

# LinearRegression

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[ ]: #Import libraries
import autograd.numpy as np
from autograd import grad
import matplotlib.pyplot as plt

[ ]: def linear(x,a,b): #creating a definition named "linear" with "x" , "a" , and
    ↪ "b" variables
    return a*x+b ##returns the equation  $y(x) = m*x+b$  or in this case  $y(x) =$ 
    ↪  $a*x+b$ 

def loss(x,y_obs,a,b): #creating a definition named "loss" with "x" , "y_obs" ,
    ↪ "a" and "b" variables
    y_model = linear(x,a,b) #creating a variable "y_model" that returns the
    ↪ linear definition (the slope formula)
    return np.sum( (y_model-y_obs)**2 ) #This is the SSR function that is
    ↪ returned in the "loss" definition

x = np.array( [0,1,2,3,4,5,6,7,8,9,10] ) #Array of numbers for the x
    ↪ coordinates (in an array)
y_obs = np.array( [0,1.1,1.9,3.2,3.8,5.1,6.3,6.9,8.5,8.5,10.2] ) #Array of
    ↪ numbers for the y_obs coordinates (in an array)

a,b = 2.0, 1.0 #Creating stagnant "a" and "b" variables (guesses)
y_model = linear(x,a,b) #Creating a "y_model" variable using the linear
    ↪ defintion with the already defined "x" , "a" , and "b" variables

print('First guess at a and b are ',a,b) #prints the a and b variables
print('First loss function is ',loss(x,y_obs,a,b)) #prints the SSR function
    ↪ using the defined "a", "b" and the "x" and "y_obs" arrays

d_by_da = grad(loss,2) #create the derivative/gradient function of "loss" -->
    ↪ called d_by_da, (equation(loss), index=2 (a))
d_by_db = grad(loss,3) #create the derivative/gradient function of "loss" -->
    ↪ called d_by_da, (equation(loss), index=3 (b))
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#Learning rate gives the rate of speed where the gradient moves during gradient
↳descent. Setting it too high would make your path instable,
#too low would make convergence slow. Put it to zero means your model isn't
↳learning anything from the gradients.
learning_rate = 0.0001 #controls the magnitude of the vector update (positive
↳number that moves the starting point by a very small number)
maximum_number_of_iterations = 1000 #number of iterations given

ssr = [] #Sum of Square Residuals -> The lower it is the better it fits the
↳linear model

#Iteratively updates according to the learning rate and the value(s) of the
↳gradient

for iter in range(maximum_number_of_iterations):
    #We are finding new "a" (slope) and "b" (intercept) variables for 1000
↳iterations.
    a -= learning_rate*d_by_da(x,y_obs,a,b) #(-=) subtracts the value of the
↳expression on the right-hand side from the value on the left-hand side and
↳then assigns the result to the left hand side variable.
    #We are changing the slope for every iteration and saving the new slope off
↳as the new "a".
    b -= learning_rate*d_by_db(x,y_obs,a,b) #(-=) subtracts the value of the
↳expression on the right-hand side from the value on the left-hand side and
↳then assigns the result to the left hand side variable.
    #We are changing the intercept for every iteration and saving the new slope
↳off as the new "b".
    y_model = linear(x,a,b) #Creates our y_model with our "a" and "b" and the
↳array of "x" values
    ssr.append(loss(x,y_obs,a,b)) #adds to the empty array list above of all of
↳the SSR generated from the current "a" and "b".

print('Best a and b are ',a,b) #outputs the "a" and "b" variable that gives the
↳SSR value
print('Best loss function is ',loss(x,y_obs,a,b)) #outputs the best SSR value

plt.subplot(1,2,1) #creates 2 plots with this plot being the 1st one shown
plt.scatter(x,y_obs) #puts the "x" and "y_obs" values from the arrays on the
↳graphs
plt.plot(x,y_model) #plots the best y_model for the linear regression

plt.subplot(1,2,2) #creates 2 plots with this plot being the 1st one shown
plt.plot(ssr) #creates a graph of all the calculated SSR values

plt.show() #outputs the graphs

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