

An image-computable spatio-chromatic receptive  
field model of the midget retinal ganglion mosaic  
across the retina

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**Abstract**

Image-computable models of retinal ganglion cell (RGC) mosaics that are synthesized and constrained jointly by optical, anatomical and physiological properties, and which operate on images defined by their spatial-spectral radiance, do not currently exist. Here, we deploy a novel computational framework which synthesizes mosaics of linear spatio-chromatic receptive fields (RFs) of ON midget RGCs (mRGCs) by integrating published anatomical, physiological, and optical quality measurements, all varying with eccentricity. We use the synthesized mRGC mosaics to simulate both *in vivo* and *in vitro* physiological experiments and demonstrate the model's consistency with published data. The model enables computation of how visual performance is shaped by the representation of visual information provided by the linear spatiochromatic processing stage of midget RGCs. The developed computational framework carefully accounts for the effect of physiological optics on mRGC responses, enables comparison of *in vivo* and *in vitro* data, and allows exploration of how different assumptions about RF organization, such as selectivity for the type of cones pooled by the RF center mechanism, affect physiological responses and psychophysical performance. The open-source and freely available implementation provides a platform for understanding how the linear spatiochromatic receptive field representation of the mRGCs shapes visual performance, as well as a foundation for future work that incorporates response nonlinearities, temporal filtering, and extends to additional RGC mosaics.

**Keywords:** retinal ganglion cells, receptive field, model

047 **1 Introduction**

048

049 An important aim in computational visual neuroscience is to create accurate computer  
050 simulations of how neurons in the visual pathways encode and respond to visual scenes.  
051 These simulations, often called digital twins, are a quantitative description of the  
052 visual system. They enable links between the neural representation and perception  
053 and provide a tool for evaluating the effects of blinding disease and its treatment.

054 Over the last ten years we have built an open-source software platform, ISETBio  
055 (Image Systems Engineering Tools for Biology) [1], which serves as a digital twin for  
056 the initial stages of the human visual system. Previously, we described how ISETBio  
057 models (a) the formation of the retinal image, (b) the excitation of the cone pho-  
058 toreceptors, (c) phototransduction, and (d) fixational eye movements [2–4]. We and  
059 others have employed ISETBio to model human vision, including sensitivity to spa-  
060 tial contrast [2, 3], the impact of chromatic aberration on acuity [5], the encoding of  
061 information from natural images captured by cones [6], the effects of optics and cone  
062 density across the visual field on performance [7], and the influence of initial visual sig-  
063 nals on tasks like judging surface properties and lighting [8, 9]. We also used ISETBio  
064 to help interpret experimental measurements of retinal ganglion cells [10].

065 Here, we describe an extension of ISETBio which models the mosaic of a class of  
066 retinal ganglion cells (RGCs), the midget RGC (mRGC) mosaic. RGCs are the only  
067 pathway for information transmission from the retina to the brain, and their properties  
068 surely impact visual performance on many tasks. The spike trains transmitted via the  
069 axons of one million RGCs that form the human optic nerve, represent the signals  
070 from roughly 6.5 million cones and 110 million rods [11, 12]. Of these RGCs, mRGCs  
071 are a particularly important subtype, comprising 80% of the perifoveal RGCs and  
072 45% of the peripheral RGCs. In the very central fovea, it has been estimated that the  
073 mRGCs are 95% of the RGC population [13].

074 The role of the mRGCs in limiting spatial and color vision is still debated [14].  
075 Simulation of performance using image computable models of the mRGC mosaic offers  
076 a powerful tool for understanding the visual information encoded by these cells, espe-  
077 cially because they are very hard to measure and isolate experimentally. We have four  
078 primary goals for this human retina model.

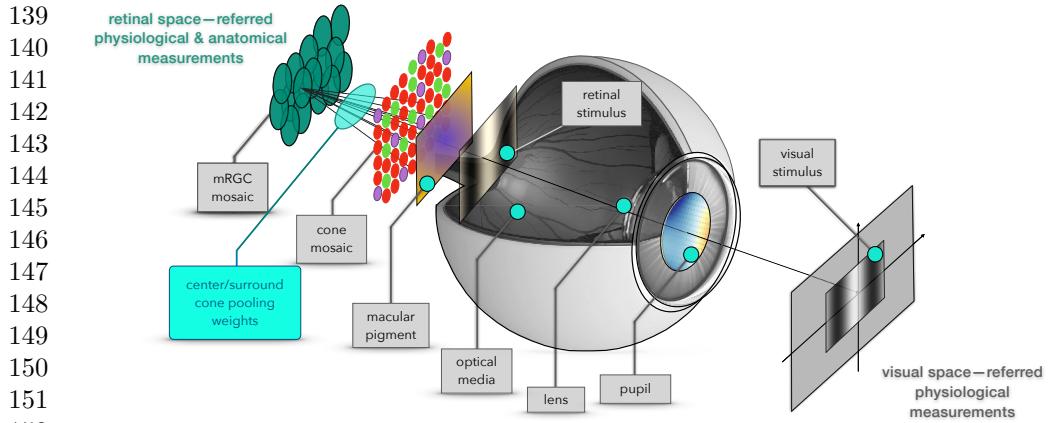
079 First, the model must distinguish the contributions of the eye’s optics and pho-  
080 toreceptors from the subsequent post-receptoral retinal circuitry. This separation is  
081 crucial for incorporating key physiological measurements, some of which are made *in*  
082 *vitro* without the eye’s optics. Failing to isolate the optical effects would prevent us  
083 from using this vital collection of data.

084 Second, the model must capture responses across a large portion of central  
085 retina. This is important because we and others are interested in how the retinal  
086 representation shapes performance not just in the fovea but also for peripheral viewing.

087 Third, the model must integrate diverse data types, including optical, anatomical,  
088 and physiological measurements. A comprehensive formulation is necessary because  
089 retinal ganglion cell (RGC) responses are shaped by all three of these factors.

090 Fourth, we aim for an extensible framework. The current implementation uses a  
091 linear spatiochromatic receptive field, which serves as a good initial approximation.  
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The framework is designed to incorporate future extensions—such as response non-linearities, temporal dynamics, and additional RGC classes—to improve the model’s accuracy over time. The following points describe how our implementation achieves these goals.	093
1. <i>Separating representations.</i> Our mRGC model operates on the cone mosaic signals. This design isolates the post-receptoral circuitry (cone-to-mRGC), which is the pathway measured in <i>in vitro</i> experiments where the eye’s optics are removed [15, 16]. This separation is also valuable for interpreting experiments that use adaptive optics to eliminate optical blur [10]. While the components are separable, our implementation integrates the optics, cone sampling, and mRGC circuitry into a complete, image-computable pipeline. This full pathway allows us to simulate the transformation of a visual stimulus into an mRGC response, matching the conditions of <i>in vivo</i> measurements [17–19] and enabling predictions of human performance under natural viewing conditions.	094
2. <i>Representation across the visual field.</i> Visual performance varies across the visual field, and a key contribution of our model is that it allows computation of the mRGC representation continuously across the retina from the fovea out to 30°, along any meridian. Achieving this goal required implementation of novel algorithms for synthesizing mRGC RF mosaics.	095
3. <i>Multiple data types.</i> By explicitly representing different biological stages, our model enables algorithms that combine anatomical, physiological, and optical data. Incorporation of multiple types of measurements from the literature is critical because at present no one type of data sufficiently constrains mRGC properties across the visual field.	096
4. <i>Extensible.</i> The current implementation is a linear spatial pooling model, a useful approximation for stimuli with modest contrast. The software’s modular design provides a foundation for future extensions. We can incorporate known nonlinear properties that shape mRGC responses, including phototransduction effects [20]; spatial and static nonlinearities, which often differ between ON and OFF pathways [21–24]; temporal dynamics [25]; and response noise [26]. Furthermore, the mRGC model is a suitable base for developing models of other types of RGCs, such as parasol and bistratified cells [27].	097
<b>1.1 Model overview</b>	098
Fig. 1 provides a model overview. Computation begins with the image spatial-spectral radiance, such as produced by a calibrated monitor. A model of the human optics (including chromatic aberrations) and spectral filtering by the lens is used to compute the retinal irradiance. Retinal irradiance is spectrally filtered by the macular pigment and then spatially and spectrally sampled by the cone photoreceptor mosaic. The parameters of the optics, macular pigment and cone mosaic all vary across the visual field, according to measurements in the literature [2].	099
The mRGC mosaic extension is composed of spatial receptive fields (RFs) whose center and surround responses are weighted sums of signals from the cone mosaic.	100
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**Fig. 1 Model overview.** The extant ISETBio model computes the mosaic of cone excitations. The model mRGCs are obtained by connecting their RF center and surround subregions to the cone mosaic. The connectivity matrix is constrained by anatomy and optimized through forward simulation of physiological measurements, so that the synthetic mRGCs are consistent with optical, anatomical and physiological data across the visual field.

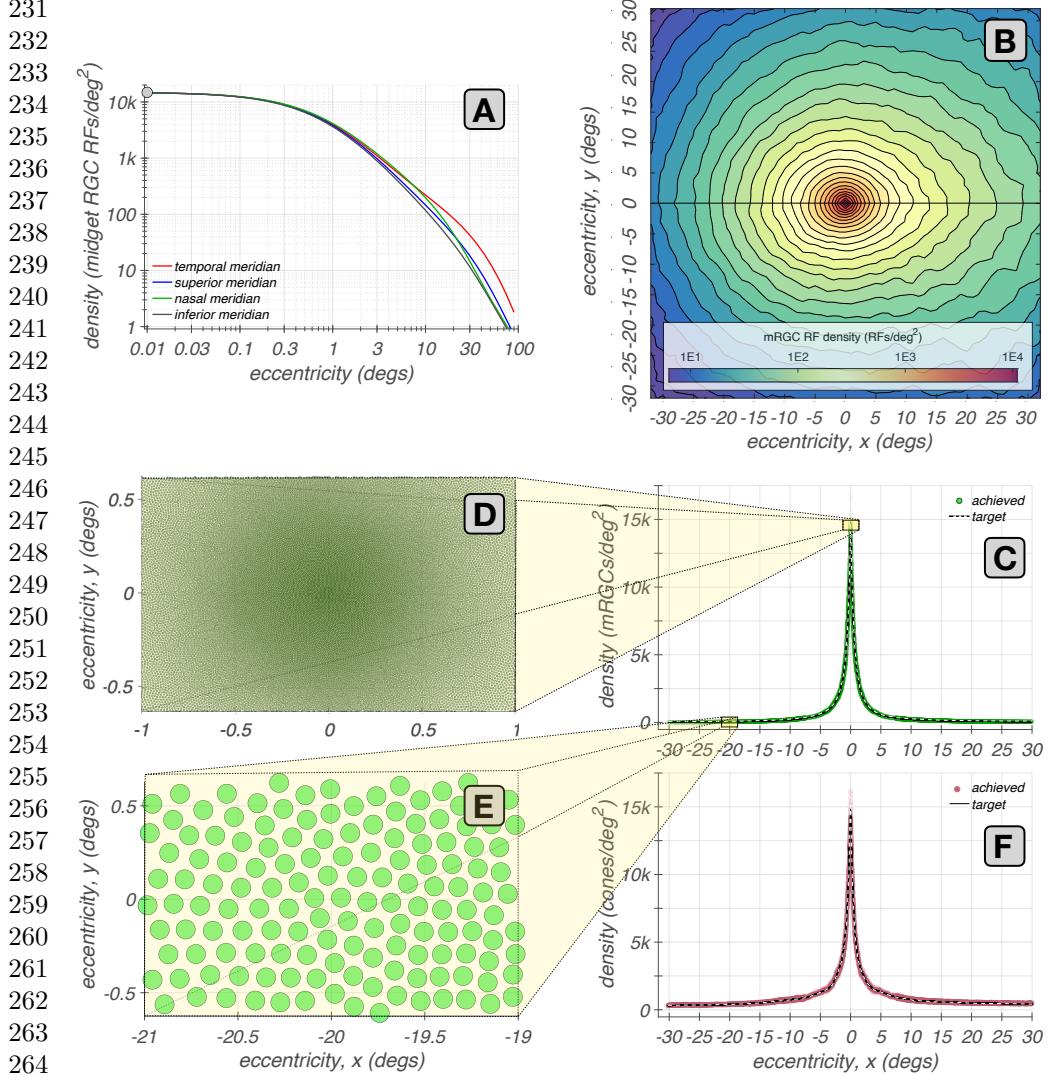
The wiring between the input cone mosaic and the mRGC mosaic is initially determined based on anatomical constraints, such as cone and mRGC densities, and is subsequently refined using optimization algorithms that align the model's spatial RF properties with physiological measurements.

A key challenge is the scarcity of *in vitro* physiological data across the visual field which could be used to directly determine the wiring between the two mosaics. To address this, our framework primarily leverages more widely available *in vivo* data to derive the wiring, while validating the synthesized model against *in vitro* data where it exists. The resulting model is simultaneously consistent with cone light encoding, anatomical properties (including those of mRGCs and H1 horizontal cells), and both *in vitro* and *in vivo* physiological data. This makes the model versatile for simulating visual stimulation under *in vivo*, *in vitro*, and adaptive optics paradigms.

### 1.1.1 Relationship to previous computational models of RGCs

To our knowledge, no previous model of RGCs has attempted to realistically capture the effects of the front end encoding in the visual system, specifically the eccentricity and wavelength-varying nature of physiological optics, and the eccentricity-varying spatio-chromatic properties of the cone mosaic. Instead previous models of RGCs have either completely ignored the impact of physiological optics [28, 29], or employed very simplistic models of the eye's optics [30]. Moreover, previous RGC models were designed to either operate directly on visual space, ignoring the spatio-spectral filtering by the tri-chromatic cone mosaic [28], or have employed simplistic implementations of the cone mosaic [30]. Finally, none of the previous models are constructed to operate on stimuli defined in terms of their physical spatial-spectral radiance, as they are designed

to operate on light intensity defined stimuli [28, 30]. As such, previous models can not capture the rich spatio-chromatic interactions between stimuli and physiological optics, and how their combined effects shape RGC responses. Indeed, we have recently shown that the spatio-chromatic interactions between stimuli and physiological optics can have profound effects of the response properties of midget ganglion cells [31].	185 186 187 188 189
On the other hand, previous computational models of RGCs have focused on other, also important, components of the RGC circuit, that our linear spatio-chromatic model does not currently address, such as processing by retinal interneurons [28–30, 32], temporal dynamics [28–30, 32], contrast grain control [28, 33], and spike generation [28, 29, 33]. We plan to extend our linear spatiochromatic model of mRGCs to include several of these components, as described in section 4.2.2.	190 191 192 193 194 195 196
<b>1.1.2 Paper organization</b>	197
The remainder of this paper is organized as follows.	198 199
• In section 2 we describe the model’s construction stages, including, how the mRGC receptive field lattice is generated from anatomical data (section 2.1), how cones get connected to the mRGC RF centers using anatomical and physiological constraints (section 2.2), and how cone connections to mRGC RF surrounds are derived by optimizing against <i>in vivo</i> data (section 2.3).	200 201 202 203 204
• In section 3 we present, validate, and discuss first applications of the model. Specifically, we illustrate examples of synthesized mRGC mosaics (section 3.1), confirm that the model mRGC spatial RFs are consistent with <i>in vivo</i> (section 3.2), and <i>in vitro</i> data (section 3.3), demonstrate the significant impact of physiological optics (section 3.4), and how simpler Difference-of-Gaussians models can fail to capture the true surround pooling (section 3.5), and finally we illustrate how the model can be used to estimate the contribution of the mRGC mosaic to spatiochromatic contrast sensitivity across the visual field (section 3.6).	205 206 207 208 209 210 211 212
• In section 4, we summarize our work, discuss ongoing applications of the model in its current stage, and discuss the model’s present limitations and planned expansions.	213 214 215
<b>2 Methods</b>	216 217
The synthesis of mRGC RF mosaics occurs in three stages. In the first stage, we generate spatial lattices representing the RF centers of cells in the mRGC mosaic and the position of cones in the cone mosaic that provides the input to the mRGC mosaic. In the second stage, we connect the input cone mosaic to the RF centers of the mRGC mosaic. In the third stage, we connect the input cone mosaic to the RF surrounds of the mRGC mosaic.	218 219 220 221 222 223 224
<b>2.1 Generating the spatial position lattice of mRGC RF centers (Stage 1)</b>	225 226 227
We begin by generating a lattice that represents the $(x, y)$ positions of mRGC RF centers. This process comprises three sub-stages, components of which are illustrated in Fig. 2.	228 229 230



266 **Fig. 2 Eccentricity-varying mRGC RF position lattices.** **A:** Meridian density functions of  
267 mRGC RFs [34]. **B:** Two-dimensional mRGC RF density map obtained by interpolating the four  
268 meridian density functions. **C:** Achieved and target densities of mRGC RF centers along the horizontal  
269 meridian (green disks and white dashed line, respectively). **D & E:** Examples of  $2^\circ \times 1^\circ$  mosaics  
270 of mRGC RF centers at eccentricities of  $0^\circ$  and  $20^\circ$  along the temporal meridian, respectively. **F:**  
271 Achieved and target densities of cones along the horizontal meridian (maroon disks and white dashed  
272 line, respectively).

273 • **Stage 1A:** We estimate the mRGC RF center densities along the four principal  
274 meridians ( $0^\circ$ ,  $90^\circ$ ,  $180^\circ$ , and  $270^\circ$ ). These estimates are based on human data  
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[34, 35]. We take the ON mRGC density to be half of the total mRGC density, ignoring the possible density differences between ON and OFF mRGCs. The meridian functions are depicted in Fig. 2A.

- **Stage 1B:** We generate a continuous, two-dimensional map representing the mRGC RF density map, depicted in Fig. 2B. This map is created by linearly interpolating the meridian estimates, and it serves as a target for the lattice synthesis algorithm in the next stage.
- **Stage 1C:** We synthesize a sampling lattice that represents the  $(x, y)$  positions of the mRGC RF centers. The lattice is created using the iterative algorithm that we introduced in earlier work [2] for generating cone mosaics, replacing the two-dimensional cone density map with the target mRGC RF density map. A typical lattice of mRGC RF positions is obtained after about 1,300 iterations and has a density that varies smoothly over space, matching the target density, as illustrated in Fig. 2C. Example patches of mRGC RF center mosaics synthesized at eccentricities of  $0^\circ$  and  $20^\circ$  along the temporal horizontal meridian, are depicted in Figs. 2D & 2E, respectively.

The same procedure is used to generate the lattice that represents the  $(x, y)$  positions of cones, but, in this case, using the meridian densities of cone photoreceptors in human retina [36] as targets. The density of cones in the synthesized cone lattice also varies smoothly over space and matches closely the target cone density, as illustrated in Fig. 2F.

## 2.2 Connecting cones to mRGC RF centers (Stage 2)

The connections between cones and mRGC centers are constrained by (1) anatomical data across the retina, specifically, the ratio of densities of mRGC RF centers to cones [34], and (2) *in-vitro* physiological data from peripheral retina, that (a) indicate that, unlike OFF-center mRGCs, which draw indiscriminately from all three cone types [15, 37, 38], ON-center mRGCs draw only from L- and M-cones, and (b) quantify the degree of RF center overlap between neighboring mRGCs [39]. The connectivity between the cone mosaic and the RF centers of the ON mRGC mosaic is established in 3 sub-stages, summarized here.

- **Stage 2A:** In the first substage, each L- and M-cone in the input cone mosaic gets connected to a single mRGC RF center; an mRGC RF center can receive input from more than one cone. At this substage, each connected cone has unit connection weight. S-cones are not connected because they do not contribute to ON-center mRGCs. This initial cone-to-RF center connectivity often results in inhomogeneities in the composition of neighboring mRGCs RF centers, which are dealt with in the next stage. Algorithmic details regarding this substage are provided in Supplemental Section A.1.
- **Stage 2B:** This substage refines the center connections to establish a balance between the spectral purity and spatial compactness of the mRGC RF centers, which is quantified by a single parameter,  $\phi$ . For the body of this work, all mRGC mosaics are generated by maximizing spatial compactness, but the option to maximize spectral purity allows testing of different scenarios where mRGC RF centers

323 may be biased to some extent towards cone type selective pooling [15, 16]. At this  
324 substage, connected cones retain their unit connection weights. Algorithmic details  
325 regarding this substage are provided in Supplemental Section A.2.  
326 • **Stage 2C:** Finally, the mutual exclusivity constraint enforced in substages 2A and  
327 2B is lifted, and single cones are permitted to connect to multiple nearby mRGC RF  
328 centers. The extent of divergence varies with retinal eccentricity, being minimal in  
329 the fovea and increasing towards the periphery to match experimental observations  
330 [39]. This is done by varying the exponent of a supra-Gaussian distribution that  
331 describes the spatial weighting profile of cone connections to the RF centers which  
332 at this substage become non-binary. Algorithmic details regarding this substage are  
333 provided in Supplemental Section A.3.

334 We illustrate Stage 2 by examining key properties of synthesized mRGC RF center  
335 mosaics at each of the three substages.  
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### 337 338 **2.2.1 Mosaics with convergent-only cone connections (stage 2A)**

339 Example mosaics of RF centers synthesized at four eccentricities along the temporal  
340 horizontal meridian at the end of this substage are depicted in Fig. 3, where each  
341 green ellipse represents the spatial extent of the RF center of a single mRGC. At this  
342 stage, the pooling weight of each cone is set to unit.

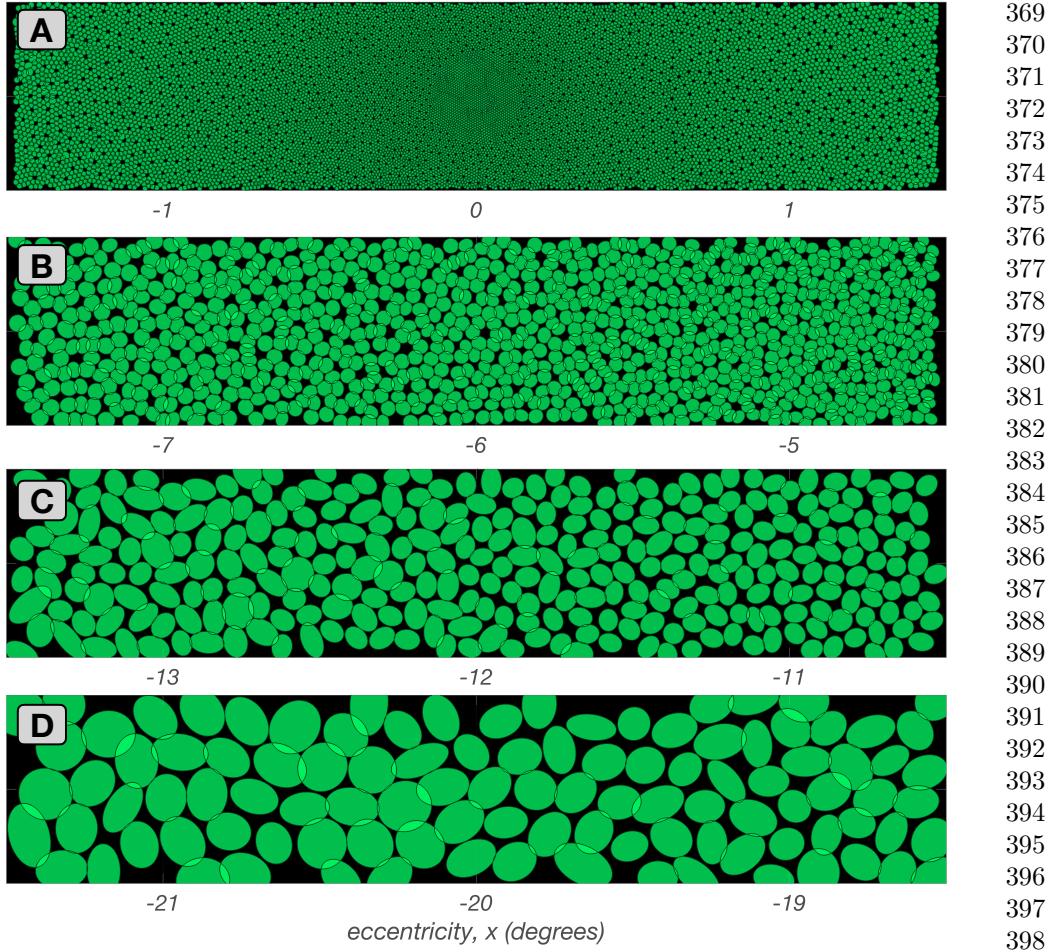
343 For the foveal mosaic depicted in Fig. 3A, RF centers connect to just a single cone.  
344 Note how RF center sizes increase as we move towards parafoveal regions to the left  
345 and right sides of Fig. 3A. This is due to the continuously increasing, with eccentricity,  
346 cone aperture in the input cone mosaic. The empty regions in this foveal mRGC RF  
347 center mosaic correspond to the location of S-cones which are not pooled by the model.

348 In the parafoveal mosaic depicted in Fig. 3B, RF centers mostly receive inputs  
349 from two cones, whereas in the more peripheral mosaics depicted in Figs 3C & 3D,  
350 RF centers connect to multiple cones. Note that the number of cones connecting to  
351 RF centers does not correspond precisely to RF center size, because cone aperture  
352 and inter-cone spacing both increase with eccentricity. At all eccentricities, however,  
353 mRGC RF center mosaics tile the retinal space with no spatial overlap or voids, except  
354 at the sparse positions where S-cones are located.  
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### 356 357 **2.2.2 Mosaics synthesized under different spatial 358 compactness/spectral purity tradeoffs (stage 2B)**

359 This substage allows for different optimizations of cone pooling within the mRGC RF  
360 centers, which is controlled by the spatial compactness/spectral purity tradeoff param-  
361 eter,  $\phi$ . At this stage, the pooling weight of each cone is still set to unit, independent  
362 of the value of  $\phi$ .

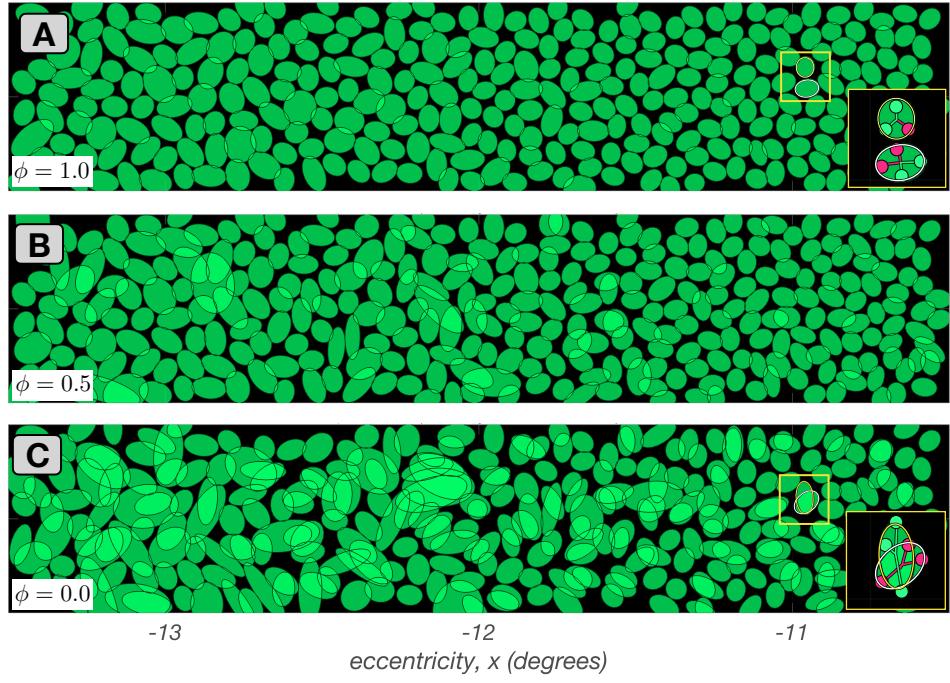
363 Fig. 4 depicts examples of mRGC RF center mosaics all synthesized at a single  
364 eccentricity ( $12^\circ$  along the temporal meridian), but under different values of  $\phi$ . The  
365 mosaic synthesized under  $\phi = 1$ , where spatial compactness is maximal and spectral  
366 purity constraint is not enforced, is depicted in Fig. 4A. Note that the RF centers  
367 tile the visual field relatively uniformly with no overlap. Figures 4B and 4C depict  
368 mosaics synthesized as  $\phi$  decreases to 0.5 and 0.0, respectively, which increasingly



**Fig. 3 Stage 2A mRGC RF mosaics.** Each panel shows a  $3.0^\circ \times 0.5^\circ$  mosaic of synthesized mRGC RF centers at a different visual field location from fovea to periphery. The green ellipses depict a spatial region that encompasses all cones pooled by single RF centers. **A:** Foveal mosaic, in which RF centers receive signals from a single L- or M-cone. **B:** Mosaic centered at  $6.0^\circ$  along the temporal horizontal meridian, in which RF centers receive signals from 2–3 L/M-cones. **C:** Mosaic centered at  $12.0^\circ$  along the temporal horizontal meridian, in which RF centers receive signals from 3–4 L/M-cones. **D:** Mosaic centered at  $20.0^\circ$  along the temporal horizontal meridian, in which RF centers receive signals from 6–9 cones.

enforces center connections to cones of the same type. Note that this occurs at the cost of reduced spatial compactness, as is evident by the increased spatial disorder and overlap in the RF centers.

By varying  $\phi$  we can examine the effect that cone-selective pooling may have on mRGC RF spatial structure, as well as on the spatio-chromatic processing in the mRGC pathway. Current electrophysiological evidence favors little selective cone pooling, i.e., a  $\phi$  value of  $\approx 1$ , in RF centers of peripheral mRGCs [15, 16, 40]. However,



**Fig. 4 Mosaics of mRGC RF centers at the end of stage 2B.** Depicted here are  $3.0^\circ \times 0.5^\circ$  mRGC mosaics, each centered at  $12^\circ$  along the temporal horizontal meridian, but synthesized under different values of tradeoff between spatial compactness and spectral purity,  $\phi$ . **A:**  $\phi = 1.0$  (maximal spatial compactness). **B:**  $\phi = 0.5$ . **C:**  $\phi = 0$  (maximal spectral purity). Insets in A and C depict pooling of cones within the RF centers of the two mRGC RF centers contained within the yellow square. The inset in C illustrates how RF center overlap and spatial disorder is introduced as the algorithm avoids cones of different types that are close to the RF center in order to maximize the spectral purity of RF centers.

the degree of cone type selectivity in more central locations is not known with as much certainty. For example, there is anatomical evidence that ON-center mRGCs in the fovea contact multiple ON-cone bipolars, as opposed to OFF-center mRGCs, which contact single OFF-cone bipolars [41], and also electrophysiological evidence that the RF centers of parafoveal mRGCs appear to be pooling from more than one cones [42]. In general, the question of whether foveal mRGCs that pool from more than one cone in the RF centers are doing so selectively remains unanswered. Our modeling approach allows exploration of the benefits and tradeoffs of cone-selective pooling at any retinal eccentricity, although we do not pursue such exploration in this paper.

### 2.2.3 Mosaics with divergent cone connections (stage 2C)

In the final substage of establishing the wiring between mRGC RF centers and the input cone mosaic, the mutual exclusivity constraint is lifted and single cones are permitted to connect to multiple nearby mRGC RF centers. This divergence of cone

connections is enabled by replacing the binary distribution of cone pooling weights in  
the mRGC RF centers with a supra Gaussian distribution, as illustrated in Fig. 5. 461  
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Fig. 5A depicts how a progressively increasing overlap in neighboring mRGC  
RF centers with eccentricity is accomplished by varying the exponent of the supra-  
Gaussian distribution. In central retina, the exponent is kept at 10, which results in  
a flat top distribution of weights with minimal overlap between neighboring RF cen-  
ters (gray histograms in the inset of Fig. 5A). As eccentricity increases beyond 7°, the  
exponent decreases, reaching a value of 2 at around 15°, which results in Gaussian  
distributions of weights and a significant overlap between neighboring RF centers (red  
histograms in the inset of Fig. 5A). 463  
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To our knowledge, there is no physiological data on the variation with eccentricity  
of the divergence of cone connections to nearby mRGC RF centers. Therefore the  
varying, with eccentricity, exponent of the supra-Gaussian distribution of cone weights  
is an arbitrary mechanism. It's intent is to capture the fact that in the fovea, input to  
mRGC RF centers comes exclusively or mostly [41, 42] from a single cone, whereas in  
the periphery, *in vitro* measurements reveal that neighboring mRGC RF centers abut  
at approximately one standard deviation of their Gaussian RF profile [39]. 471  
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The transformation of cone pooling weights from binary and mutually exclusive to  
graduated and shared is depicted in Fig. 5B for an mRGC located at an eccentricity of  
12°, with gray and blue histograms depicting the spatial distributions of cone pooling  
weights before and after, respectively, substage 2C. 478  
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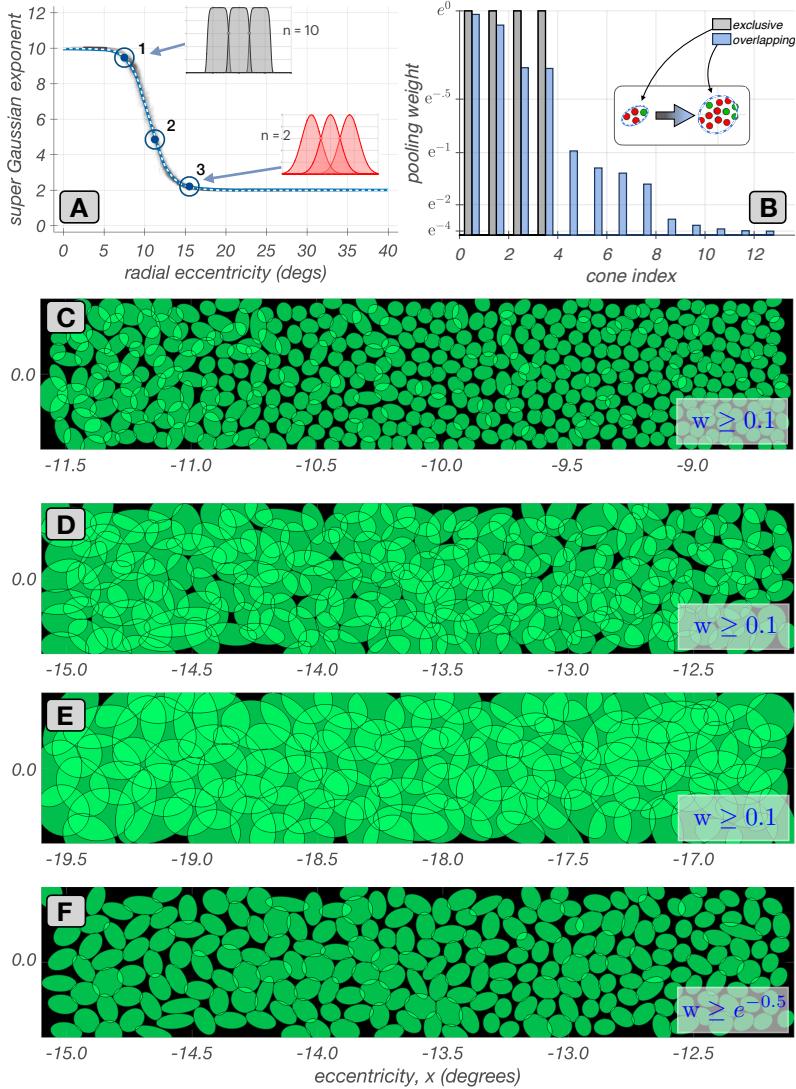
Figs. 5C–5E depict mosaics with divergent connections synthesized at three eccen-  
tricities. In these mosaic depictions, each green ellipse represents the spatial extent  
that encompasses all cones that are pooled by the RF center of a single mRGC with  
weights  $\geq 0.1$ . For the mosaic centered at 10° (Fig. 5C), divergence of cone connec-  
tions has just begun. The overlap in RF centers due to the divergence of connections  
increases as we move in eccentricity from 9° on the right side to 11°, on the left side.  
For the mosaic centered at around 13° (Fig. 5D), cone divergence and RF center over-  
lap is higher and again increases with increasing eccentricity. For the mosaic centered  
at around 18° (Fig. 5E), divergence of cone connections has assymptoted, and we have  
a constant RF center overlap. 482  
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Finally, Fig. 5F provides a visualization comparable to the visualization commonly  
reported by *in vitro* RF mapping studies [39]. It depicts the same mosaic as Fig. 5D,  
but with ellipses encompassing cones that are pooled with weights  $\geq e^{-1/2} \approx 0.67$ .  
This depiction choice makes the overlap less visually salient. 492  
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## 2.3 Connecting cones to mRGC RF surrounds (Stage 3) 497

### Overview 498

In the last stage of mRGC mosaic synthesis, we derive the cone pooling weights  
for the mRGC RF surrounds. Since there are no clear anatomical data on surround  
sizes, these weights are determined using *in vivo* characterizations of macaque mRGC  
visual space-referred spatial transfer functions, vSTF( $\omega$ ), i.e., the variation in response  
amplitude of mRGC cells as a function of stimulus spatial frequency,  $\omega$ . We use the  
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542 **Fig. 5 Mosaics of mRGC RF centers with divergent cone connections (stage 2C).**  
543 **A:** Variation with eccentricity of the exponent of the supra-Gaussian distribution of cone pooling  
544 weights in mRGC RF centers. The exponent is set to 10 in the central retina, resulting in flat top  
545 weight distributions with zero overlap (gray histograms). As eccentricity is increased, the exponent  
546 is gradually decreased, achieving a value of 2.0, at around 15° (red histograms). **B:** Transformation  
547 of cone pooling weights, from binary, in mutually exclusive connections, (gray histogram) to non-  
548 binary in shared cone connections, (blue histogram) due to the supra-Gaussian distribution for an  
549 example mRGC. Insets depict the spatial arrangement of cones that are connected with binary and  
550 non-binary weights. **C, D & E:** Mosaics at 10°, 13°, and 18°, respectively, along the temporal  
551 horizontal meridian with divergent cone connections. The RF center ellipses encompass the ensemble  
552 of cones with pooling weights  $\geq 0.1$ . **F:** Same mosaic as **C**, but with ellipses showing cones with  
553 pooling weights  $\geq e^{-0.5}$ .

measurements of Croner & Kaplan [17], who characterized vSTF( $\omega$ ) for populations of mRGCs across a wide range of eccentricities.	553 554
We incorporate these data into the model using numerical optimization. More specifically, we determine the cone-to-mRGC RF surround connections such that a forward simulation of the <i>in vivo</i> physiological experiments of Croner & Kaplan through the model best reproduces the experimental data. This approach allows us to use data collected through physiological optics, which blur the stimulus in an eccentricity and wavelength dependent manner, to determine the wiring of cones to mRGC RF surrounds across eccentricities.	555 556 557 558 559 560 561
Importantly, the optimization is achieved while adhering to the connectivity between the cone mosaic and mRGC RF centers established in stage 2. Simultaneously, the parametric form of the surrounds is constrained based on Packer & Dacey's characterizations of the spatial RF of macaque H1 horizontal cells [43], which are the main components of the linear spatial mRGC RF surrounds [44]. The use of optimization around forward simulation of an experiment to integrate data from multiple non-commensurate sources is an important innovation of our RGC modeling approach. Stage 3 proceeds in three sub-stages.	562 563 564 565 566 567 568 569
• <b>Stage 3A:</b> We begin by computing the visual space-referred cone mosaic responses to stimuli used to measure vSTFs in macaque mRGCs. This is done by presenting achromatic gratings of different spatial frequencies which are delivered to the retina through human physiological optics [45]. We use human optics as a proxy of how macaque optics would have blurred the stimuli employed by the <i>in vivo</i> characterizations of Croner & Kaplan [17], which were collected with stimuli viewed through the animal's natural optics.	570 571 572 573 574 575 576 577
• <b>Stage 3B:</b> We derive surround cone pooling functions for a subset of target synthetic mRGCs, which span the extent of the synthesized mRGC mosaic. This optimization is done so that the ensuing target cells (a) have vSTF characteristics that are well approximated by a Difference of Gaussians (DoG) model, (b) the parameters of the DoG model reasonably match the DoG model parameters reported by Croner & Kaplan at corresponding eccentricities, and (c) have surround cone pooling weights that maintain macaque H1-like spatial properties as characterized by Packer & Dacey.	578 579 580 581 582 583 584 585 586 587 588 589 590
• <b>Stage 3C:</b> We compute surround cone pooling weights for all cells in the synthesized mRGC mosaic by evaluating the derived surround cone pooling functions at the vicinity of each mRGC's input cone mosaic and subsequently interpolating the weights computed by the different pooling functions. A small amount of jitter in the ratio of the surround to center weights is added to simulate the variance in integrated surround to center ratios seen in the macaque data.	591 592 593 594 595 596 597 598

599 **2.3.1 Computation of visual space-referred cone mosaic responses**  
600 **to stimuli used to measure vSTFs in macaque mRGCs**  
601 **(Stage 3A)**

602 We employ the ISETBio machinery to compute the excitation of the input cone mosaic  
603 to achromatic gratings of different spatial frequencies delivered to the retina via phys-  
604 iological optics. This process captures several crucial spatio-chromatic effects in the  
605 transformation of scene radiance into cone responses: spatial and chromatic filtering  
606 by physiological optics, spectral filtering by the eye's inert pigments, and sampling by  
607 the interdigitated trichromatic cone mosaic. To mimic the phototransduction process,  
608 cone excitation responses are converted to cone modulation responses.

609 In these computations, we employ human physiological optics matched to the  
610 eccentricity of each synthesized mRGC, but we adjust the defocus term of the modeled  
611 optics so as to maximize the Strehl ratio. The Strehl ratio is defined as the ratio of peak  
612 sensitivity of the optical point spread function (PSF) at the wavelength of focus, here  
613 550 nm, to the peak sensitivity of a diffraction-limited PSF. This is done as a proxy to  
614 the experimental paradigm of Croner & Kaplan, in which corrective lenses were used  
615 to maximize cell responses at high spatial frequencies (personal communication with  
616 the late Ehud Kaplan).

618 **619 2.3.2 Deriving surround cone pooling functions for a subset of**  
620 **target synthetic mRGCs (Stage 3B)**

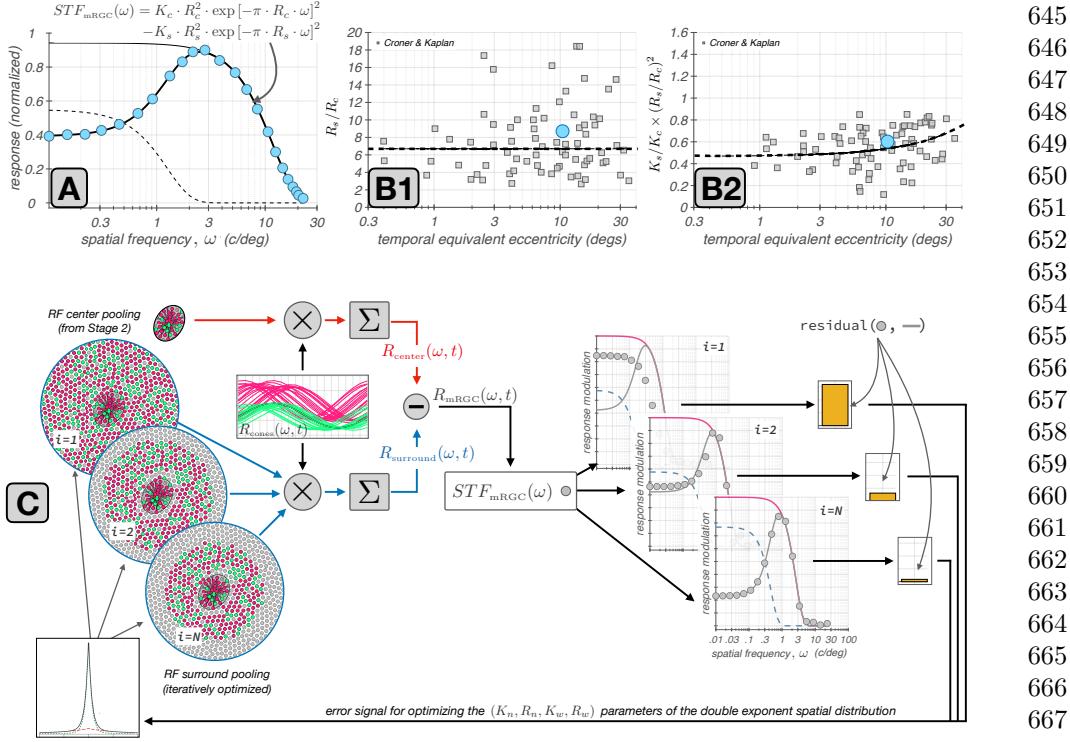
621 Croner & Kaplan reported summaries of the spatial RF characteristics across pop-  
622 ulations of mRGCs by measuring their vSTF and then fitting a DoG model to the  
623 measured vSTF. The DoG model defined in spatial frequency,  $\omega$ , domain is given by:

625 
$$\text{DoG}(\omega) = K_c \cdot R_c^2 \cdot \exp[-\pi \cdot R_c \cdot \omega]^2 - K_s \cdot R_s^2 \cdot \exp[-\pi \cdot R_s \cdot \omega]^2 \quad (1)$$

627 where  $K_c$  and  $K_s$  are the peak sensitivities of the RF center and RF surround mecha-  
628 nisms, and  $R_c$  and  $R_s$  are the corresponding characteristic radii. The vSTF of a typical  
629 macaque mRGC is depicted in Fig. 6A with cyan disks. The solid heavy line depicts  
630 the fitted DoG model, with the center and surround components depicted by the thin  
631 solid and dashed lines, respectively.

632 The shape of the vSTF is determined by two key measures, the ratio of surround  
633 to center characteristic radii,  $R_s/R_c$ , and the ratio of surround to center integrated  
634 sensitivities,  $K_s/K_c \times (R_s/R_c)^2$ . The distributions of these two ratios as a function of  
635 eccentricity in the population of mRGCs recorded by Croner & Kaplan are depicted  
636 by the gray squares in Figs 6B1 & 6B2. The mean variation in these two ratios, shown  
637 as dashed lines, are the target values used to derive the surround cone pooling weights  
638 in the synthetic mRGCs.

639 The optimization process of deriving the mRGC RF surround cone pooling func-  
640 tions is illustrated schematically in Fig. 6C. The vSTF of the target synthetic mRGC  
641 is computed by forward simulation of the experiment of Croner & Kaplan. The time  
642 course of responses of L- and M-cones in the input cone mosaic to a drifting grat-  
643 ing stimulus of spatial frequency  $\omega$ ,  $R_{\text{cones}}(\omega, t)$ , (computed in Stage 3A) are depicted  
644



**Fig. 6 Derivation of cone weights to mRGC surrounds by forward simulation of the Croner & Kaplan vSTF measurements.** **A:** Typical macaque mRGC vSTF (cyan disks) fitted with a Difference of Gaussians model (thick black line). The model's center and surround components are depicted by the thin black and the dashed line, respectively. **B1 & B2:** Ratios of surround to center characteristic radii,  $R_s/R_c$ , and ratios of surround to center integrated sensitivities,  $K_s/K_c \times R_s^2/R_c^2$  as a function of eccentricity in the population of mRGCs recorded by Croner & Kaplan [17]. The dashed lines represent the trends in these two ratios as a function of eccentricity. The cyan disks depict the ratios for the example vSTF depicted in A. **C:** Depiction of the iterative estimation of surround cone pooling weights in synthetic mRGCs by forward simulation of the Croner & Kaplan vSTF measurements. See description in text for more details.

by the red and green traces in the rectangular panel of Fig. 6C. A spatially weighted sum of these cone responses using the RF center cone pooling weights (computed in Stage 2), is used to compute the response of the RF center,  $R_{\text{center}}(\omega, t)$ . This operation, which is depicted by the red computation arm in Fig. 6C, is fixed throughout the optimization of the surround.

In the computation of the spatial distribution of surround cone pooling weights, we impose a parametric form that is described by the sum of a narrow and a wide exponential spatial component, based on characterizations of the spatial RF properties of H1 horizontal cells by Packer & Dacey [43]. Specifically,

$$W_s(r) = K_{\text{narrow}} \times \exp[-r/R_{\text{narrow}}] + K_{\text{wide}} \times \exp[-r/R_{\text{wide}}] \quad (2)$$

691 where  $r$  is the radial distance from the RF center,  $K_{\text{wide}}$  and  $K_{\text{narrow}}$  are the peak sen-  
692 sitivities of the wide and the narrow components, respectively, and  $R_{\text{wide}}$  and  $R_{\text{narrow}}$   
693 are the corresponding characteristic radii.

694 Beginning with a random initial value for the parameters of the double exponential  
695 distribution, we compute an initial estimate of the surround cone weights by eval-  
696 uating  $W_s(r)$  at the vicinity of the input cone mosaic that surrounds the RF center.  
697 These weights are depicted in the top-left circular panel of Fig. 6C (labeled as  $i = 1$ ,  
698 with  $i$  denoting iteration). Using these initial weights we compute a weighted sum of  
699 the surround cone responses to derive the initial estimate of the surround response,  
700  $R_{\text{surround}}(\omega, t)$ . This operation is depicted by the blue computation arm in Fig. 6C.

701 The composite response of the synthesized mRGC is obtained by instantaneously  
702 subtracting the surround response from the center response:

703

$$704 \quad R_{\text{mRGC}}(\omega, t) = R_{\text{center}}(\omega, t) - R_{\text{surround}}(\omega, t) \quad (3)$$

705

706 The amplitude modulation of  $R_{\text{mRGC}}(\omega, t)$  is taken as the value of the synthesized  
707 cell's visual space-referred STF,  $v\text{STF}_{\text{mRGC}}(\omega)$ . Repeating over a range of spatial  
708 frequencies, we obtain the initial estimate of the full  $v\text{STF}_{\text{mRGC}}$ , which is depicted by  
709 the gray disks in the top-right rectangular panel of Fig. 6C, labeled as  $i = 1$ .

710 Following the experimental procedure of Croner & Kaplan, we fit the computed  
711  $v\text{STF}_{\text{mRGC}}(\omega)$  with a DoG model. The DoG fit is depicted by the solid gray line in  
712 the top-right rectangular panel of Fig. 6C. Note that in this procedure we constrain  
713 the DoG model fit so that its shape parameters,  $R_s/R_c$ , and  $K_s/K_c \times R_s^2/R_c^2$ , both  
714 lie within a narrow range of the mean values of  $R_s/R_c$ , and  $K_s/K_c \times R_s^2/R_c^2$  ratios  
715 reported for macaque mRGCs at corresponding eccentricities [17]. Due to this con-  
716 strain, in the first iteration the residual between the computed  $v\text{STF}_{\text{mRGC}}$  and the  
717 DoG model fit to it, is large.

718 This residual  $\|v\text{STF}_{\text{mRGC}} - \text{DoG}\|$ , depicted by the yellow bar in the right-most  
719 panel of Fig. 6C, serves as an error signal. The optimization algorithm minimizes  
720 this error signal by adjusting the parameters of  $W_s(r)$ , which controls the surround  
721 weights. This adjustment is also constrained, so that the parameters of  $W_s(r)$  remain  
722 within a range of the values reported in macaque H1 horizontal cells [43].

723 When the  $\|v\text{STF}_{\text{mRGC}} - \text{DoG}\|$  reaches a minimum value, at iteration  $i = N$   
724 in Fig. 6C, we obtain the optimized surround cone pooling function for the target  
725 synthetic mRGC. Additional details about this surround optimization method are  
726 provided in Supplemental Section B.1.

727

## 728 2.4 Deriving surround cone pooling weights for each cell in 729 the mosaic(stage 3C)

730

731 The optimization of the surround cone pooling functions is a computationally expensive  
732 process. It is therefore conducted on a sparse spatial grid (with  $N_{xy}$  nodes), which  
733 encompasses the spatial extent of the synthesized mRGC mosaic. At each node of the  
734 spatial grid, we determine the range of cone numerosities in the RF centers of nearby  
735 synthetic mRGCs, and we derive optimized surround cone pooling functions for each  
736

of the encountered RF center cone numerosities ( $N_c$ ), and we do this twice, once for L-cone dominated RF centers, and once for M-cone dominated RF centers. 737  
738

Once these  $N_{xy} \times N_c \times 2$  surround cone pooling functions are derived, we compute 739  
surround cone pooling weights for all synthetic mRGCs. For each synthetic mRGC we 740  
determine the 3 nearest spatial grid nodes, and extract the optimized surround cone 741  
pooling functions that were derived at this node for the cone numerosity that matches 742  
that of the examined mRGC, for both L- and M-center cone dominance variants. Then 743  
we evaluate the six optimized surround pooling functions at the input cone mosaic 744  
in the vicinity of the examined mRGC, deriving six sets of surround cone pooling 745  
weights. The surround cone pooling weights are determined by interpolating the 6 746  
sets of weights spatially, weighted inversely proportionally by the distance between 747  
the location of the examined mRGC and the location of the optimized model, and 748  
spectrally, weighted based on the relative L-/M-cone weight ratio in the RF center of 749  
the examined mRGC. 750  
751

#### 2.4.1 Adjusting the surround pooling variance 752

The final step in the generation of the mRGC RF surrounds is to apply a noisy scalar 753  
multiplier to all surround pooling weights of individual mRGCs. The value of this 754  
scalar is chosen so that the variance in the ratio of surround to center integrated 755  
sensitivities,  $K_s/K_c \times (R_s/R_c)^2$ , of the synthetic mRGCs matches the variance observed 756  
in the population of macaque mRGCs recorded by Croner & Kaplan at the corresponding 757  
eccentricity. The manipulation in  $K_s/K_c \times (R_s/R_c)^2$  variance does not require 758  
re-computing the surround pooling functions. This is unlike manipulating the variance 759  
in the  $R_s/R_c$  ratio, which requires re-computing the surround pooling functions. 760  
761

### 2.5 Computing mRGC responses from cone mosaic responses 762

A fully synthesized mRGC mosaic consists of two connectivity matrices:  $P_{center}(i, k)$ , 763  
determined in synthesis stage 2, and  $P_{surround}(i, k)$ , determined in synthesis stage 764  
3, which capture the weights by which the RF center and surround mechanisms, 765  
respectively, of the  $k^{th}$ - cell in the mRGC mosaic pools signals from the  $i^{th}$  cone in 766  
the input cone mosaic. 767  
768

Since the current version of the mRGC model does not contain a temporal component, 769  
the response of the  $k^{th}$  mRGC to some stimulus at time instant,  $t$ ,  $R_{stim}(k, t)$ , is 770  
computed instantaneously by weighting the response of the input cone mosaic to that 771  
stimulus at time  $t$ ,  $C_{stim}(:, t)$ , as follows: 772  
773

$$R_{stim}(k, t) = \frac{1}{\sum_{i=1}^n P_{center}(i, k)} \times \dots \\ \left( \sum_{i=1}^n P_{center}(i, k) \cdot C_{stim}(i, t) - \sum_{j=1}^m P_{surround}(j, k) \cdot C_{stim}(j, t) \right) \quad (4)$$

783 To mimic adaptation to the background stimulus, the mRGC mosaic typically operates  
784 on cone contrast responses, instead of cone excitation responses, so the  $C_{\text{stim}}(i, t)$   
785 term in the above equation is computed as follows:

786

$$787 C_{\text{stim}}(i, t) = \frac{E_{\text{stim}}(i, t) - E_{\text{bkgnd}}(i)}{E_{\text{bkgnd}}(i)} \quad (5)$$

788

789 where  $E_{\text{stim}}(i, t)$  is the excitation response of the  $i^{\text{th}}$  cone to the examined stimulus at  
790 time  $t$ , and  $E_{\text{bkgnd}}(i)$  is that cone's excitation response to a uniform field, zero con-  
791 trast stimulus, whose mean chromaticity and luminance match those of the examined  
792 stimulus.

793

### 794 3 Results

795

796 A key feature of our model is its dual representation of mRGC receptive field (RF)  
797 properties, which separates neural circuitry from optical effects. The first representa-  
798 tion, in *retinal space*, models the direct pooling of cone signals by the RF center and  
799 surround. This describes the cell's intrinsic spatio-chromatic filtering and is directly  
800 comparable to anatomical data and physiological measurements that bypass the eye's  
801 optics (e.g., *in vitro* or adaptive optics experiments [10, 46]). In contrast, the second  
802 representation, in *visual space*, models the end-to-end processing of a stimulus as it  
803 passes through the eye's optics to the mRGC mosaic. This representation is applicable  
804 to conventional *in vivo* physiology and psychophysical assessments of visual function.

805 The ability to go back and forth between cone and visual space is critical to under-  
806 standing how retinal cone pooling interacts with physiological optics to generate the  
807 processing characteristics of cells in visual space, which is what ultimately determines  
808 natural visual performance. This ability is also critical in interpreting results from *in*  
809 *vivo* physiology in terms of the underlying retinal wiring [31], as well as to relating  
810 results obtained under adaptive optics viewing conditions to results obtained under  
811 natural viewing conditions [10].

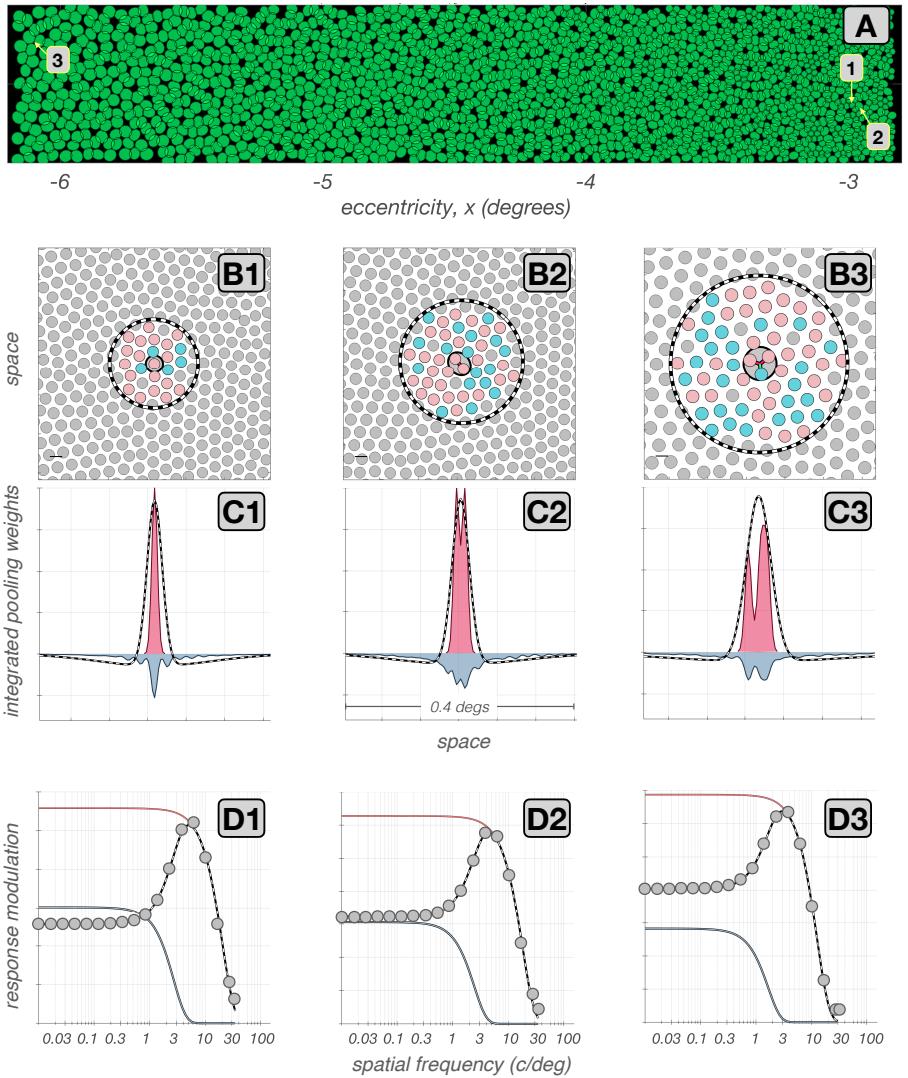
812 In this section we illustrate and contrast spatial RF characteristics of synthetic  
813 mRGCs in the two representations and validate the properties of synthetic mRGCs  
814 against those of macaque mRGCs as characterized by *in vivo* and *in vitro* physiological  
815 studies.

816

#### 817 3.1 Spatial characteristics of synthesized mRGC receptive 818 fields

819 Spatial characteristics of cells in an mRGC mosaic synthesized at  $4.5^{\circ}$  along the tem-  
820 poral horizontal meridian are depicted in Fig. 7. The employed mosaic is depicted in  
821 Fig. 7A. The numbered positions in Fig. 7A identify the locations of three selected  
822 cells whose spatial RF characteristics are explored in detail next.

823 The cone pooling maps of these exemplar mRGCs are depicted in Figs 7B1–B3.  
824 Here, pink and cyan disks depict L- and M-cones, respectively, that are pooled by  
825 the RF center with a weight  $\geq 0.1$ , or by the RF surround with a pooling weight  $\geq$   
826 0.005, and gray disks depict cones that are either not pooled at all or pooled with



**Fig. 7 Spatial RF characteristics of synthetic mRGCs** **A:** Mosaic of RF centers of an mRGC mosaic synthesized at  $4.5^\circ$  along the temporal horizontal meridian. **B1–B3:** Cone pooling maps for 3 exemplar cells whose positions within the mRGC mosaic are labeled in A. Pink and cyan disks depict L- and M-cones, respectively, with RF center pooling weights  $\geq 0.1$ , or with RF surround weights  $\geq 0.005$ . Gray disks represent either S-cones, which are not pooled in our model, or L-/M-cones with pooling weights lower than the labeling thresholds. The solid and dashed black lines depict the extents of the RF center and surround pooling regions. **C1–C3:** Y-axis integrated cone pooling weight profiles within the RF center (maroon) and RF surround (slate). The dashed lines depict the visual space-referred line weighting functions as derived by fitting Difference of Gaussians (DoG) models to each cell's vSTF. **D1–D3:** The vSTFs of the exemplar mRGCs, computed under physiological optics, are depicted by the gray disks. The gray lines depict the DoG model fits to these vSTFs, and the maroon and slate lines depict the models' center and surround components, respectively.

875 a weight less than the threshold for labeling. The solid and dashed lines depict the  
876 spatial pooling extents of the RF center and surround mechanisms, respectively.

877 The cell depicted in Fig. 7B1 is located at an eccentricity of  $3^\circ$ . Its RF center  
878 pools from a single L-cone and its RF surround pools from a total of 16 L- and M-  
879 cones. The cell depicted in Fig. 7B2, also located at  $3^\circ$ , pools from two L-cones in its  
880 RF center, and its RF surround is larger, pooling from 44 L- and M-cones. The cell  
881 depicted in Fig. 7B3 is located at  $6^\circ$ . Its RF center, which pools from 2 L-cones and 1  
882 M-cone, and its RF surround are both larger than those of the first 2 cells. The cone  
883 pooling maps depicted in Figs 7B1–B3 illustrate the spatial connectivity between the  
884 input cone mosaic and the center and surround subregions of mRGC RFs, but do not  
885 depict the strength of these connections. In this sense, these maps depict the type of  
886 information that is available from detailed anatomical studies.

887 Figs 7C1–C3 add to this view by providing information about the strength of the  
888 cone inputs for the three exemplar cells. Here, the maroon and slate histograms depict  
889 the cells' spatially integrated (along the y-axis) cone pooling weights for the RF cen-  
890 ter and the RF surround mechanisms, respectively. Note that in the cell depicted in  
891 Fig. 7C1, the double exponential spatial profile of the surround cone pooling mech-  
892 anism, with a sharp peak around the RF center and more shallow weights in peripheral  
893 regions, is prominent. In the two other cells shown, this feature is less prominent.

894 This observation, where cells with larger RF centers have less peaked surround  
895 weights than cells with smaller RF centers is seen commonly in our synthetic mRGCs.  
896 The variation in surround pooling characteristics with RF center size results from  
897 constraints in the model, which maintain vSTF shape parameters that are consistent *in*  
898 *vivo* measurements [17] while at the same time remaining consistent with the surround  
899 parametric form indicated by measurements of H1 receptive fields [43].

900 Visual space-referred spatial transfer functions are commonly measured in *in vivo*  
901 physiological assessments to estimate spatial RF properties of mRGCs [17, 18]. The  
902 vSTFs of the three examined synthetic mRGCs are depicted by the gray disks in  
903 Figs 7D1–7D3. The corresponding DoG model fits are depicted by the solid gray lines,  
904 and the spatial RF profiles corresponding to these DoG model fits are depicted by the  
905 dashed lines in Figs 7C1–C3. Contrasting these inferred spatial RF profiles with the  
906 actual cone pooling profiles, it becomes evident that one cannot use characterizations  
907 obtained under physiological optics viewing conditions to directly infer the character-  
908 istics of spatial pooling of cone signals in the retina. We discuss this issue further in  
909 later sections.

### 910 3.2 Validation against *in vivo* physiology across the visual field

911 To validate our model, we synthesized mRGC mosaics across a wide region of the  
912 retina, and computed vSTFs of individual mRGCs by probing them with drifting  
913 achromatic gratings of different spatial frequencies delivered to the retina under phys-  
914 iological optics appropriate for the eccentricity of the examined cells, simulating the  
915 experimental paradigm of Croner & Kaplan [17].

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To compare synthetic and macaque mRGCs we fitted the synthetic cell vSTFs with the DoG model employed by Croner & Kaplan and compared the ratios of surround to center characteristic radii,  $R_s/R_c$ , and ratios of surround to center integrated sensitivities,  $K_s/K_c \times R_s^2/R_c^2$ , to those reported by Croner & Kaplan. 921  
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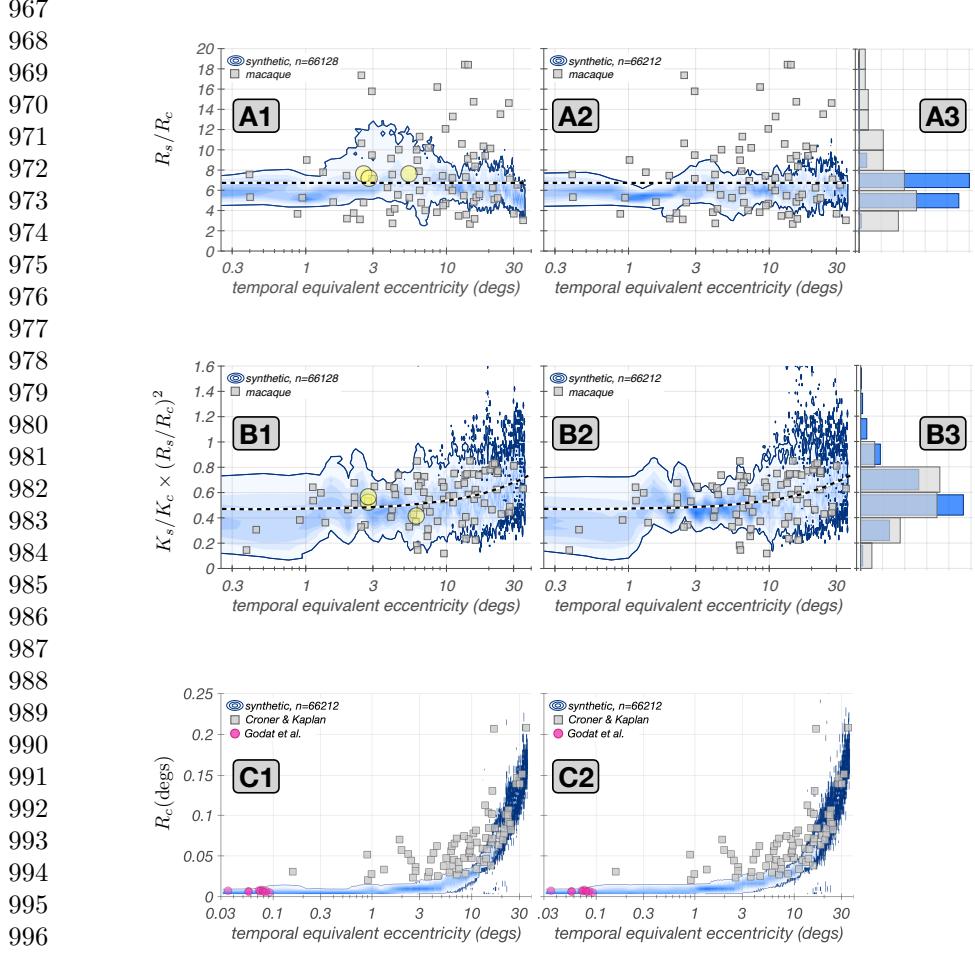
The results of this analysis are depicted in Fig. 8, in which the left and right panels depict data from mRGC mosaics synthesized under the physiological optics of two different human observers. Figs. 8A1 and 8A2 compare macaque vs. synthetic mRGCs in terms of the distribution of their  $R_s/R_c$  ratios. Gray squares depict the macaque mRGC data and the blue density plots depict the 5%–95% percentile range of the  $R_s/R_c$  ratios in a population of 66,128 synthetic mRGCs. The three yellow disks in Fig. 8A1 correspond to the three exemplar cells illustrated in Fig. 7. Note that the  $R_s/R_c$  ratios in synthetic mRGCs follow the macaque data across eccentricity for both human subjects. The synthetic data do not, however, capture the full variance seen in the macaque data, as is evident by the marginal histograms (Fig. 8A3). To capture the full variance seen in the macaque data, we could consider synthesizing multiple surround pooling functions, each with different target values of  $R_s/R_c$ , and then randomly selecting for each synthesized mRGC from the multiple sets. 925  
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On the other hand, the integrated sensitivity ratios,  $K_s/K_c \times R_s^2/R_c^2$ , of the synthetic mRGC population, depicted in Figs 8B1–B3, capture both the trend with eccentricity and the variance of the macaque data. The variance match was achieved by enforcing a target variance in the  $K_s/K_c \times R_s^2/R_c^2$  ratio of the synthetic cells as described earlier. 938  
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Note that, although we did use the mean variation with eccentricity of macaque  $R_s/R_c$  and  $K_s/K_c \times R_s^2/R_c^2$  ratios during construction of the model, the model was derived using additional constraints: those imposed by the densities of cones and mRGC RFs, by the spatial characteristics of H1 horizontal cells, and by the influence of human optics. These validations, therefore, check both that we have not over constrained our model in a manner that makes it inconsistent with the macaque data, and that our method of interpolating surround pooling weights from models derived at a set of discrete retinal locations works well. 943  
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We next examined the correspondence between synthetic and macaque mRGCs in terms of their visual space-referred RF center sizes,  $R_c$ . Recall that in synthesizing mRGC mosaics, the RF centers are constructed independently of the Croner & Kaplan physiological data, using only anatomical data and estimates of RF center overlap obtained from *in vitro* physiology in the periphery [39]. Figs. 8C1–C2 compare the distributions of  $R_c$  between the macaque and synthetic mRGCs. Note that  $R_c$  in the synthetic mRGCs follows the trend seen in macaque mRGCs with eccentricity, with good agreement at eccentricities above 10° for both subjects. In more central locations, however, the synthetic mRGC RF center sizes are 2–3 times smaller than those in the macaque. We believe that the discrepancy at central locations is not a deficiency of our model, but rather results from several factors. 951  
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First, the cone mosaic in our model has a peak density of 288,000 cones/mm<sup>2</sup> which is near the high end of densities reported in humans [36], whereas the average macaque peak cone density is around 200,000 cones/mm<sup>2</sup> [47, 48]. The higher cone density in humans implies smaller cone apertures, which in turn would bias our synthetic mRGCs towards somewhat smaller RF centers. 962  
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**Fig. 8 Validation against *in vivo* measurements.** In all panels, gray squares depict data from the population of macaque mRGCs recorded by Croner & Kaplan [17]. Blue contours depict the probability density function of the examined parameter in a population of 66,128 synthetic mRGCs with color saturation encoding probability level. Solid blue lines represent the 5% – 95% percentile range of examined parameter. Left and right panels are for mosaics synthesized under physiological optics of two different human subjects. **A1–A2:** Correspondence in ratio of surround-to-center characteristic radii,  $R_s/R_c$ , across eccentricity. The dashed line represents the target value that is in effect during the optimization of the synthetic mRGC surrounds, which is the mean value of  $R_s/R_c$  across the population of all mRGCs recorded by Croner & Kaplan. **A3:** Marginal histograms of  $R_s/R_c$  for macaque (gray) and synthetic mRGCs (blue). **B1–B2:** Correspondence in ratio of surround-to-center integrated sensitivities,  $K_s/K_c \times (R_s/R_c)^2$ , across eccentricity. The dashed line represents the target values in effect during the optimization of the synthetic mRGC surrounds, which is the trend observed with eccentricity in the population of the macaque mRGCs recorded by Croner & Kaplan. **B3:** Marginal histograms of  $K_s/K_c \times (R_s/R_c)^2$  for macaque (gray) and synthetic mRGCs (blue). **C1–C2:** Correspondence in RF center characteristic radius,  $R_c$ , across eccentricity. The fuschia disks represent the  $R_c$  of foveolar mRGCs recorded by Godat *et al.* [10], back-projected in visual space using the monkey's own physiological optics.

Second, in acute macaque experiments, the achieved optical refraction is not necessarily perfect, so there could be residual blur due to errors in refraction, as well as due to corneal edema from the contact lens used in typical multi-day acute experiments. This would increase the size of the RF centers in the physiological data relative to those in our model in central retina. Moreover, residual eye movements can occur in acute experiments, despite the ocular muscle paralysis (personal observations by N.P. Cottaris). Such residual movements would artificially enlarge estimates of RF center size for central retina mRGCs. Finally, in the macaque mRGC vSTF characterizations of Croner & Kaplan, stimulus orientation was not optimized to match any orientation bias in the RF of macaque mRGCs (Lisa Croner, personal communication), whereas in the simulated experiments, stimulus orientation was matched to the cell's visual-space referred orientation bias, which results in the smallest possible estimate of RF center size. Indeed, in additional analyses (not shown) in which we computed vSTFs under random grating orientations as well as a fixed orientation (as was done by Croner & Kaplan), we found enlarged estimates of  $R_c$ . However, these enlarged estimates still fall short of those reported by Croner & Kaplan, so the first two factors that we mentioned above must also be at play.

Further support for our assertion that the discrepancy in  $R_c$  between synthetic and macaque mRGCs at central locations is not a deficiency of our model, is provided by *in vivo* data from foveal macaque mRGC vSTFs obtained under adaptive optics viewing conditions [10]. The center sizes of these cells, blurred by the optics measured for the monkey subjects studied, are depicted by the purple disks in Figs. 8C1 & 8C2. Note that these align well with the  $R_c$  values of our synthetic mRGCs.

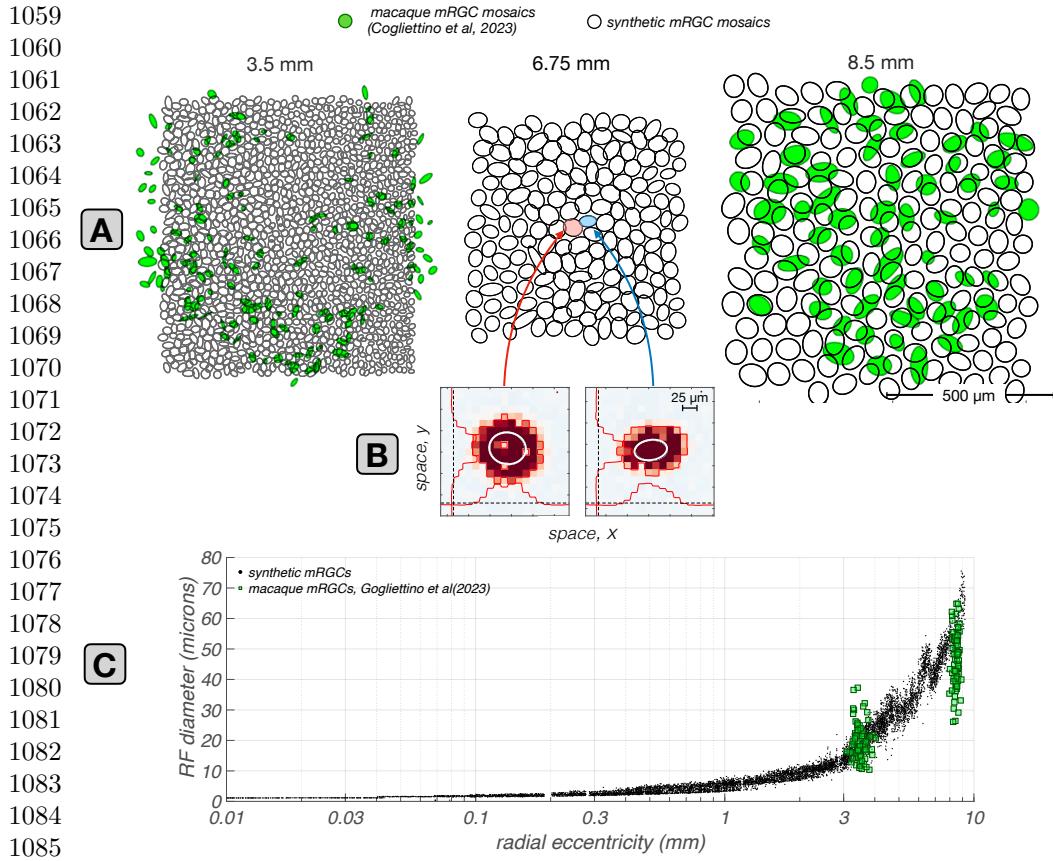
### 3.3 Validation against *in vitro* physiology in the periphery

We also compared spatial RF properties of synthetic mRGCs against macaque data from *in vitro* mRGC recordings. Since the *in vitro* data are not subject to optical blur, they may be compared directly to the retinal-space characteristics of our model. Data of this sort are currently only available in the peripheral retina.

The first study considered is that of Gogliettino *et al.* [49], in which the spatial RFs of mosaics of macaque mRGCs were mapped using white noise stimulation. To simulate their experiments, we probed synthetic mRGCs with white noise modulated achromatic checkerboard stimuli delivered to the retina under diffraction limited optics. To compute the spatial RFs of synthetic mRGCs, we cross-correlated the synthetic mRGC responses with the white noise stimulus sequence. Results of this analysis are depicted in Fig. 9.

The spatial RFs of cells in synthetic mRGC mosaics at three eccentricities, 3.5 mm, 6.75 mm and 8.5 mm, are illustrated by the black ellipses in the three top panels of Fig. 9A. The superimposed green filled ellipses depict spatial RFs from macaque mRGC mosaics located at 3.5 mm and 8.5 mm. Note that at both eccentricities, there is good correspondence in RF center size and coverage between the synthetic and the macaque mRGC mosaics.

To quantify the retinal space-referred RF center sizes in synthetic mRGCs, we computed the diameter of their RF centers as  $2 \times \sqrt{\sigma_{\text{minor}} \times \sigma_{\text{major}}}$ , where  $\sigma_{\text{minor}}$  and  $\sigma_{\text{major}}$  are the standard deviations of the fitted Gaussian ellipsoid along its minor and



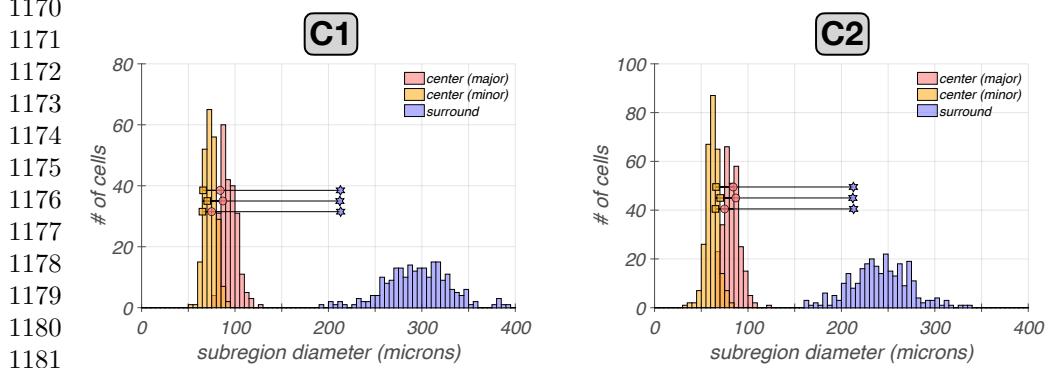
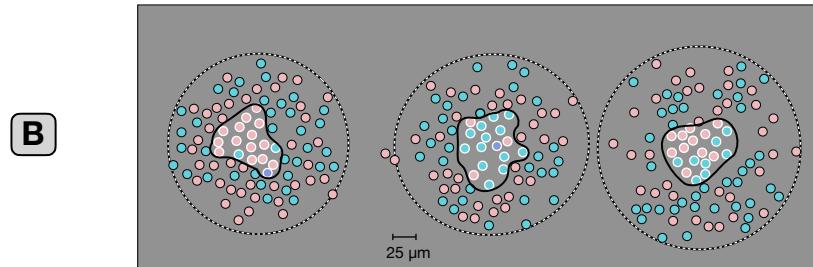
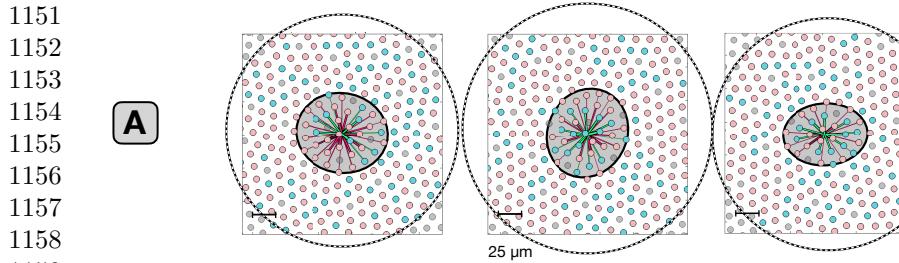
Note that the correspondence between synthetic and macaque data is excellent at 3.5 mm, whereas at 8.5mm, the RF diameters of the synthetic mRGCs are, on average, 30–40% larger than the RF diameters of macaque mRGCs. The deviation in RF center size at the far periphery may occur because human and macaque retinas differ somewhat in the periphery. For example, in the human retina, cone density does not change much for eccentricities > 5mm, whereas in the macaque retina it continues to drop as eccentricity increases [50]. The RF size deviation we observe could be the result of a higher mRGC density in the peripheral macaque retina, relative to the human retina.

The second *in vitro* study we validated our synthetic mRGCs against, is that of Field *et al.* [15], which examined the spatial layout of single cone inputs to the RF centers and surrounds in peripheral macaque mRGCs. Results of this comparison are depicted in Fig. 10. The cone pooling maps of three synthetic mRGCs at a temporal eccentricity of 6.75 mm are depicted in Fig. 10A. The spatial distribution of cone pooling weights in three macaque mRGCs at the same eccentricity from the study of Field *et al.* [15], adapted from their Fig. 4, are shown in Fig. 10B. For both synthetic and macaque mRGCs, the visualized surround cones have pooling weights  $> 0.005 \times$  the peak center cone weight (Greg Field, personal communication).

Note the general agreement between synthetic and macaque mRGCs in the extent of both their RF centers and surrounds, although again, synthetic mRGCs appear to have slightly larger RFs than their macaque counterparts. Also notable is that the density of cones in the synthetic mRGC cone pooling maps is higher than that seen in the macaque mRGCs. This occurs because our model is based on human cone mosaics, and human cone density is higher than macaque cone density at temporal eccentricities above 5 mm [50], which is where these comparisons are made.

To contrast the relationship in center and surround cone pooling regions between synthetic and macaque mRGCs more quantitatively we compared the diameters of cone pooling regions of the three depicted macaque mRGCs against those of populations of synthetic mRGCs at two eccentricities: 6.75 mm, and 6.0 mm. Results of this analysis are depicted in Fig. 10C1 and 10C2. The minor and major diameters of the center pooling mechanism and the diameter of the surround pooling mechanism for the 3 macaque mRGC cells are depicted by the yellow squares, pink circles and magenta stars, respectively. The corresponding distributions in populations of synthetic mRGCs are depicted by the yellow, pink and magenta histograms, respectively. Note that at 6.75 mm (Fig. 10C1), the cone pooling regions of the synthetic mRGCs are consistently larger than those of the three macaque mRGCs. However, at the slightly less peripheral eccentricity of 6.0 mm (Fig. 10C2) a better agreement exists between model and macaque mRGCs.

These observations highlight an inherent issue in building our mRGC model, namely that we had to employ a mixture of human and macaque data sources: human data regarding the density of cones and the density of mRGC RFs across visual space, human data regarding the characteristics of physiological optics across the retina, and macaque data regarding the spatial characteristics of mRGC RFs and of H1 horizontal cells, with our validations done against macaque data. This is not ideal, as there are some differences between human and macaque retinas [50]. But, it is unavoidable given



1183 **Fig. 10 Cone pooling maps in RF centers and surrounds: synthetic vs. macaque mRGCs**  
1184 **recorded *in vitro*.** **A:** Center and surround cone pooling weight maps for three synthetic mRGCs  
1185 at an eccentricity of 6.75 mm along the temporal raphe. Solid and dashed contours include cones  
1186 pooled by the RF center and the RF surround, respectively, with pooling weights  $> 0.005 \times$  the peak  
1187 center weight. **B:** Center and surround cone pooling weights for three macaque mRGCs recorded in  
1188 *vitro* at an eccentricity of 6.75 mm along the temporal raphe. White and black disks indicate cones  
1189 pooled by the RF center and the RF surround respectively, with same threshold pooling weights as  
1190 in A. The macaque mRGCs are from the *in vitro* recordings of Field *et al.* [15]. **C1 &C2:** Compari-  
1191 son of minor and major diameters of the center pooling mechanism (yellow squares and pink circles)  
1192 and of the surround pooling mechanism (purple stars) in the 3 macaque mRGC cells against corre-  
1193 sponding distributions (yellow, pink and magenta histograms) in populations of synthetic mRGCs at  
1194 eccentricities of 6.75 mm (C1) and 6.0 mm (C2).

1193

1194 the lack of complete data in either species. The modeling framework that we devised  
1195 however, which incorporates data from different sources, can be easily modified as new  
1196 data become available.

### 3.4 Visual *vs.* retinal space– referred RFs: the impact of physiological optics

In this section we characterize how physiological optics interacts with the retinal cone pooling within the RFs of mRGCs to shape their visual space–referred RF properties. Fig. 11 illustrates examples of this interaction at five horizontal eccentricities,  $x = [-16^\circ, -8^\circ, 0^\circ, +8^\circ, +16^\circ]$ , and 3 vertical eccentricities,  $y = [-8^\circ, 0^\circ, +8^\circ]$ . The yellow ellipses in each panel of the  $3 \times 5$  grid of Fig. 11A depict Gaussian ellipsoids fitted to the retinal space–referred RF maps of synthetic mRGCs at the examined eccentricities. The small and non-systematic orientation biases in the retinal space–referred RF maps emerge due to the pooling of multiple cones by the RF center mechanism and are reminiscent of RGC mosaics mapped *in vitro* [39].

The blue ellipses in Fig. 11B depict Gaussian ellipses fitted to the visual space–referred RF maps of the same cells. Note that there are striking and systematic orientation biases in these visual space–referred RF maps, which emerge due to the characteristics of physiological optics, whose PSFs are depicted in Fig. 11C. Clearly, the shape of the PSFs, especially at peripheral locations is a major determinant of the visual space–referred RFs in mRGCs.

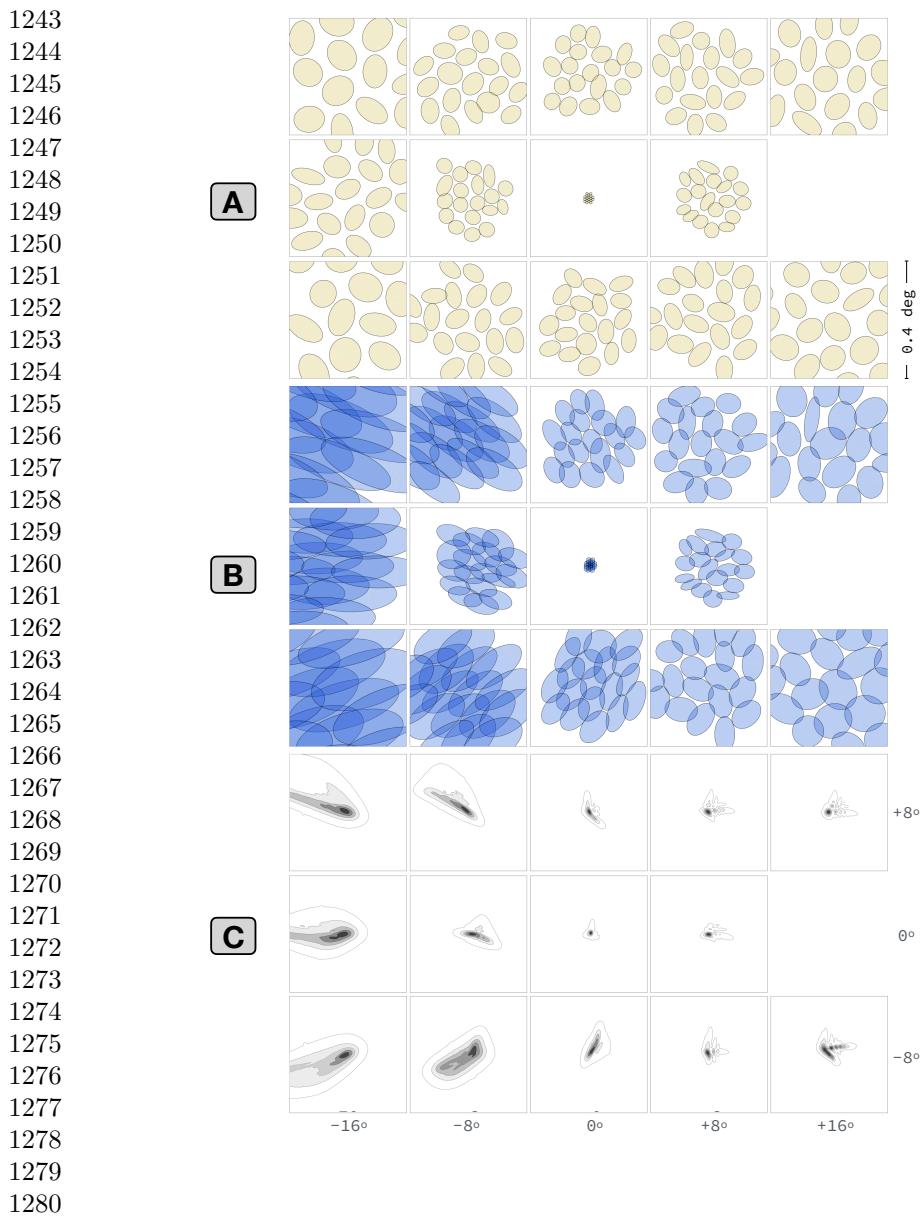
Overall, this analysis demonstrates that there can be substantial differences between *in vivo* and *in vitro* estimates of the spatial RFs of mRGCs, and, once again highlights the notion that inferences regarding retinal wiring from *in vivo* measurements must be evaluated in the context of the effect of the physiological optics. Indeed, in recent on-going work, [31], we have shown the importance of such analyses in assessing inferences regarding cone wiring to the surround subregions of mRGCs based on *in vivo* measurements of their spatio-chromatic RFs.

### 3.5 Validity of the Difference of Gaussians model applied to *in vitro* responses of mRGCs in retrieving their spatial pooling characteristics

In our synthetic mRGCs, the spatial characteristics of cone pooling within the RF center and the RF surround *component* mechanisms are known by design. This allows us to test how well one can predict these characteristics from DoG model fits to *in vitro* measurements of mRGC STFs, where the RF center and surround mechanisms are driven simultaneously in the absence of optics [16].

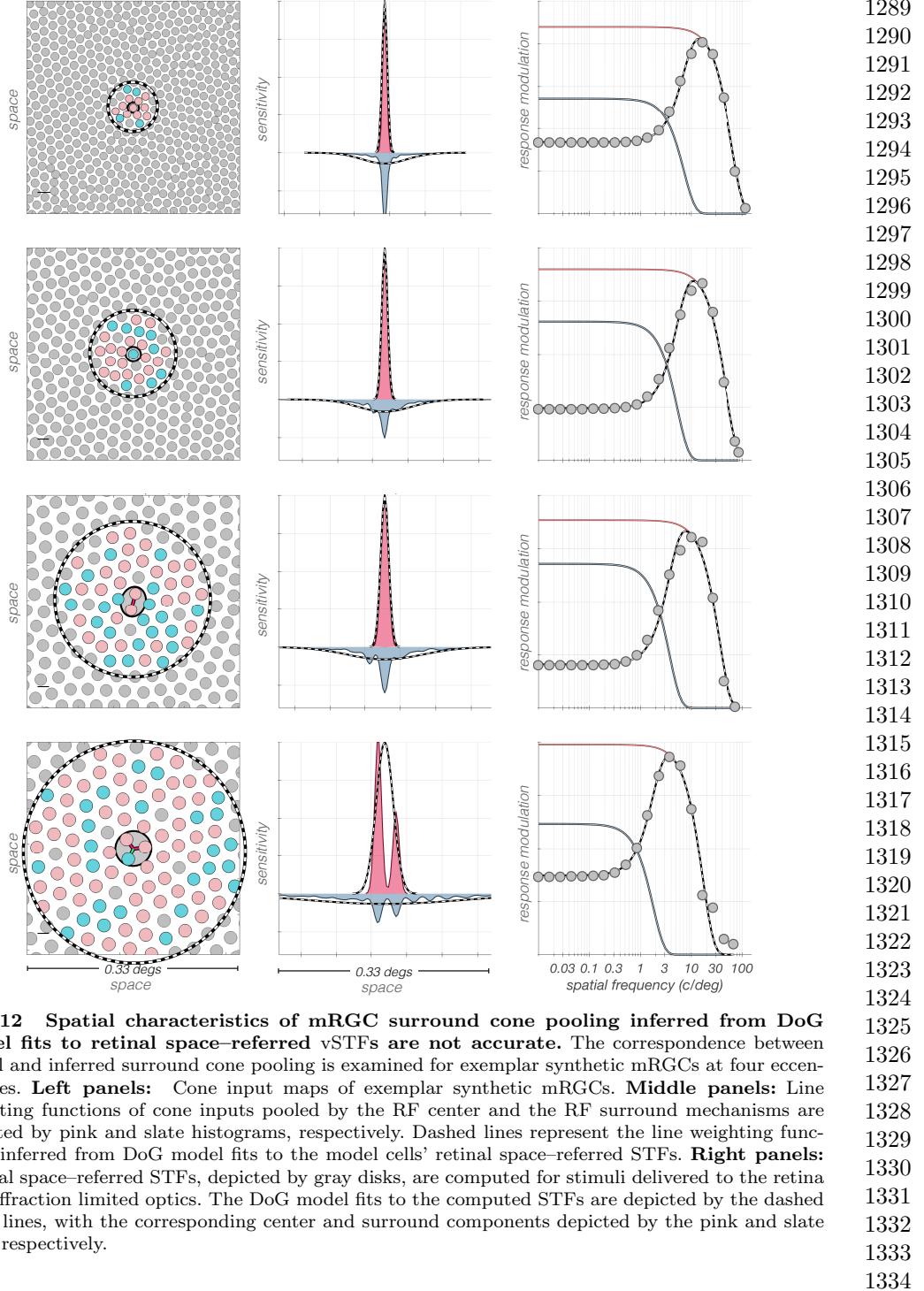
Results of this analysis are illustrated in Fig. 12. The cone pooling maps of four exemplar mRGCs are depicted in the left column. The cells in the top two rows both have RF centers with a single cone input, whereas the cell in the third row has a 2-cone RF center, and the cell in the fourth row has a 3-cone RF center.

The pink and maroon histograms depicted in the middle column of Fig. 12, are the y-axis integrated cone pooling weights within these cells’ RF center and surround sub-regions, respectively. The superimposed dashed lines depict the center and surround line weighting profiles, as estimated by the DoG model fit to the cells’ retinal space–referred STFs, which are depicted by the gray disks in the right column of Fig. 12. Note that although the DoG model fits to the computed retinal space–referred STFs (solid lines in right column) are good for all cells, the inferred spatial RF profiles, (dashed



1281 **Fig. 11 Retinal vs. visual space-referred mRGC RF maps across the retina.** Illustration  
 1282 of the effect of physiological optics on visual space-referred spatial RF maps of synthetic mRGCs  
 1283 across eccentricity. **A:** Retinal space-referred spatial RF maps at different (x,y) eccentricities. Within  
 1284 each panel, yellow contours depict Gaussian ellipsoid fits to RF maps of up to 19 cells from a single  
 1285 mRGC mosaic. RF maps are computed using white noise stimulation under diffraction limited optics.  
 1286 **B:** Visual space-referred spatial RF maps of the same cells, computed under physiological optics  
 1287 of one human subject at corresponding eccentricities. **C:** Point spread functions of the employed  
 1288 physiological optics at corresponding eccentricities.

1288



**Fig. 12 Spatial characteristics of mRGC surround cone pooling inferred from DoG model fits to retinal space-referred vSTFs are not accurate.** The correspondence between actual and inferred surround cone pooling is examined for exemplar synthetic mRGCs at four eccentricities. **Left panels:** Cone input maps of exemplar synthetic mRGCs. **Middle panels:** Line weighting functions of cone inputs pooled by the RF center and the RF surround mechanisms are depicted by pink and slate histograms, respectively. Dashed lines represent the line weighting functions inferred from DoG model fits to the model cells' retinal space-referred STFs. **Right panels:** Retinal space-referred STFs, depicted by gray disks, are computed for stimuli delivered to the retina via diffraction limited optics. The DoG model fits to the computed STFs are depicted by the dashed black lines, with the corresponding center and surround components depicted by the pink and slate lines, respectively.

1335 lines in the middle column), do not capture accurately the cone pooling regions of  
1336 the RF surrounds (slate histograms in the middle column). The discrepancy between  
1337 actual and inferred surround pooling is most obvious in the two top cells which have  
1338 single-cone RF centers, and becomes less pronounced as RF center size increases. The  
1339 discrepancy involves both the spatial extent and the peak sensitivity of the inferred  
1340 surround pooling, which is estimated by the DoG model to be more diffuse with a  
1341 weaker peak sensitivity than the cell's actual surround cone pooling.

1342 It is perhaps not surprising that the DoG model does not do a good job of fitting  
1343 the model cell surrounds, given that they were constructed as double exponentials to  
1344 match the spatial properties of H1 horizontal cells. The key point, however, is that the  
1345 DoG model fits to the observable composite STFs are quite good. These observations  
1346 suggest that caution should be exercised when inferring mRGC RF surround properties  
1347 from DoG model fits to *in vitro* STF measurements.

1348

### 1349 3.6 Applications

1350

1351 We [2, 3, 6], and others [51–53] have reported on how the representation of visual  
1352 information at the level of the cone mosaic shapes visual performance, in our case by  
1353 exploiting the ISETBio image computable model of cone excitations. The transforma-  
1354 tion from cone excitations to RGC responses further shapes the information available  
1355 for perceptual decisions, and we can interrogate our linear spatio-chromatic RF model  
1356 of the ON-center mRGC mosaic to understand how the information available from  
1357 this neuron class differs from that at the cone mosaic.

1358 In this section, we present two example computations of this nature. Our goal is to  
1359 illustrate how our model may be exploited in this way, and not to present a full analysis  
1360 in either case. Even these initial calculations, however, provide interesting insight.

1361

#### 1362 3.6.1 Achromatic and chromatic spatial contrast sensitivity

1363 We used a computational observer approach to compute spatial contrast sensitivity  
1364 functions (CSFs) for achromatic and L – M cone opponent stimuli, based both on the  
1365 representation at the cone mosaic and on the representation at the mRGC mosaic. To  
1366 do so, we computed responses to drifting gratings of varying spatial frequency,  $\omega$ .

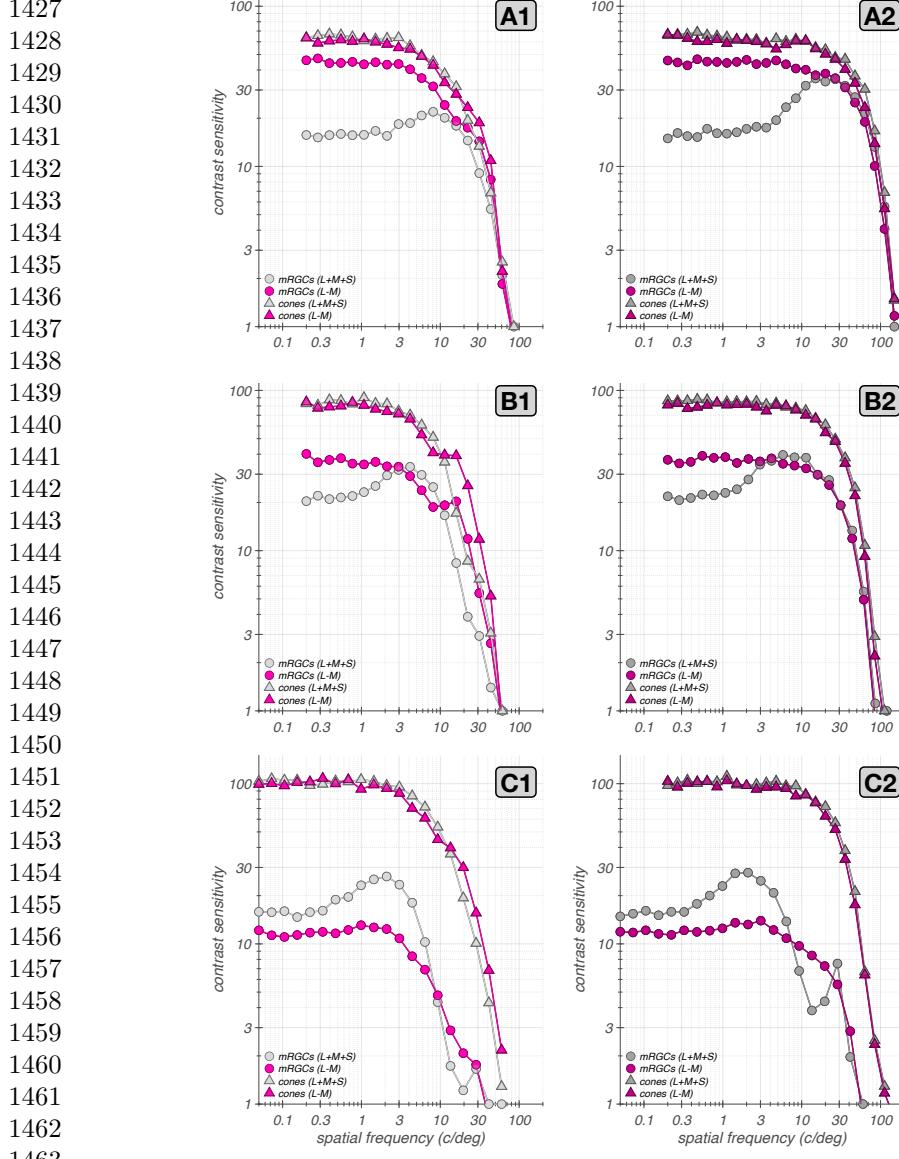
1367 For the achromatic gratings, the L–, M– and S–cone contrast component gratings  
1368 were in phase,  $C_L(\omega, x, y) = C_M(\omega, x, y) = C_S(\omega, x, y)$ . For the L – M gratings, the  
1369 L– and M–cone contrast components were in antiphase,  $C_L(\omega, x, y) = -C_M(\omega, x, y)$ ,  
1370 and  $C_S(\omega, x, y) = 0$ . For all stimuli, the mean  $(x, y)$  chromaticity was  $(0.30, 0.32)$  and  
1371 the mean luminance was  $100 \text{ cd/m}^2$ . Stimuli were simulated as presented on a typical  
1372 CRT monitor, but with 20-bit channel DACs, to avoid intrusion of quantization effects.

1373 For each eccentricity we studied, we oriented the gratings so that they were aligned  
1374 with the axis of elongation of the optical point spread function at that eccentricity.  
1375 Stimulus size was specified so that it extended over the area spanned by the input  
1376 cone mosaic of the employed mRGC mosaic. The size of the mRGC mosaics was varied  
1377 between eccentricities so as to achieve nearly equal numbers of mRGCs for mosaics  
1378 between which we wished to compare performance.

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Cone fundamentals vary with eccentricity because of variation in macular pigment density and photopigment axial density, and this variation is captured by ISET-Bio. Therefore, in these computations, stimuli were designed using cone fundamentals specific to the eccentricity of the employed mRGC mosaic.	1381
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At present, our mRGC model does not include spike generation or response noise. Therefore, in the computations described here we modeled response variability by adding zero mean Gaussian noise to the noise-free responses of the synthetic mRGCs. This approximation allows us to examine relative sensitivity across stimuli and eccentricity, but the overall level of predicted sensitivity is arbitrary. Given the choice of Gaussian noise, we used a template matching computational observer decision rule, with templates provided by the noise-free mRGC responses to the stimuli being discriminated. For comparing computational observer performance at the mRGCs with that at the cones, we also adopted the Gaussian noise approximation for the cone excitations, and used the template matching decision rule.	1386
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To estimate contrast sensitivity, we varied, for each tested spatial frequency, $\omega$ , the contrast of the test stimulus and identified threshold contrast, $C_{\text{threshold}}(\omega)$ , as that for which the probability of correctly identifying the test versus a zero contrast stimulus was 80.6%. Contrast sensitivity was defined as $\text{CSF}(\omega) = 1/C_{\text{threshold}}(\omega)$ .	1395
	1396
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Estimates of so computed contrast sensitivities at three eccentricities are depicted in Fig. 13. The contrast sensitivities for stimuli viewed through typical human optics are shown in the left panels of Fig. 13, with disks and triangles depicting sensitivity at the mRGC mosaic and at its input cone mosaic, respectively. For comparison, the right panels of Fig. 13 depict corresponding calculations for stimulus viewed under diffraction-limited optics with no chromatic aberration, as might be measured using adaptive optics. The comparison between left and right panels helps understand which effects in the computed CSFs have their origin in the optics or sampling by the cone mosaic, and which should be attributed to retinal processing through to the mRGCs.	1400
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1464 **Fig. 13 Computational observer spatial CSFs.** Left column: CSFs computed with stimuli that  
1465 are delivered to the retina through typical human optics. Right column: CSFs computed with stimuli  
1466 that are delivered to the retina under diffraction limited optics. Disk and triangles depict the CSFs  
1467 of the mRGC mosaic and of its input cone mosaic, respectively. Gray and magenta symbols depict  
1468 achromatic and L – M CSFs, respectively. **A1&A2:** CSFs for a  $0.6^\circ \times 0.6^\circ$  foveal mRGC mosaic and of  
1468 its input cone mosaic. This mosaic contains 4628 mRGCs. **B1&B2:** CSFs for a  $2.1^\circ \times 2.1^\circ$  parafoveal  
1469 mRGC mosaic synthesized at an eccentricity of  $4^\circ$  along the temporal meridian. This mosaic contains  
1470 4633 mRGCs. **C1&C2:** CSFs, respectively for a  $4.1^\circ \times 4.1^\circ$  peripheral mRGC mosaic synthesized at  
1470 an eccentricity of  $14^\circ$  along the temporal meridian. This mosaic contains 2195 mRGCs.  
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1472

[16, 56], demonstrate that L – M sensitivity exceeds achromatic sensitivity at low spatial frequencies, consistent with the literature [57].

At high spatial frequencies there is little difference between computational observer sensitivity to achromatic and L – M modulations. This is not true of human observers, where sensitivity drops more rapidly as a function of spatial frequency for red-green isoluminant gratings than for achromatic gratings either with [56] or without typical optical blur [58]. Although our L – M opponent CSFs are not precisely equivalent to the red-green isoluminant CSFs measured in many human experiments, this is not the primary source of the difference between computational and human observers. Rather, it is known that compared to ideal observers, humans lose foveal information available from the cones more rapidly as a function of spatial frequency for red-green than for achromatic gratings [53].

Our example calculation here suggests that this information loss should not be attributed to the linear receptive fields of the mRGCs. We believe this is because optical blur dominates computational observer performance at high spatial frequencies and the single cone RF centers of foveal mRGCs transmit information about each type of stimulus equally well; the surrounds have little effect at high spatial frequencies. Also, we do note that in the present calculations the specific resolution limit, i.e., the spatial frequency at which sensitivity drops to 1, depends on the variance of the added Gaussian noise and is thus somewhat arbitrary. We have chosen a noise level that is low relative to human observers so that our computations show the behavior in the high-spatial frequency regime more fully than would psychophysics conducted through natural optics.

As we move to more peripheral locations, additional features of the CSF emerge. Figs. 13B1 and 13C1 depict results of computations at 4°. Note that under physiological optics viewing (Fig. 13B1) there is a spatial frequency regime in which L – M sensitivity exceeds the corresponding achromatic sensitivity, with the L – M CSF having a notched shape. We have reported this observation in conference abstract form [59]. It occurs because of the wavelength dependent defocus that is introduced by longitudinal chromatic aberration (LCA), which can change the spatial phase of the L– and M–cone stimulus components in the retinal image. Consistent with this interpretation, the notch is present in the CSFs both at the cones and at the mRGCs on the left, but not under diffraction-limited optics (Fig. 13B2), where LCA is zero. Similar effects have been observed for S–cone CSFs [60]. We have presented in abstract form experimental results that suggest that these effects occur in measurements of the human L – M spatial CSF [61].

Comparison of the cone-based CSFs in Fig. 13A1 with those in Fig. 13B1 and Fig. 13C1 also reveals the effect of stronger optical blur with eccentricity, which increases the rolloff of the CSFs with spatial frequency. Similar comparison of the mRGC-based CSFs shows additional rolloff introduced by the increasing size of mRGC RF centers with eccentricity.

Additional observations are notable at 14° (Figs. 13C1 and 13C2). First, a notch arises in the achromatic CSF at high spatial frequencies for the mRGC CSF that is not apparent in the cone CSF. This seems unlikely to be an optical effect, because it is more salient in Fig. 13C2 where optical effects are not present. To explore the origin

1519 of this effect, we computed CSFs at different orientations (not shown), which show  
1520 that this notch is orientation dependent and has to do with the precise alignment of  
1521 individual cones with the receptive field of an mRGC. We do not explore it further  
1522 here.

1523 We also note, once again, that our computational observer is with respect to a noise  
1524 level that makes it more sensitive than the human observer, so that the notch shown  
1525 in Fig. 13C1 would be unlikely to be revealed with psychophysics conducted with  
1526 natural optics. Indeed, in further simulations (data not shown) conducted with twice  
1527 the noise variance, we observed that, in addition to an overall reduction in sensitivity,  
1528 the high frequency notch disappeared under both physiological and adaptive optics  
1529 conditions. It is an interesting question as to whether such effects could be observed  
1530 experimentally under adaptive optics conditions.

1531 Finally, note that the L – M advantage over the achromatic CSF is reversed at 14°  
1532 of eccentricity. This is because at such high eccentricities, the L – M signal is reduced  
1533 by the increased mixing of L– and M–cone signals within the larger mRGC RF centers  
1534 and surrounds. Careful comparison of this effect with computational observer predic-  
1535 tions for various choices of the model’s spatial homogeneity/spectral purity tradeoff  
1536 parameter,  $\phi$ , is an interesting future direction.

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### 1538 3.6.2 Chromatic contrast sensitivity of synthetic mRGC mosaics: 1539 dependence on eccentricity

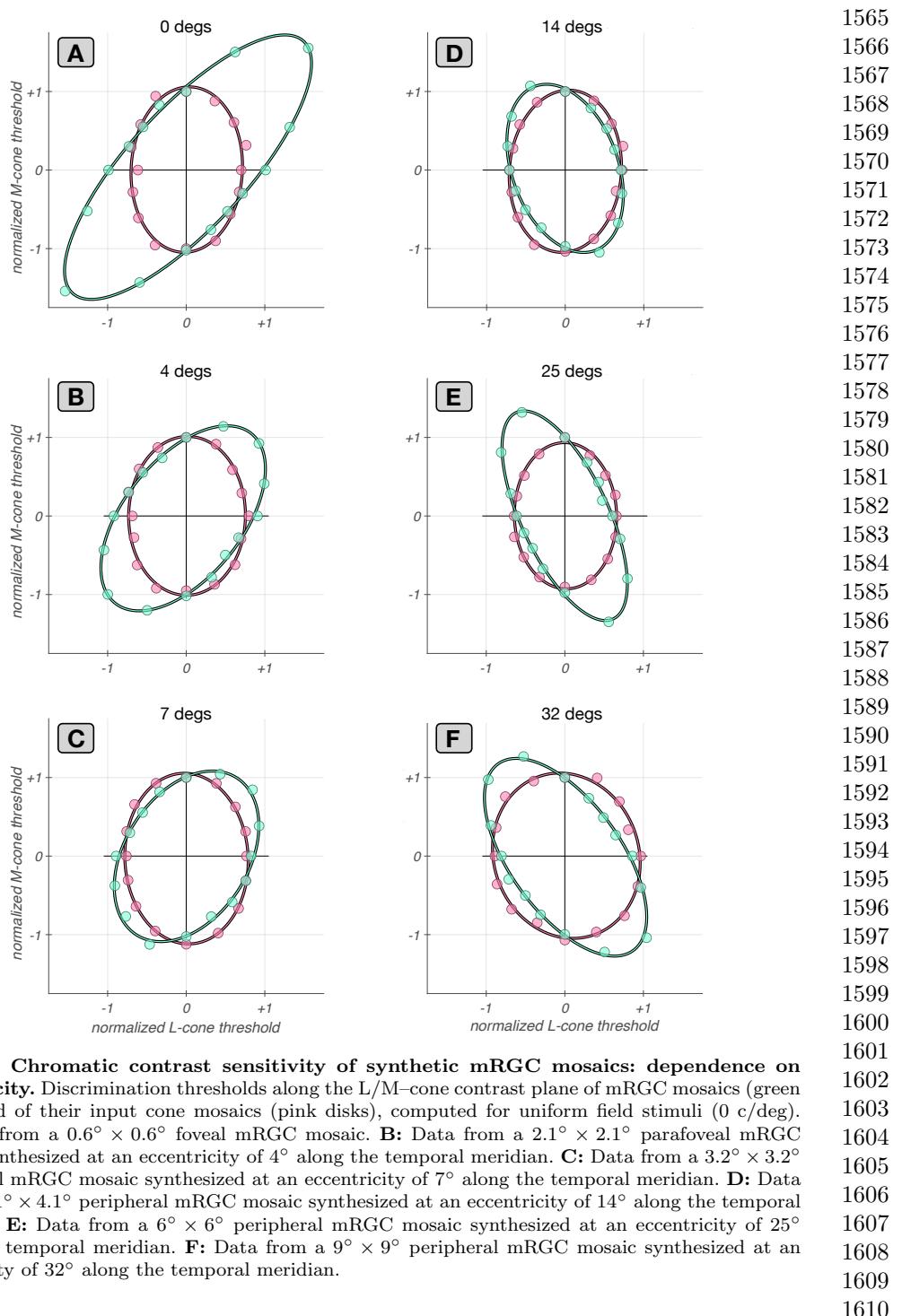
1540

1541 As a second example application, we examined chromatic sensitivity for uniform fields  
1542 modulated in different directions in the L/M-cone contrast plane. We used the same  
1543 computational observer approach described above, and evaluated threshold for stimuli  
1544 whose contrast was modulated in time. The cone contrasts of stimuli at different chro-  
1545 matic directions,  $\theta$ , on the LM plane were:  $C_L(\theta) = \rho \cdot \cos(\theta)$ ;  $C_M(\theta) = \rho \cdot \sin(\theta)$ ;  $C_S(\theta) =$   
1546 0. For each  $\theta$ , we varied  $\rho$  to find its threshold value for discriminating that modula-  
1547 tion direction from a zero contrast stimulus with a probability of 0.806. To summarize  
1548 the computed thresholds across the different chromatic directions, we fit ellipses to  
1549 the locus of threshold contrast points.

1550 Fig. 14 depicts computational observer thresholds for synthetic mRGC mosaics and  
1551 for their input cone mosaics at different eccentricities. Note that how computational  
1552 observer sensitivity changes with eccentricity depends on how stimulus size is covaried  
1553 with eccentricity, as does human sensitivity (e.g. [62]). Comparison of the magnitude  
1554 of sensitivity for cone- and mRGC-based computational observers depends on how the  
1555 noise levels are chosen. For these example calculations, we focus on the shape rather  
1556 than magnitude of the elliptical threshold contours. Therefore, each contour shown in  
1557 Fig. 14 is normalized so that the threshold along the M cone direction is equal to one.

1558 A few observations are notable. First, the normalized contours for the cone mosaic-  
1559 based observer are similar across eccentricities and align with the L– and M–cone  
1560 contrast axes. They are more elongated in the M–cone direction because our mosaics  
1561 have more L cones than M cones. The alignment with the axes is expected [63], and  
1562 the similarity of the normalized shapes occurs because this shape depends primarily  
1563 on the relative numbers of L and M cones.

1564



**Fig. 14 Chromatic contrast sensitivity of synthetic mRGC mosaics: dependence on eccentricity.** Discrimination thresholds along the L/M-cone contrast plane of mRGC mosaics (green disks) and of their input cone mosaics (pink disks), computed for uniform field stimuli (0 c/deg). **A:** Data from a  $0.6^\circ \times 0.6^\circ$  foveal mRGC mosaic. **B:** Data from a  $2.1^\circ \times 2.1^\circ$  parafoveal mRGC mosaic synthesized at an eccentricity of  $4^\circ$  along the temporal meridian. **C:** Data from a  $3.2^\circ \times 3.2^\circ$  parafoveal mRGC mosaic synthesized at an eccentricity of  $7^\circ$  along the temporal meridian. **D:** Data from a  $4.1^\circ \times 4.1^\circ$  peripheral mRGC mosaic synthesized at an eccentricity of  $14^\circ$  along the temporal meridian. **E:** Data from a  $6^\circ \times 6^\circ$  peripheral mRGC mosaic synthesized at an eccentricity of  $25^\circ$  along the temporal meridian. **F:** Data from a  $9^\circ \times 9^\circ$  peripheral mRGC mosaic synthesized at an eccentricity of  $32^\circ$  along the temporal meridian.

1611 Second, in contrast to the cone mosaic-based thresholds, the mRGC mosaic-based  
1612 threshold contours change markedly with eccentricity. For the foveal mRGC mosaic,  
1613 the threshold ellipse is highly elongated along  $45^\circ$  in the L/M-cone contrast plane,  
1614 indicating that the highest discrimination thresholds occur when  $C_L = C_M$  and lowest  
1615 thresholds occur when  $C_L = -C_M$ . This difference in comparison to the cone-based  
1616 computations is a consequence of the chromatic opponency of foveal mRGC RFs,  
1617 which have single cone centers, and thus opponency between their centers and the  
1618 surrounds as the surrounds draw on mixed cone-types [64, 65]. This opponency leads to  
1619 cancellation of non-opponent L- and M-cone signals for low spatial frequency stimuli  
1620 and thus the observed contour elongation along  $45^\circ$  [63, 66].

1621 Third, as eccentricity increases, the contours first become less elongated and then  
1622 elongation starts increasing again but along the  $135^\circ$  rather than the  $45^\circ$  axis. This  
1623 is because the cone non-selective wiring model we implemented leads to progressively  
1624 less opponency with increasing RF center size [16, 64, 65].

1625 Although the qualitative features that emerge from this example calculation are  
1626 understood in the literature, the example illustrates that our model enables this type  
1627 of calculation to be made quantitatively in a way that takes chromatic aberration,  
1628 stimulus size and spatial frequency and retinal position into account. Of particular  
1629 interest to us will be exploring how this type of threshold contour varies with the the  
1630 tradeoff between spatial homogeneity and spectral purity of mRGC RF centers (the  
1631 center wiring parameter  $\phi$  of our model).

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## 1633 4 Discussion

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1635 We developed an image computable model of the linear spatio-chromatic RF mosaic  
1636 of mRGCs across the retina. The model extends our image-computable cone mosaic  
1637 model [2, 3] by adding a layer of mRGCs which pool signals directly from the cone  
1638 mosaic. The connectivity between cones and mRGCs is derived using a simulation  
1639 framework that integrates anatomical, physiological and optical quality data, all of  
1640 which vary across eccentricity.

1641 By explicitly modeling the optics and photoreceptors, rather than directly express-  
1642 ing the RFs in terms of the stimulus, we are able to link our model with both *in-vitro*  
1643 and *in-vivo* data, and to make predictions over a range of experimental conditions  
1644 that are otherwise difficult to compare. These include psychophysical and physiolog-  
1645 ical measurements made through physiological optics (natural viewing conditions),  
1646 interferometric and adaptive optics techniques that bypass or correct for optical  
1647 aberrations, and *in-vitro* physiology, where the natural optics are not present.

1648 To build the model we had to overcome the challenge that current data about  
1649 mRGC properties are incomplete and, where they exist, may come from different  
1650 species, different measurement modalities, and from different eccentricities. For exam-  
1651 ple, there are *in-vivo* measurements of mRGC linear receptive fields across the retina  
1652 [17], but physiological optics blur the stimuli so that they do not constrain mRGC  
1653 input at the cone-by-cone resolution we seek. On the other hand, although there is  
1654 single cone-resolution connectivity data from *in-vitro* physiology [15], these data are  
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currently limited to large eccentricities ( $\geq 25^\circ$ ). Thus, we developed a modeling framework that allows integration of data from multiple sources. This framework is an important contribution in its own right; we expect it will be useful to us and others, for incorporating new data that become available and for modeling other RGC classes.	1657
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We showed that the model captures visual space-referred spatial RF properties of macaque mRGCs recorded <i>in-vivo</i> across eccentricities, as well as retinal space-referred spatial RF properties of macaque mRGCs recorded <i>in-vitro</i> . We also showed that physiological optics plays a major role in shaping the visual space-referred spatial RF properties, so that inferences regarding retinal circuitry made from <i>in-vivo</i> measurements need to be evaluated in the context of the optics. Further, we showed that even under <i>in-vitro</i> conditions, where the optics are eliminated, the traditional approach of fitting a Difference of Gaussian model to spatial responses can lead to incorrect assessments of the properties of cone pooling in the mRGC surrounds.	1662
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1703 not been our goal, we would have had to bring in human data to characterize the  
1704 physiological optics across the visual field, as such data are not currently available in  
1705 macaque. At the same time, not all the required data are available for human: although  
1706 measurements of cone and mRGC density and physiological optics across the retina  
1707 are available, physiological characterizations come from the macaque.

1708 The need to mix data across the two closely related species produces tension in  
1709 cases where the parameters for the two species differ. An example is the different  
1710 cone densities in the far periphery [50], which intrudes on the interpretation of the  
1711 comparison between our model and *in-vitro* physiology in that retinal region. As more  
1712 data become available in both species, and as species differences come more fully into  
1713 focus [67], our approach should allow more fully differentiated models to be developed  
1714 targeted at each.

1715

#### 1716 4.2.2 Noise, nonlinearities and temporal dynamics

1717 Although the current model captures fundamental aspects of the visual representation  
1718 at the level of the mosaic of ON mRGCs, there are known characteristics of mRGCs  
1719 that it does not account for. These include static and spatial nonlinearities, temporal  
1720 filtering, spike generation, and physiologically constrained response noise. The modeling  
1721 framework we developed is extensible however, so that these components may be  
1722 included through future work.

1723 Response variability models are available for macaque mRGCs, as descriptions of  
1724 spike generation mechanisms [26, 33, 68]. In addition, we can incorporate nonlinearities,  
1725 such as (a) light adaptation effects introduced through the phototransduction  
1726 cascade [69], (b) compressive and expansive static nonlinearities in the output of  
1727 mRGCs [23, 33], and (c) spatial nonlinearities introduced by rectifying sub-units within  
1728 the RFs of mRGCs [21, 22]. Explicit inclusion of photocurrent-based responses in the  
1729 input to the mRGCs introduces a temporal component to the response model [69]. In  
1730 addition, a second temporal filter may be added, such that when combined with the  
1731 photocurrent filter will yield the bandpass filter characteristics observed in macaque  
1732 mRGCs [25].

1733 Our current model does not represent explicitly the properties of the retinal circuitry (horizontal, bipolar, and amacrine cells) that produces the mRGC response  
1734 properties, as we have opted instead to work towards a functional model that describes  
1735 those properties. A complementary mRGC modeling approach that does consider some  
1736 of these cell types explicitly has recently been published [30], and there are other  
1737 modeling efforts that have examined the influence of the various retinal interneurons  
1738 on RGC response properties [28, 32]. We note however, that some of the processing  
1739 performed by these other retinal cell types is incorporated implicitly in the current  
1740 cone-to-mRGC model, such as the parametric form of the surrounds inherited from  
1741 H1 cells.

1742 The framework we developed is designed so that it would be possible to interpose  
1743 explicit models of intermediate retinal cell types. Representing the action of different  
1744 cell types explicitly may in the longer run be an effective way to account for response  
1745 nonlinearities in the mRGCs, or in other classes of retinal ganglion cells. Moreover,  
1746 using our framework to model other cell classes may be of interest to those seeking to  
1747

interpret responses of those classes *per se*, or in the retinal mechanisms that produce RGC response properties. 1749  
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#### 4.2.3 OFF mRGC mosaic

Because we model the linear RF, the distinction between ON and OFF mRGCs is subtle. However, our model should be thought of as a model of only the ON mRGCs because the synthetic cells only pool signals from L- and M-cones. This is believed true for ON mRGCs, but recent evidence suggests that OFF mRGCs draw upon all three types of cones in their RF centers [15, 37, 38]. Incorporating S-cone input into an OFF mRGC model is straightforward.

Another question that arises when considering a model of OFF mRGC mosaic is how to split the density of mRGCs in two populations at different eccentricities. In the current model, the ON mRGC density was assumed to be half of all mRGCs across all eccentricities. This seems reasonable for central retina where mRGC centers draw primarily on a single cone and where anatomical evidence suggests that each cone provides input to the center of one ON and one OFF midget bipolar cell. However, there is evidence that the RFs of peripheral ON midget (and parasol) RGCs are larger than their OFF counterparts in both human and macaque retinas [40]. This implies that the density of ON RGC cells might be lower in the periphery than that of OFF cells, given that ON and OFF mRGCs have similar RF overlap [39]. One idea is to treat the asymmetry between ON and OFF mRGC RF densities in an eccentricity-dependent manner, similar to the way we encoded a variable-with-eccentricity RF center overlap.

Finally, when adding an OFF mRGC mosaic one should allow for the possibility of coordination between the ON and the OFF submosaics, to account for recent observations regarding systematic shifts in the spatial layouts of ON and OFF mRGCs [70].

### Using the software

The developed software for synthesizing ON mRGCm mosaics across the retina and for computing with them is part of ISETbio and is freely available at

<https://github.com/isetbio/isetbio>. An introduction to using the mRGCmosaic software is available at:

[https://github.com/isetbio/isetbio/wiki/Retinal-ganglion-cell-\(RGC\)-mosaics](https://github.com/isetbio/isetbio/wiki/Retinal-ganglion-cell-(RGC)-mosaics), and a number of MATLAB tutorials specific to the mRGCmosaic can be found at <https://github.com/isetbio/isetbio/tree/main/tutorials/mrgc>.

These tutorials demonstrate (a) how to use mosaics of ON mRGCs that have been synthesized at a number of eccentricities, and (b) how to build and validate mRGC mosaics at any desired eccentricity, using a number of design choices. A summary of current available tutorials is shown in Table 1.

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1795      **Table 1 List of tutorials for computing with mRGC mosaics and de novo**  
 1796      **synthesis of mRGC mosaics.**

1797	Tutorial name	Scope
<i>Computing with mRGC mosaics</i>		
1799	<code>t_mRGCMosaicVisualizeWithOptics.m</code>	Visualizes a previously synthesized mRGC mosaic and the optics that were used for its synthesis
<i>Synthesizing mRGC mosaics</i>		
1800	<code>t_mRGCMosaicSynthesizeAtStage1.m</code>	Denovo synthesis of the spatial position lattices of cones and mRGC RF centers (stage 1)
1801	<code>t_mRGCMosaicSynthesizeAtStage2.m</code>	Denovo synthesis of an mRGC mosaic at different sub-stages of cone-to-mRGC RF center connectivity (stage 2)
1802	<code>t_mRGCMosaicSynthesizeAtStage3.m</code>	Denovo synthesis of an mRGC mosaic at different sub-stages of cone-to-mRGC RF surround connectivity (stage 3)

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 1816  
 1817      **Declarations**

1819      **Funding**

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 1823

1824      **Conflict of interest/Competing interests**

1825 Not applicable

1827

1828      **Ethics approval and consent to participate**

1829 Not applicable

1831      **Consent for publication**

1833 Not applicable

1834

1835      **Data availability**

1836 Datasets (ON mRGCmosaics) generated during the current study are available at:

1837 <https://github.com/isetbio/isetbio/tree/main/isettools/ganglioncells/data/>

1838 [prebakedRGCmosaics/ONmRGCmosaics](https://github.com/isetbio/isetbio/tree/main/isettools/ganglioncells/data/prebakedRGCmosaics/ONmRGCmosaics)

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<b>Materials availability</b>	1841
Not applicable	1842
	1843
<b>Code availability</b>	1844
The code used to generate the data, and various tutorials on how to use the software are available at:	1846
<a href="https://github.com/isetbio/isetbio/tree/main">https://github.com/isetbio/isetbio/tree/main</a>	1847
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An introduction to using the software is available at:	1850
<a href="https://github.com/isetbio/isetbio/wiki/Retinal-ganglion-cell-(RGC)-mosaics">https://github.com/isetbio/isetbio/wiki/Retinal-ganglion-cell-(RGC)-mosaics</a>	1851
	1852
	1853
<b>Author contribution</b>	1854
NPC: conceptualization, mosaic synthesis & optimization algorithms, data curation, model validation, visualization, coding, writing of original draft	1855
DHB: conceptualization, coding, reviewing and editing of manuscript	1856
BW: conceptualization, coding, reviewing and editing of manuscript	1857
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1887 **Appendix A Deriving cone weights to the mRGC  
1888 RF centers**  
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1890 **A.1 Local topology-based convergent connections (stage 2A)**  
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1892 During the first sub-stage of cone to mRGC RF center connectivity, cones are con-  
1893 nected to single mRGC RF centers based on the local topology of their respective  
1894 lattices. Starting with the cell whose RF center is at most central location of the  
1895 mRGC lattice, we connect  $n_{pool}(\epsilon)$  number of L- and M-cones to it, where:

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1897 
$$n_{pool}(\epsilon) = \lfloor \frac{D_{cones}(\epsilon)}{D_{mRGCRF}(\epsilon)} \rfloor \quad (A1)$$
  
1898

1899 with  $D_{cones}(\epsilon)$  and  $D_{mRGCRF}(\epsilon)$  being the local spatial densities of the cone mosaic  
1900 and of the mRGC RF centers, respectively, at the eccentricity,  $\epsilon$ , of the target mRGC.  
1901 We draw from the nearest cones that have not yet been connected and whose distance  
1902 to the mRGC RF center does not exceed a fraction of the local mRGC RF center  
1903 spacing. This fraction is a parameter of the model and for the work presented here  
1904 was set to 0.6.

1905 Continuing with these assignments of cones to mRGC RF centers, we move outward  
1906 to more peripheral locations in the mRGC mosaic, connecting cones to each mRGC  
1907 RF center. Any L- and M-cones that remain unconnected at the end of this sub-stage  
1908 are then connected to their nearest mRGC RF center, so that all cones are connected  
1909 to one mRGC RF center.

1910 This sub-stage can result in local inhomogeneities in both the number of cones and  
1911 the type of cones pooled within neighboring mRGC RF centers. These inhomogeneities  
1912 are smoothed out as part of the next sub-stage.

1913  
1914 **A.2 Optimizing cone connections to mRGC RF centers  
1915 (stage 2B)**

1916 In the second sub-stage of the cone to mRGC RF center connectivity, convergent  
1917 connections from multiple cones to single mRGC RF centers are optimized according  
1918 to a desired balance between spatial homogeneity and spectral purity. This is achieved  
1919 by reassigning cones between nearby mRGC RF centers, which itself occurs in two  
1920 steps.

1921 In the first step, we allow cone reassessments to a target mRGC from neighboring  
1922 mRGCS that have a higher input cone numerosity in their RF centers. In the second  
1923 step, we allow cone swaps between a target mRGC and its neighbors, independently  
1924 of their input cone numerosities.

1925 The heuristics followed in the first step are as follows. We begin by targeting  
1926 mRGCS with a single input cone and continue to target mRGCS with progressively  
1927 higher input cone numerosity. Within each set of targeted input cone numerosity,  
1928 mRGCS are sorted based on ascending retinal eccentricity. For each targeted mRGC  
1929 we determine up to 6 neighboring mRGCS which have input numerosity that exceeds  
1930 that of the target mRGC by at least 2 cones.

Cone reassessments from the candidate donor mRGCs to the target mRGC are executed in multiple passes. Starting with the neighboring mRGC of the highest input numerosity, we determine the best transfer of a single cone. If there are no eligible donor nearby mRGCs, we move to the next targeted mRGC. If there is a single candidate, we accept it and execute the cone transfer. If there are more than one candidates, for each candidate donor mRGC we compute a cost function, C, for reassigning each of its cones to the target mRGC, and pick the transfer that minimizes C across all cones and all candidate donor mRGCs. The cost function is described in more detail below.	1933
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Once the optimal cone transfers for each mRGC of the targeted input cone numerosity are executed, we move to the next pass, examining possible transfers from neighboring mRGCs of lower input cone numerosity than before, but still higher than the input cone numerosity of the targeted mRGCs. Once all passes are executed, this process is repeated, now targeting mRGCs with increasing input cone numerosity, until all input cone numerosities have been targeted.

In the second step, we only allow for cone swaps between an mRGC RF center and one of its neighbors. For each mRGC of the targeted input cone numerosity, we determine its 6 closest neighbors, but now without regard to their input cone numerosity. For each of these neighboring mRGCs, we evaluate the cost function, C, for all possible combinations of cones from the target mRGC and cones from the neighboring mRGC and pick the combination that minimizes C. The selected cone swap is executed only if the post-swap value of C is lower than its pre-swap value. Multiple passes through the entire mRGC mosaic, are executed, with each pass targeting mRGCs with progressively higher input cone numerosity.

The cost function, C, employed to determine the optimal transfer/swapping is based on the position and types of the cones pooled by the target mRGC,  $t$ , and the examined neighboring mRGC,  $t_i$ . For each examined pair of mRGCs,  $(t, t_i)$ ,  $C^{(t, t_i)}$  is defined as:

$$C^{(t, t_i)} = \phi \cdot C_{\chi}^{(t, t_i)} + (1 - \phi) \cdot C_{\lambda}^{(t, t_i)} \quad (\text{A2})$$

where  $C_{\chi}^{(t, t_i)}$  quantifies the degree of spatial incompactness,  $C_{\lambda}^{(t, t_i)}$  quantifies the degree of spectral impurity. The  $\phi$  parameter controls the desired trade-off between spatial incompactness and spectral impurity of the RF centers. When  $\phi = 1$ , cone reassessments/swaps are selected so as to minimize the spatial incompactness score, when  $\phi = 0$ , cone reassessments are chosen so as to minimize the spectral impurity score, and for intermediate values of  $\phi$ , cone reassessments are chosen so as to minimize a ratio of the two scores.

The spatial incompactness score,  $C_{\chi}^{(t, t_i)}$ , in Eq. A2 is defined as:

$$C_{\chi}^{(t, t_i)} = C_{\chi_N}^{(t, t_i)} + C_{\chi_o}^{(t, t_i)} \quad (\text{A3})$$

The  $C_{\chi_N}^{(t, t_i)}$  term quantifies the differential input cone numerosity between the examined pair of mRGCs, and is defined as:

$$C_{\chi_N}^{(t, t_i)} = |(N_L^t + N_M^t) - (N_L^{t_i} + N_M^{t_i})| \quad (\text{A4})$$

1979 with  $N_L^t$  and  $N_M^t$  are the numbers of L– and M–cones pooled by the RF center of  
 1980 mRGC  $t$ , respectively. The  $C_{\chi_o}^{(t,t_i)}$  term is a measure of the spatial overlap of the two  
 1981 sets of cones pooled by the two mRGCs, and is defined as the inverse of the distance  
 1982 between the centroids,  $(P^t, P^{t_i})$ , of the sets of pooled cones normalized by the sum of  
 1983 their respective spatial standard deviations,  $(\sigma^t, \sigma^{t_i})$ :

1984

$$1985 \quad C_{\chi_o}^{(t,t_i)} = 1 / \left( \frac{\|P^t - P^{t_i}\|}{\sigma^t + \sigma^{t_i}} \right) \quad (\text{A5})$$

1987

1988 A low value of  $C_{\chi_o}^{(t,t_i)}$  indicates low overlap between the sets of cones pooled by the  
 1989 examined pair of mRGCs and conversely, a high value indicates a large overlap.

1990 The spectral impurity score,  $C_\lambda^{t,t_i}$ , in Eq. A2, is defined as the sum of spectral  
 1991 impurities of the RF centers of the pair of analyzed mRGCs:

1992

$$1993 \quad C_\lambda^{t,t_i} = C_\lambda^t + C_\lambda^{t_i} \quad (\text{A6})$$

1994

1995 with  $C_\lambda^t$ , quantifying the degree of non-specificity, with regard to the type of cone, in  
 1996 the pooling within the RF center of an mRGC, defined as:

1997

$$1998 \quad C_\lambda^t = \frac{\min([N_L^t, N_M^t])}{N_L^t + N_M^t} \quad (\text{A7})$$

2000

2001 Values of  $C_\lambda^t$  near zero indicate a low amount of mixture of L– and M–cones, and  
 2002 therefore a RF with a high degree of spectral purity, and conversely, values of  $C_\lambda^t$ , near  
 2003 0.5, indicate an equal mixture of L– and M–cones, and therefore a RF center with a  
 2004 low degree of spectral purity.

2005

### 2006 A.3 Divergent cone connections to multiple mRGC RF 2007 centers (stage 2C)

2009 In the final sub-stage of establishing the RF center connectivity, the exclusivity of  
 2010 connections is relaxed, and cone connections are allowed to diverge to more than one  
 2011 mRGC RF center. This divergence is guided by *in-vitro* measurements of mRGC RF  
 2012 center overlap in the macaque [39].

2013 According to these observations, neighboring mRGC RF centers abut at approxi-  
 2014 mately one standard deviation of their Gaussian RF profile. One caveat of using these  
 2015 *in-vitro* measurements to establish cone divergence in the model, is that these measure-  
 2016 ments are only available in the far periphery (30–40 degrees), with no data available  
 2017 for more central locations. Anatomical studies suggest, however, that, in the central  
 2018 retina, there must be little to no divergence of cone signals to mRGCs RF centers, so  
 2019 we chose to implement an eccentricity-varying divergence in our model.

2020 To achieve this, we begin by fitting an ellipsoid to the spatial pooling map of cones  
 2021 that are exclusively connected to the RF center of an mRGC, and extract the rotation,  
 2022  $\alpha$ , and the major/minor axes,  $\sigma_x, \sigma_y$  of the fitted ellipsoid. Next, a supra-Gaussian  
 2023

2024

ellipsoid function,  $G(x, y, n)$ , defined as:

$$G(x, y, n) = \exp \left[ -0.5 \times \left( \sqrt{(y'^2 + y'^2)} \right)^n \right] \quad (A8)$$

with:

$$\begin{bmatrix} x' & y' \end{bmatrix} = \begin{bmatrix} x & y \end{bmatrix} \cdot \begin{bmatrix} \cos(\alpha) & -\sin(\alpha) \\ \sin(\alpha) & \cos(\alpha) \end{bmatrix} \cdot \begin{bmatrix} 1/\sigma_x & 0 \\ 0 & 1/\sigma_y \end{bmatrix} \quad (A9)$$

is computed by scaling the values of  $\sigma_x, \sigma_y$  by a common factor, so that the value of  $G(x, y, n)$ , evaluated at the most remote exclusively-connected cone(s) is  $k \times e^{-1/2}$ . The value of  $k$  is determined empirically so that RF maps of nearby mRGCs computed under diffraction-limited optics abut when their sensitivities drop to  $e^{-1/2}$  (per [39]).

By varying the exponent of the supra-Gaussian,  $n$ , we model varying degrees of cone divergence. When  $n = 10$ , we obtain a flat-top Gaussian with very sharp fall-offs, modeling minimal cone divergence. When  $n = 2$ , we get a standard Gaussian modeling cone divergence that is consistent with the *in-vitro* measurements of RF center overlap at peripheral locations.

By allowing  $n$  to vary with eccentricity using a sigmoidal function we obtain a gradual transition in cone divergence with eccentricity. The slope and mid-point of the sigmoidal variation of  $n$  are currently chosen arbitrarily, with the only restrictions that above  $15^\circ$ ,  $n$  is stable at 2.0, and below  $7^\circ$ ,  $n$  is stable at 10.0. The weights of divergent cone-mRGC RF center connections are computed by evaluating the supra-Gaussian ellipsoid at the positions of all cones in the vicinity of the examined mRGC.

## Appendix B Deriving cone weights to the mRGC RF surrounds

### B.1 Choosing physiology-based constraints for deriving surround cone weights in stage 3B

The optimization of the parameters of the surround cone pooling functions at each iteration is driven by the residual between the visual STF that is computed based on the surround pooling weights at the previous iteration and the Difference of Gaussians model fit to it,  $DoG(\omega)$ , which is given by:

$$DoG(\omega) = K_c \cdot R_c^2 \cdot \exp[-\pi \cdot R_c \cdot \omega]^2 - K_s \cdot R_s^2 \cdot \exp[-\pi \cdot R_s \cdot \omega]^2 \quad (B10)$$

This aspect of the optimization captures the observation that the DoG model provides a reasonable fit to the *in-vivo* measured STFs of macaque mRGCs. To ensure adherence to the *in-vivo* data of Croner & Kaplan, the DoG model fit is constrained so that the ratio of surround to center radii,  $R_s/R_c$ , and the ratio of surround to center integrated sensitivities,  $K_s/K_c \times (R_s/R_c)^2$ , both remain within a specified tolerance range from the corresponding macaque data.

2071 Specifically, for the model's  $R_s/R_c$  ratio, we enforce  
2072

$$2073 \quad \frac{R_s^m}{R_c^m} \times (1 - \tau) \leq \frac{R_s}{R_c} \leq (1 + \tau) \times \frac{R_s^m}{R_c^m} \quad (B11)$$

2074

2075 where  $R_c^m$  and  $R_s^m$  are the mean values of center and surround radii across the Croner  
2076 & Kaplan population of macaque mRGCs at the eccentricity of the synthesized mRGC.  
2077 The model's  $K_s/K_c \times (R_s/R_c)^2$  ratio is constrained in the same way.

2078 The residual between the visual STF and the Difference of Gaussians model fit to  
2079 it, drives the optimization of the surround pooling function. This function is a double  
2080 exponent (following the H1 horizontal cell spatial RF in the macaque [43]):  
2081

$$2082 \quad W_s(r) = K_{\text{wide}} \times \exp[-r/R_{\text{wide}}] + K_{\text{narrow}} \times \exp[-r/R_{\text{narrow}}] \quad (B12)$$

2083

2084 To ensure that the surround pooling function remains consistent with parameter  
2085 values observed in macaque H1 cell [43], the optimization of  $W_s(r)$  is also constrained  
2086 so that ratio of radii,  $R_{\text{narrow}}/R_{\text{wide}}$ , and the ratio of volumes,  $V_{\text{narrow}}/V_{\text{wide}} =$   
2087  $K_{\text{narrow}}/K_{\text{wide}} \times (R_{\text{narrow}}/R_{\text{wide}})^2$ , of the two exponentials both remain within a  
2088 specified tolerance range of the macaque data.

2089 In the present work, the tolerance range for  $R_{\text{narrow}}/R_{\text{wide}}$  was set to [0.07, 0.35]  
2090 for all mosaics, whereas the tolerance range for  $V_{\text{narrow}}/V_{\text{wide}}$  was set to [0.01, 0.6]  
2091 for mosaics at eccentricities  $\leq 15^\circ$ , to [0.3, 0.9] for eccentricities in  $15^\circ \dots 25^\circ$ , and to  
2092 [0.6, 1.3], for eccentricities  $\geq 25^\circ$ .

2093 The joint manipulation of the tolerance values applied to the parameters of the  
2094 DoG model fit to the vSTF, and to the parameters of the double exponential surround  
2095 pooling model,  $W_s(r)$ , allows for different options for deriving spatial pooling functions  
2096 in synthetic mRGC surrounds.

2097 One option is to set very strict tolerances on the parameters of DoG model fit  
2098 while allowing for a large tolerance in the parameters of  $W_s(r)$ . Results of this choice  
2099 are depicted in the left-most column of Figure B1. A second option would be to allow  
2100 medium tolerance levels in both the DoG model fit and the  $W_s(r)$ . Results of this  
2101 choice are depicted in the middle column of Figure B1. A third option would be to  
2102 enforce strict tolerances in  $W_s(r)$ , for example matching parameters of individual H1  
2103 horizontal cells, while allowing for a loose tolerance in the DoG model fit. Results of  
2104 this choice are depicted in the right column of Figure B1. In the present work, we  
2105 chose the second option.

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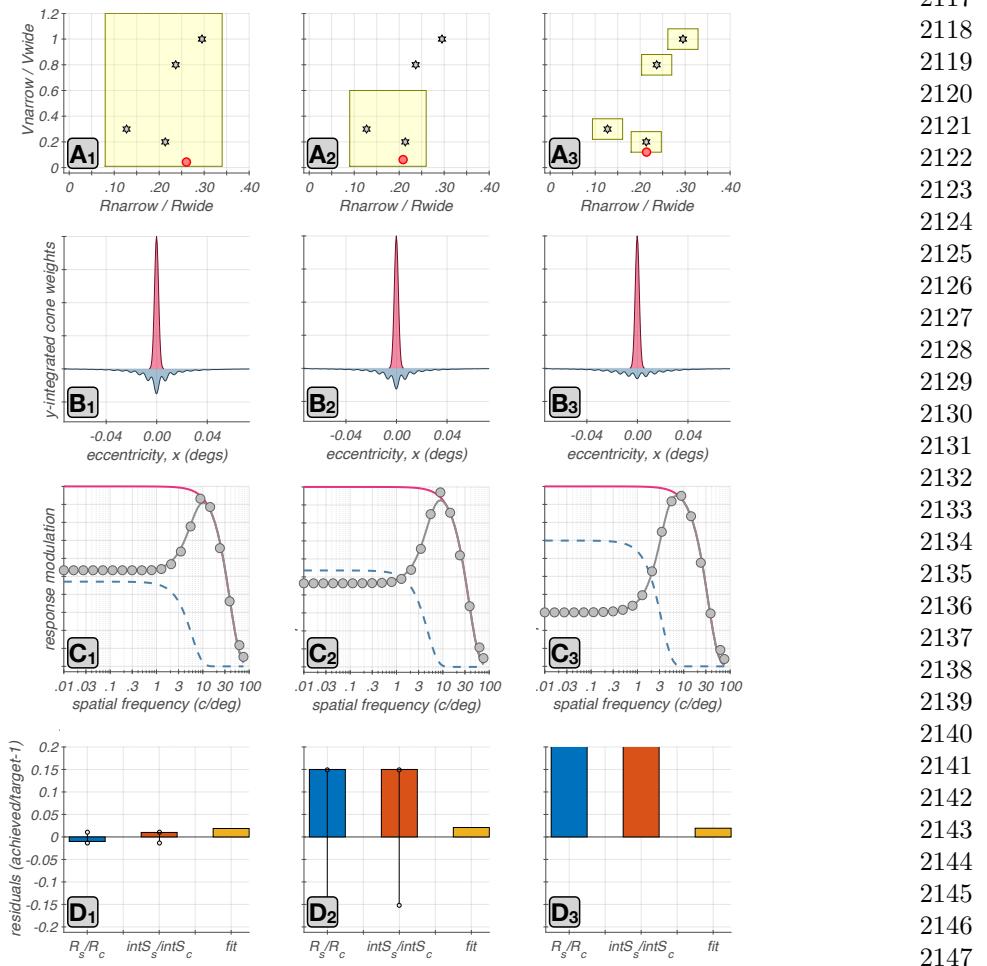
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**Fig. B1 Effect of constraints on surround cone pooling.** Results from three options for constraining the surround optimization. Left column: tight tolerance in the parameters of the DoG model fit to the vSTF and loose tolerance in the parameters of the double exponential surround pooling model,  $W_s(r)$ . Middle column: medium tolerance in both sets of parameters. Right column: loose tolerance in the DoG parameters and tight tolerance in the  $W_s(r)$  parameters. **A1-A3:** The yellow rectangles indicate the tolerance range in the joint space of the two surround cone pooling related parameters,  $V_{\text{narrow}}/V_{\text{wide}}$  and  $R_{\text{narrow}}/R_{\text{wide}}$ . Stars depict the corresponding parameter values in four macaque H1 horizontal cells from the study of Packer & Dacey. The red disk depicts the achieved parameter values under each strategy for an example foveal synthetic mRGC. **B1-B3:** Line weighting functions of the retinal space referred center and surround cone pooling weights under the three examined strategies. **C1-C3:** The vSTF computed under the three strategies (gray disks) and corresponding DOG model fits (gray lines). The red and blue lines depict the center and surround components of the fitted DOG model. **D1-D3:** Blue and orange bars depict the residuals for the ratios of visual space-referred  $R_s/R_c$  and  $K_s/K_c \times (R_s/R_c)^2$  ratios. Black circles connected by a black line depict the enforced tolerance range in these ratios. The enforced tolerance value in D3 was  $\tau = 0.5$ , and is not visualized. The orange bars depict the  $\|\text{vSTF}(\omega) - \text{DOG}(\omega)\|$  residual.

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