Outer Joins

The joins you know from RA

These can go in a FROM clause:

Expression	Meaning
`R, S`	$R \times S$
`R cross join S`	
`R natural join S`	$R \bowtie S$
`R join S on Condition`	$R \bowtie_{condition} S$

In practise, natural join is brittle

- A working query can be broken by adding a column to a schema.
  - Example:

```
SELECT sID, instructor
FROM Student NATURAL JOIN Took
             NATURAL JOIN Offering;
```

  - What if we add a column called `campus` to `Offering`?
- Also, having implicit comparisons impairs readability.
- Best practise: Don't use natural join.

Dangling tuples

- With joins that require some attributes to match, tuples lacking a match are left out of the results.
- We say that they are "dangling".
- An outer join preserves dangling tuples by padding them with `NULL` in the other relation.
- A join that doesn't pad with `NULL` is called an inner join.

Three kinds of outer join

- `LEFT OUTER JOIN`
  - Preserves dangling tuples from the relation on the LHS by padding with nulls on the RHS.
- `RIGHT OUTER JOIN`
  - The reverse.
- `FULL OUTER JOIN`
  - Does both.

Example: joining R and S various ways

R

A	B
1	2
4	5

S

B	C
2	3
6	7

R NATURAL JOIN S

A	B	C
1	2	3

Example

R

A	B
1	2
4	5

S

B	C
2	3
6	7

R NATURAL FULL JOIN S

A	B	C
1	2	3
4	5	NULL
NULL	6	7

Example

R

A	B
1	2
4	5

S

B	C
2	3
6	7

R NATURAL LEFT JOIN S

A	B	C
1	2	3
4	5	NULL

Example

R

A	B
1	2
4	5

S

B	C
2	3
6	7

R NATURAL RIGHT JOIN S

A	B	C
1	2	3
NULL	6	7

Summary of join expressions

Cartesian product

```
A CROSS JOIN B
```

same as `A,B`

Theta-join

```
A JOIN B ON C
```

✓`A {LEFT|RIGHT|FULL} JOIN B ON C`

Natural join

```
A NATURAL JOIN B
```

✓`A NATURAL {LEFT|RIGHT|FULL} JOIN B`

✓ indicates that tuples are padded when needed.

Keywords INNER and OUTER

- There are keywords `INNER` and `OUTER`, but you never need to use them.
- Your intentions are clear anyway:
  - You get an outer join iff you use the keywords `LEFT`, `RIGHT`, or `FULL`.
  - If you don't use the keywords `LEFT`, `RIGHT`, or `FULL` you get an inner join.

Impact of having null values

Missing Information

- Two common scenarios:
  - Missing value.
    E.g., we know a student has some email address, but we don't know what it is.
  - Inapplicable attribute.
    E.g., the value of attribute spouse for an unmarried person.

Representing missing information

- One possibility: use a special value as a placeholder. E.g.,
  - If age unknown, use 0.
  - If StNum unknown, use 999999999.
- Implications?
- Better solution: use a value not in any domain. We call this a null value.
- Tuples in SQL relations can have `NULL` as a value for one or more components.

Checking for null values

- You can compare an attribute value to `NULL` with
  - `IS NULL`
  - `IS NOT NULL`
- Example:

```
SELECT *
FROM Course
WHERE breadth IS NULL;
```

In SQL we have 3 truth-values

- Because of `NULL`, we need three truth-values:
  - If one or both operands to a comparison is `NULL`, the comparison *always* evaluates to `UNKNOWN`.
  - Otherwise, comparisons evaluate to `TRUE` or `FALSE`.

Combining truth values

- We need to know how the three truth-values combine with `AND`, `OR` and `NOT`.
- Can think of it in terms of the truth table.
- Or can think in terms of numbers:
  - `TRUE` = 1, `FALSE` = 0, `UNKNOWN` = 0.5
  - `AND` is min, `OR` is max,
  - `NOT` x is (1-x), i.e., it "flips" the value

The three-valued truth table

A	B	A and B	A or B
T	T	T	T
TF or FT		F	T
F	F	F	F
TU or UT		U	T
FU or UF		F	U
U	U	U	U

Thinking of the truth-values as numbers

A	B	as nums	A and B	min	A or B	max
T	T	1, 1	T	1	T	1
TF or FT		1, 0	F	0	T	1
F	F	0, 0	F	0	F	0
TU or UT		1, 0.5	U	0.5	T	1
FU or UF		0, 0.5	F	0	U	0.5
U	U	0.5, 0.5	U	0.5	U	0.5

Thinking of the truth-values as

A	as a num, x	not A	1 - x
T	1	F	0
F	0	T	1
U	0.5	U	0.5

Surprises from 3-valued logic

- Some laws you are used to still hold in three-valued logic. For example,
  - `AND` is commutative.
- But others don't. For example,
  - The law of the excluded middle breaks: `(p or (NOT p))` might not be `TRUE`!
  - `(0*x)` might not be `0`.

Impact of null values on WHERE

- A tuple is in a query result iff the WHERE clause is `TRUE`.
- `UNKNOWN` is not good enough.
- "WHERE is picky."
- Example: where-null

Impact of null values on aggregation

- Summary: Aggregation ignores `NULL`.
  - `NULL` never contributes to a sum, average, or count, and
  - can never be the minimum or maximum of a column (unless *every* value is `NULL`).
- If there are no *non*-`NULL` values in a column, then the result of the aggregation is `NULL`.
  - Exception: `COUNT` of an empty set is 0.

Aggregation ignores nulls

	some nulls in A	All nulls in A
`min(A)`	ignore the nulls	null
`max(A)`		
`sum(A)`		
`avg(A)`		
`count(A)`		0
`count(*)`	all tuples count	

Example: aggregation-nulls

More re the impact of null values

- Other corner cases to think about:
  - `SELECT DISTINCT`: are 2 `NULL` values equal?
  - natural join: are 2 `NULL` values equal?
  - set operations: are 2 `NULL` values equal?
- And later, when we learn about constraints:
  - `UNIQUE` constraint: do 2 `NULL` values violate?

- This behaviour may vary across DBMSs.

Summary re NULL

- Any comparison with `NULL` yields `UNKNOWN`.
- `WHERE` is picky: it only accepts `TRUE`.
- Therefore `NATURAL JOIN` is picky too.
- Aggregation ignores `NULL`.
- In other situations where `NULL`s matter
  - when a truth-value may be `NULL`
  - when it matters whether two `NULL` are considered the same

Don't assume. Behaviour may vary by DBMS.