Quad. edge-on)	$1.1 \times 10^1$	$7.7 \times 10^1$	$5.5 \times 10^1$
nrot ( $\Psi_4$ face-on)	$2.1 \times 10^0$	$1.8 \times 10^1$	$9.5 \times 10^0$
nrot (Quad. face-on)	$6.7 \times 10^0$	$4.9 \times 10^1$	$3.4 \times 10^1$
rot_ar075 ( $\Psi_4$ edge-on)	$4.3 \times 10^2$	$3.7 \times 10^3$	$1.9 \times 10^3$
rot_ar075 (Quad. edge-on)	$4.3 \times 10^2$	$3.6 \times 10^3$	$2.0 \times 10^3$
rot_ar075 ( $\Psi_4$ face-on)	$7.8 \times 10^2$	$6.7 \times 10^3$	$3.5 \times 10^3$
rot_ar075 (Quad. face-on)	$8.1 \times 10^2$	$6.9 \times 10^3$	$3.7 \times 10^3$
rot ( $\Psi_4$ edge-on)	$5.1 \times 10^2$	$4.4 \times 10^3$	$2.3 \times 10^3$
rot (Quad. edge-on)	$5.1 \times 10^2$	$4.3 \times 10^3$	$2.3 \times 10^3$
rot ( $\Psi_4$ face-on)	$9.5 \times 10^2$	$8.2 \times 10^3$	$4.3 \times 10^3$
rot (Quad. face-on)	$9.7 \times 10^2$	$8.3 \times 10^3$	$4.4 \times 10^3$

Best case scenario

# Gravitational Waves: Detection Horizons (SNR = 8)

<b>rot (<math>\Psi_4</math>)</b>	<b>LIGO</b>	<b>CE</b>	<b>ET</b>
edge-on	~ 0.6 Mpc	~ 5 Mpc	~ 3 Mpc
face-on	~ 1 Mpc	~ 10 Mpc	~ 5 Mpc



Model	LIGO	CE	ET
nrot ( $\Psi_4$ edge-on)	$1.7 \times 10^1$	$1.5 \times 10^2$	$7.6 \times 10^1$
nrot (Quad. edge-on)	$1.1 \times 10^1$	$7.7 \times 10^1$	$5.5 \times 10^1$
nrot ( $\Psi_4$ face-on)	$2.1 \times 10^0$	$1.8 \times 10^1$	$9.5 \times 10^0$
nrot (Quad. face-on)	$6.7 \times 10^0$	$4.9 \times 10^1$	$3.4 \times 10^1$
rot_ar075 ( $\Psi_4$ edge-on)	$4.3 \times 10^2$	$3.7 \times 10^3$	$1.9 \times 10^3$
rot_ar075 (Quad. edge-on)	$4.3 \times 10^2$	$3.6 \times 10^3$	$2.0 \times 10^3$
rot_ar075 ( $\Psi_4$ face-on)	$7.8 \times 10^2$	$6.7 \times 10^3$	$3.5 \times 10^3$
rot_ar075 (Quad. face-on)	$8.1 \times 10^2$	$6.9 \times 10^3$	$3.7 \times 10^3$
rot ( $\Psi_4$ edge-on)	$5.1 \times 10^2$	$4.4 \times 10^3$	$2.3 \times 10^3$
rot (Quad. edge-on)	$5.1 \times 10^2$	$4.3 \times 10^3$	$2.3 \times 10^3$
rot ( $\Psi_4$ face-on)	$9.5 \times 10^2$	$8.2 \times 10^3$	$4.3 \times 10^3$
rot (Quad. face-on)	$9.7 \times 10^2$	$8.3 \times 10^3$	$4.4 \times 10^3$

# Detection Rates

Based on SNIa rates:

I. SNIa:  $3 \times 10^{-4} \text{ yr}^{-1} \text{Mpc}^{-3}$  (Cappellaro et al.'2015)

II.AIC:

a.LIGO:  $(x/10\%) \times 2.2 \times 10^{-4} \text{ yr}^{-1}$

b.CE:  $(x/10\%) \times 0.14 \text{ yr}^{-1}$

Cavients:

I. Unknown relative fraction AIC to SNIa

Based on nucleosynthesis (Fryer et al.'99):

I.Upper limit as  $\sim 200 \text{ AIC / Myr / galaxy}$

II. 45 I galaxies for  $D < 10 \text{ Mpc}$  (Karachentsev et al'04)

III.AIC rate  $\sim 0.08 \text{ yr}^{-1}$

Cavients:

I.Assuming that all galaxies contribute equally to AIC rate

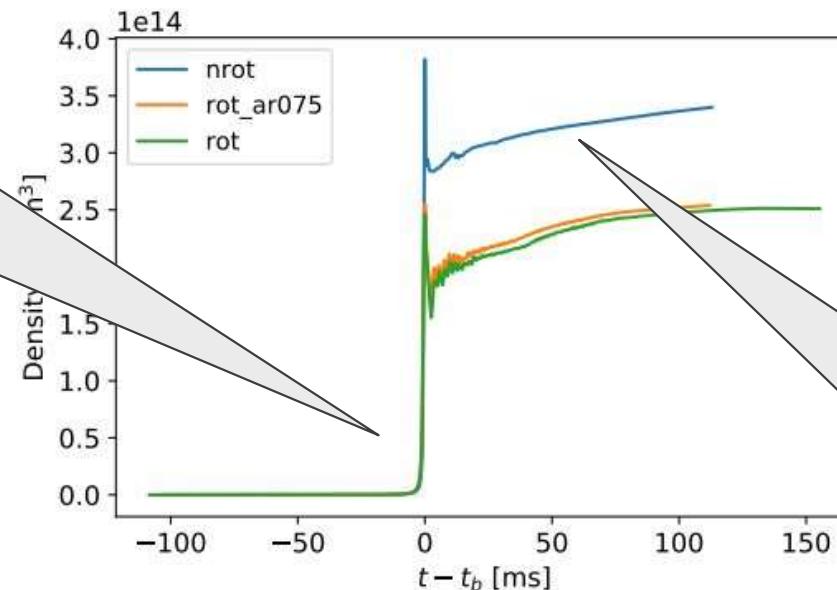
II.All exotic neutron-rich material are produced by AIC

# Neutrino Treatment

Pre-bounce phase:  
Liebendörfer'05  
de-leptonization scheme

$$Y_e = Y_e(\rho)$$

Although it assumes the  $\beta$  decay  
No neutrino is accounted for  
WD is considered to be  
transparent at this point



Post-bounce phase:  
Radice et al.'21  
Neutrino M1 treatment  
Neutrinos opacities are numerically  
solved for  
Includes Doppler effects at all  
orders  
in v/c  
Accounts for non-linear couplings  
between neutrino and matter<sup>[6]</sup>

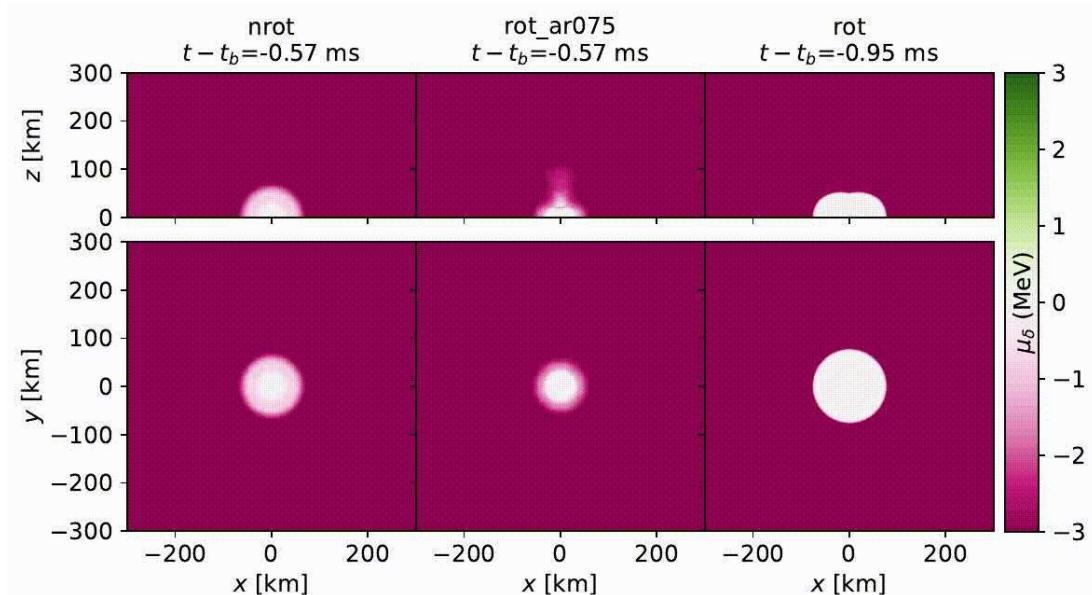
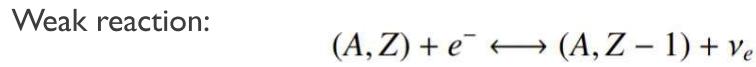
# Chemical Potential

$$\mu_\delta = \mu_n + \mu_v - \mu_e - \mu_p$$

If  $\mu_\delta = 0$ ,  $\beta$ - equilibrium  $\rightarrow$  Neutrinos in thermal equil.

If  $\mu_\delta > 0$ , leptonize  $\rightarrow$  Absorbs Neutrinos

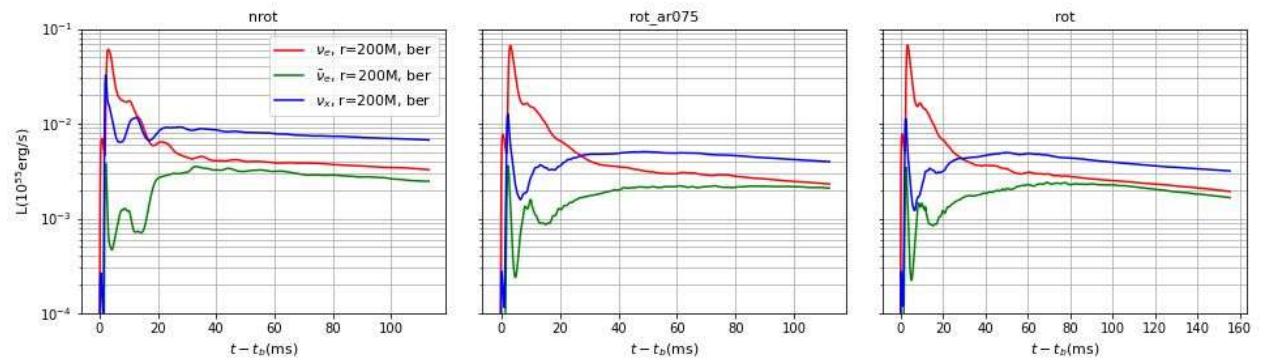
If  $\mu_\delta < 0$ , neutronize  $\rightarrow$  Neutrinos Emission



# Neutrino Luminosity :AIC vs CCSNe

## I.AIC (at 100 ms)

- a.  $L_{\nu_e} \approx 4 \times 10^{52} \text{ erg s}^{-1}$
- b.  $L_{\bar{\nu}_e} \approx 3 \times 10^{52} \text{ erg s}^{-1}$
- c.  $L_{\nu_x} \approx 7 \times 10^{52} \text{ erg s}^{-1}$
- d. O(1) correction due rotation



## 2. CCSNe at 100 ms (H. Nagakura et al.'21)

- a.  $L_{\nu_e} \approx (4 - 8) \times 10^{52} \text{ erg s}^{-1}$
- b.  $L_{\bar{\nu}_e} \approx (4 - 8) \times 10^{52} \text{ erg s}^{-1}$
- c.  $L_{\nu_x} \approx (2.5 - 3.5) \times 10^{52} \text{ erg s}^{-1}$

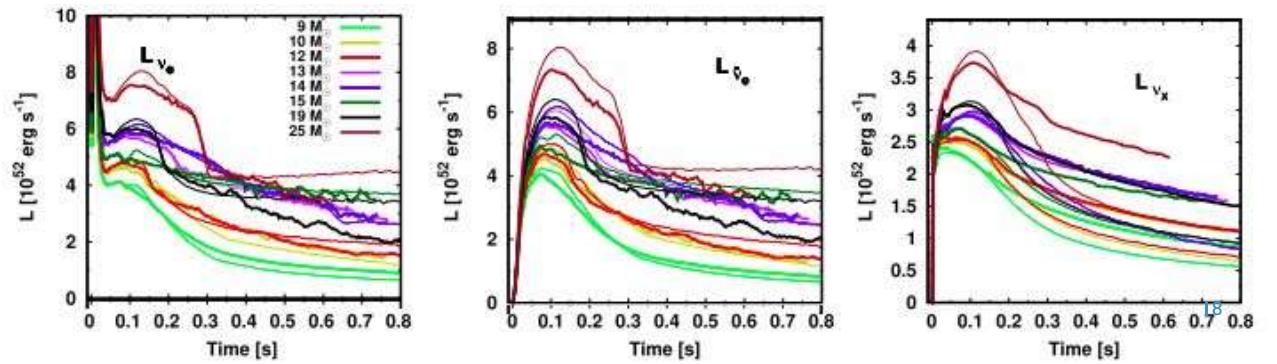
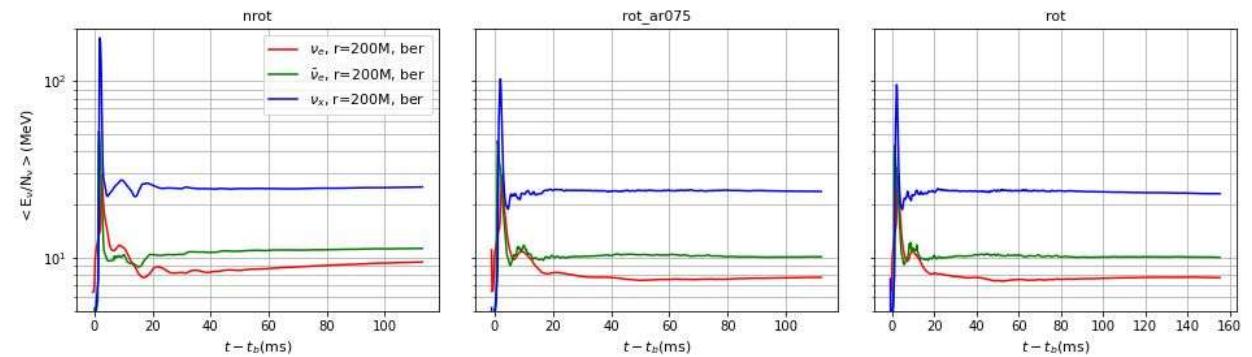


Image reproduced from H. Nagakura et al.'21

# Neutrino Average Energy :AIC vs CCSNe

## 1. AIC (at 100 ms)

- a.  $\langle E/N \rangle_{\nu_e} \approx 9 \text{ MeV}$
- b.  $\langle E/N \rangle_{\bar{\nu}_e} \approx 12 \text{ MeV}$
- c.  $\langle E/N \rangle_{\nu_x} \approx 25 \text{ MeV}$



## 2. CCSNe (at 100 ms)

- a.  $\langle E/N \rangle_{\nu_e} \approx 9 \text{ MeV}$
- b.  $\langle E/N \rangle_{\bar{\nu}_e} \approx 12 \text{ MeV}$
- c.  $\langle E/N \rangle_{\nu_x} \approx 15 \text{ MeV}$

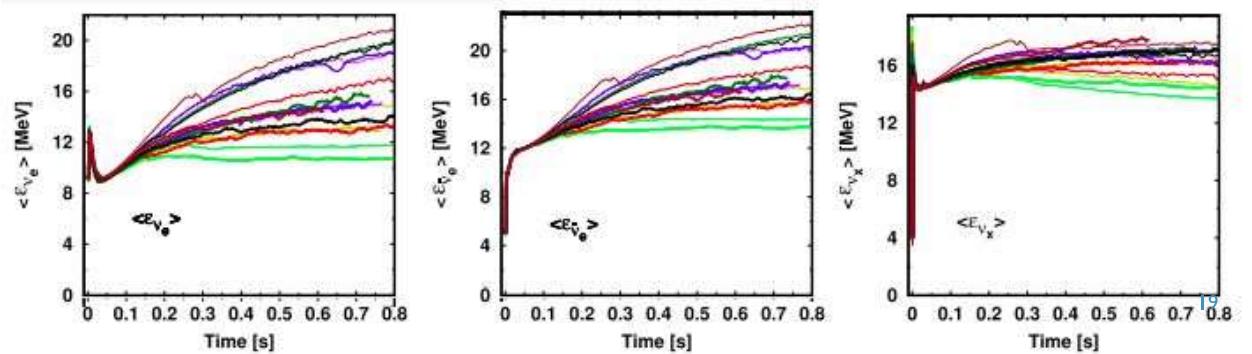
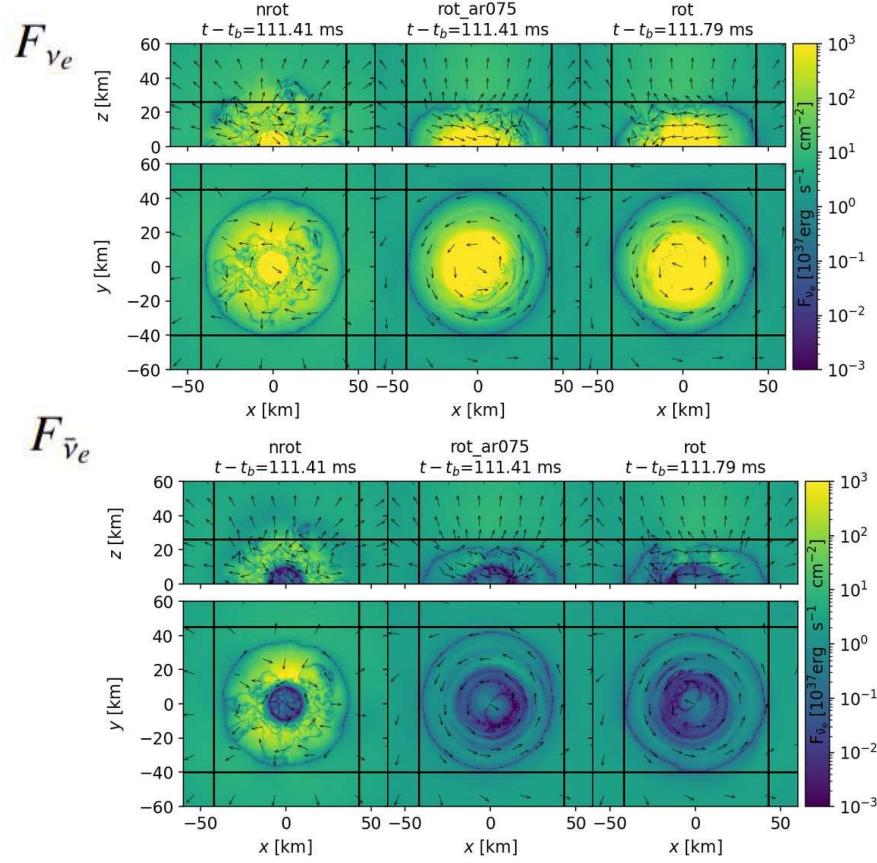


Image reproduced from H. Nagakura et al.'21

# Neutrino emission



What can it tell us?

I. Flux

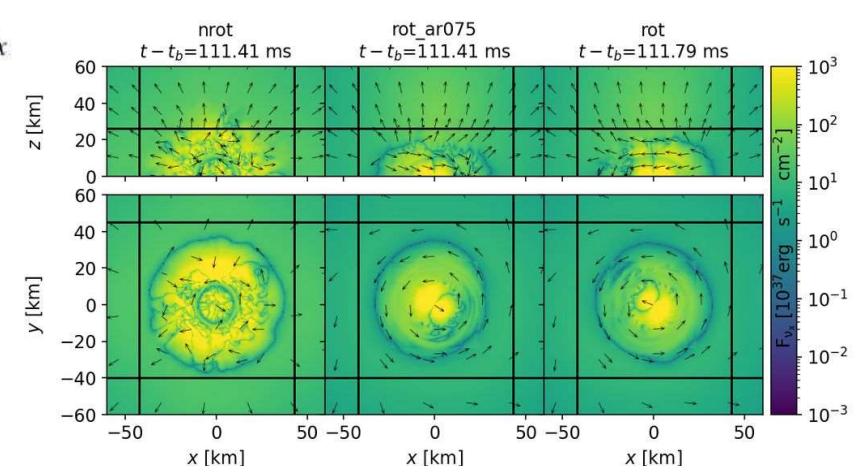
$$F_{\nu_e} > F_{\bar{\nu}_e} > F_{\nu_\mu}$$

II. Thermal decoupling

$$R_{\nu_e} > R_{\bar{\nu}_e} > R_{\nu_\mu}$$

III. Temperature

$$T_{\nu_e} < T_{\bar{\nu}_e} < T_{\nu_\mu}$$



# Ejecta Properties

## I. Temperature:

Ejecta cools down as it expands

## II. Entropy:

Roughly constant

$O(1)$  adiabatic expansion

## III. Ye:

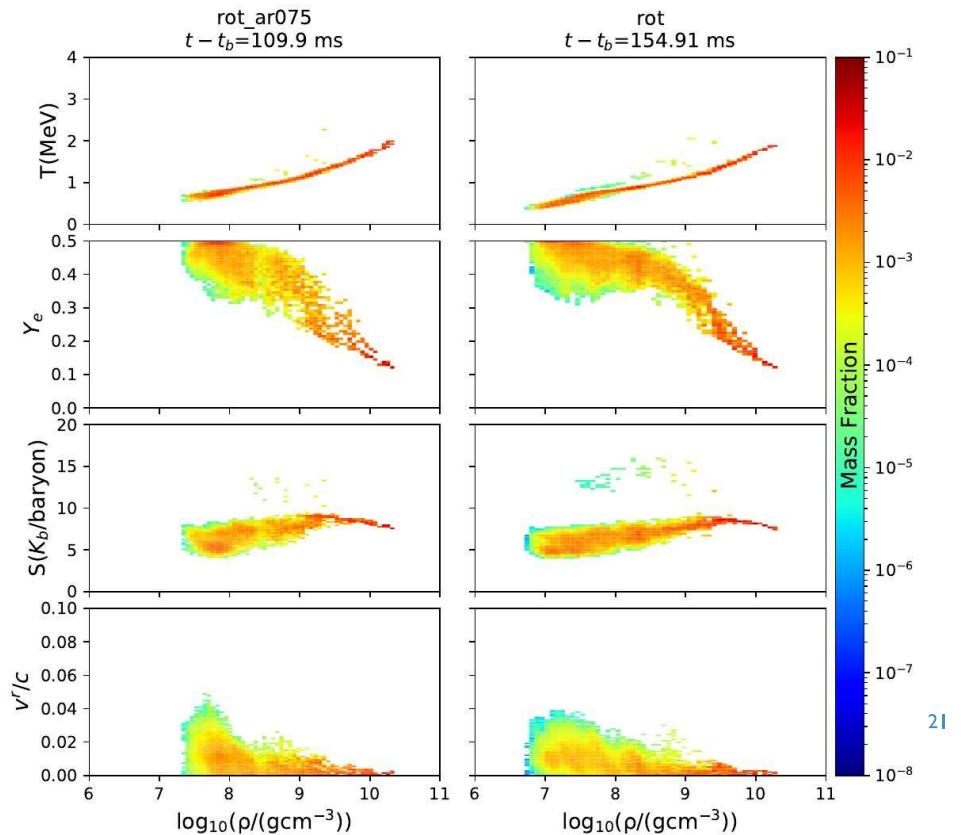
Ejecta with almost symmetric electron fraction ( $\sim 0.46$ )

## IV. Ejecta Mass:

No evidence of ejecta for the non-rotating case (stalled shock)

Around  $M_{ej} \approx 3 \times 10^{-2} M_{\odot}$  for both rotating models

Agreement with 1D models of Metzger et al. '09



# Ejecta Energy

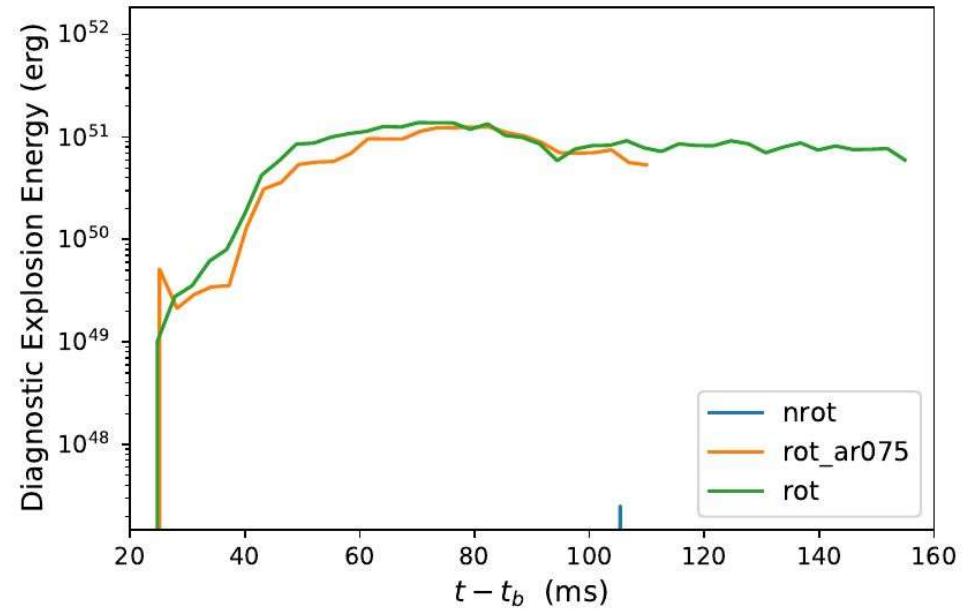
Relativistic energy :

$$E_{\text{exp.}} = \int_V \left( \rho \varepsilon W^2 + \rho W(W - 1) + P(W^2 - 1) \right) \sqrt{\gamma} dV$$

$$E_{\text{exp.}} \sim 5.3 \times 10^{50} \text{ erg (rot\_ar075)}$$
$$E_{\text{exp.}} \sim 5.9 \times 10^{50} \text{ erg (rot)}$$

Ejecta velocity :

$$v_\infty^r \sim (2E_{\text{exp.}}/M_{\text{ej.}})^{1/2}$$
$$\sim 0.14c$$



# Electromagnetic Emission

Arnett's Law (Arnett'82):

$$L_{\text{peak}} \sim \dot{Q}(t_{\text{peak}})$$

Peak Luminosity (Metzger '20):

$$L_{\text{peak}} \approx 10^{41} \text{ erg s}^{-1} \left( \frac{\epsilon_{\text{th,v}}}{0.5} \right) \left( \frac{M}{10^{-2} M_{\odot}} \right)^{0.35} \left( \frac{v}{0.1c} \frac{1 \text{ cm}^2 \text{ g}^{-1}}{\kappa} \right)^{0.65}$$

Time of peak (Metzger '20):

$$t_{\text{peak}} \approx 1.6 \text{ days} \left( \frac{M}{10^{-2} M_{\odot}} \right)^{1/2} \left( \frac{v}{0.1c} \frac{1 \text{ cm}^2 \text{ g}^{-1}}{\kappa} \right)^{-1/2}$$

Estimates for our models

$$L_{\text{peak}} = 5.1 \times 10^{41} \text{ erg/s} \quad t_{\text{peak}} = 1 \text{ day} \text{ (rot_ar075)}$$

$$L_{\text{peak}} = 5.5 \times 10^{41} \text{ erg/s} \quad t_{\text{peak}} = 1.3 \text{ days} \text{ (rot)}$$



Image reproduced from [www.nasa.gov](http://www.nasa.gov)  
James Webb Space Telescope's image

## Comparison against SNIa

$$L_{\text{peak}} = 5.1 \times 10^{41} \text{ erg/s} \quad t_{\text{peak}} = 1 \text{ day} \text{ (rot\_ar075)}$$

$$L_{\text{peak}} = 5.5 \times 10^{41} \text{ erg/s} \quad t_{\text{peak}} = 1.3 \text{ days (rot)}$$

AIC are:

- a. Faster evolving than SNIa: timescale of ~ weeks
- b. Fainter than SNIa :
  - By 2 orders of magnitude
  - Mainly due a lower ejecta mass for SNIa
  - (K D Wilk et al.'18)
  - Not likely to be observed as far (but still far enough)

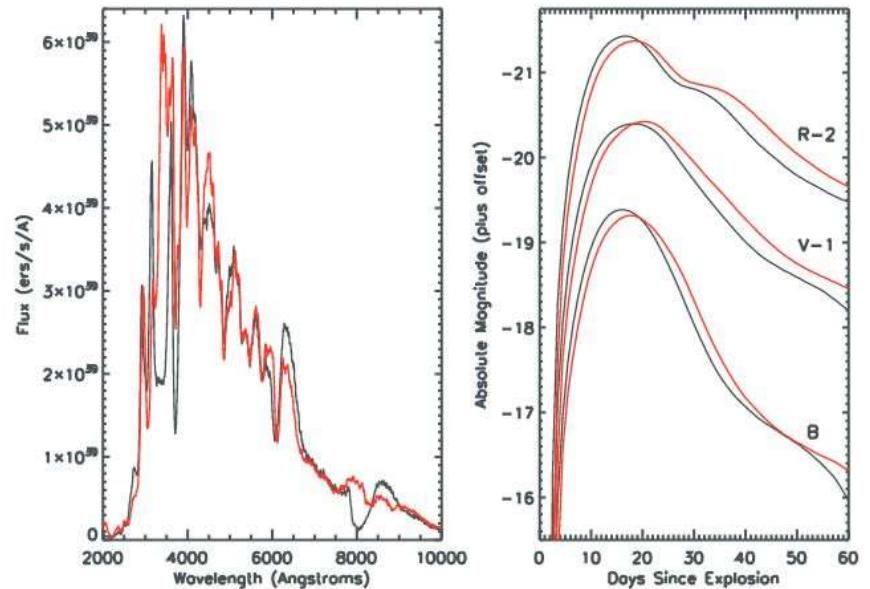


Image reproduced from Woosley et al.'07

# Conclusions

Gravitational radiation:

- I. kHz band
- II.  $D_h \sim 500$  cm
- III. Polarization
  - i.  $m=0$  (prompt emission) linear
  - ii.  $m=2$  (late emission) circular
- IV. Detectable up to  $D \sim 10$  Mpc in CE

Electromagnetic radiation:

- I.  $n_{\text{rot}} \sim$  no ejecta mass  $\sim$  no EM emission
- II.  $\text{rot\_ar075}$  and  $\text{rot}$ :
  - i.  $L \sim 5 \times 10^{41}$  erg/s ( $\sim 10^2 \times$  less than SNIa)
  - ii. time scale of few days (few weeks for SNIa)

Neutrino emission ( $\sim 100$ ms after bounce):

- I. Neutrino luminosities  $\sim 4-7 \times 10^{52}$  erg/s
- II. Average energy per neutrino  $\sim 9-25$  MeV
- III. Slight suppression due to rotation
- IV. Comparable to CCSNe (H.Nagakura et al.'20)



# Angular momentum imprints in the Multimessenger signals of Accretion Induced Collapse of White Dwarfs

**FAPESP**



# THANK YOU!

# Possible connection to GRBs & Future Work

Works such B. D. Metzger et al.'08 :

- I. AIC produces a protomagnetar and a disc of  $M \sim 0.1 M_\odot$  ( $t \sim 100$  ms)
- II. Disc accretion, prompt EM emission ( $t \sim 0.1 - 1$  s)
- III. Neutrino wind becomes ultra-relativistic ( $t \sim 3-10$  s)
- IV. Protomagnetar spins down, X-ray emission ( $t \sim 10-100$  s)

Realizable?

- I. sGRB+EE : such as GRB211211A

Future work:

- I. Inclusion of magnetic fields
- II. Jet formation (?)
- III. Light curves
- IV. Comparison against events like GRB211211A

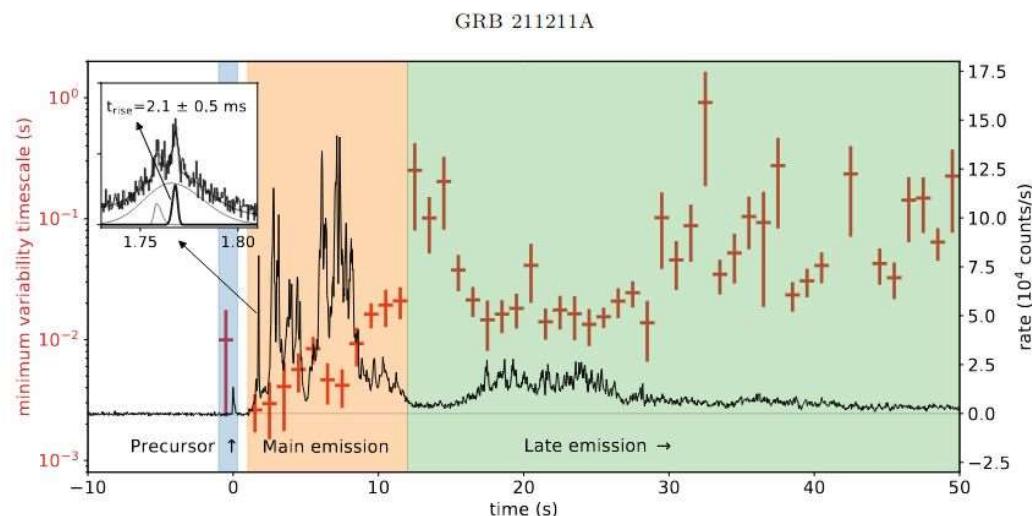
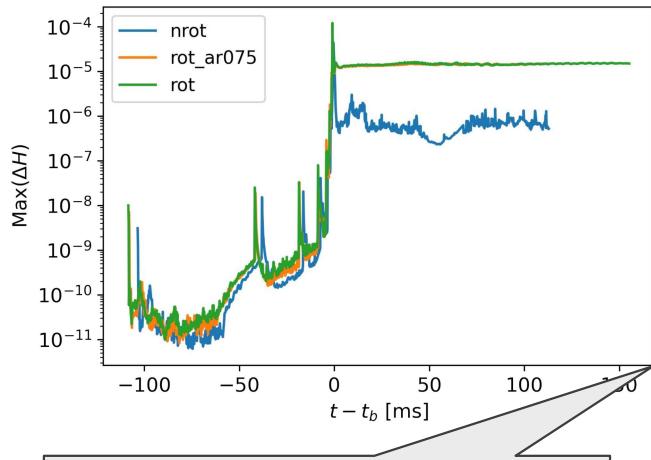


Image reproduced from  
P.Veres et al 2023 ApJL 954 L5

# Error Control



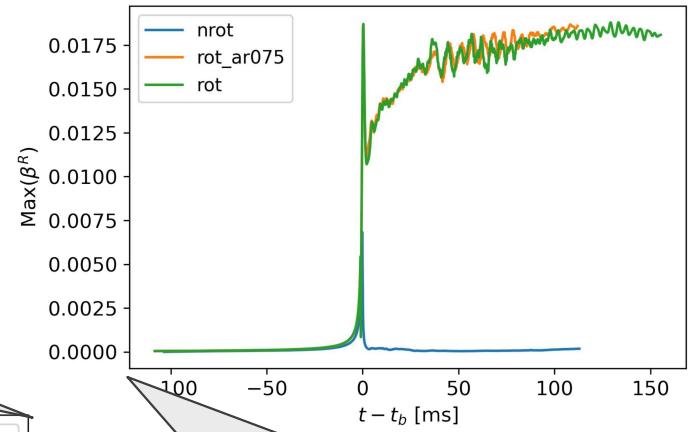
$${}^{3D}R + K^2 - K_{ij}K^{ij} = 16\pi E$$

$$\Delta H = |{}^{3D}R + K^2 - K_{ij}K^{ij} - 16\pi E|$$

$$g_{\mu\nu}dx^\mu dx^\nu = -\alpha^2 dt^2 + \gamma_{ij}(dx^i - \beta^i dt)(dx^j - \beta^j dt)$$

$$g_{\mu\nu}dx^\mu dx^\nu = -\left(1 - \frac{2GM}{c^2 r}\right) dt + \left(1 - \frac{2GM}{c^2 r}\right)^{-1} \gamma_{ij} dx^i dx^j$$

$$\alpha \sim 1 - \mathcal{O}(M/r)$$



$$g_{\mu\nu}dx^\mu dx^\nu = -\alpha^2 dt^2 + \gamma_{ij}(dx^i - \beta^i dt)(dx^j - \beta^j dt)$$

$$g_{\mu\nu}dx^\mu dx^\nu = -\left(1 - \frac{2GM}{c^2 r}\right) dt + \left(1 - \frac{2GM}{c^2 r}\right)^{-1} \gamma_{ij} dx^i dx^j$$

$$\beta^R \equiv \sqrt{(\beta^x)^2 + (\beta^y)^2 + (\beta^z)^2}$$

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