Applied Physics Lecture

(Slides from MS Thesis of Melvin Estonactoc)

- Improve the image intensity representation of a camera

#### **Brief History**

#### 1963 – Charles Wyckoff

- high dynamic range film was used by chemically fabricating a multilayer of photographic emulsion with different sensitivities to time of exposures to the impinging light.
- example of a scene captured using the technique is a nuclear explosion

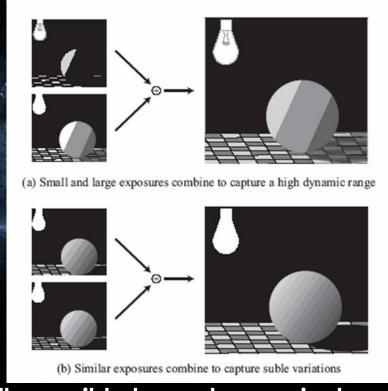
#### 1990's - onwards

- HDR imaging in digital cameras using multiexposure capture

Sequential Exposure Variation – Static Scene

Exposure for each image is controlled and varied by the f-number of the imaging optics or the detector exposure time.

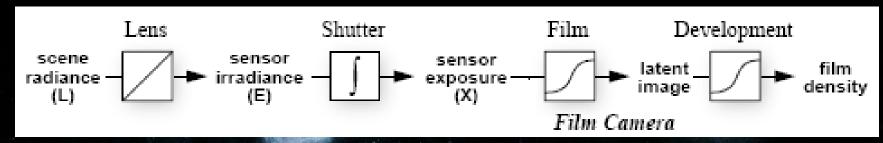
Figure. Capturing a single scene at different exposures. (a) Low and high exposures produced an HDR image but no subtle variations. (b) Same exposure produced subtle variations but with limited dynamic range.



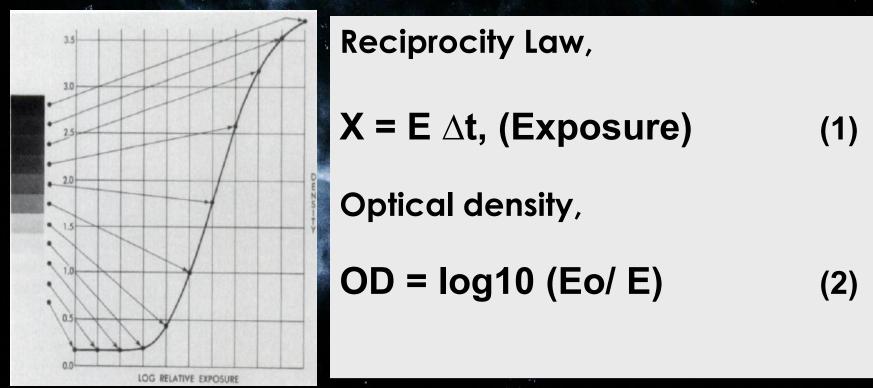
Combining these images is numerically possible to produce a single HDR image.



#### Film Camera Model

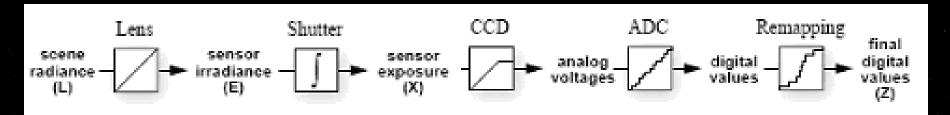


Film camera image acquisition flowchart.



Typical characteristic (H-D) curve of a mammographic film.





#### Digital Image Acquisition Flowchart.

(3)

$$X = f^{-1}(Z) = E\Delta t$$

(4), (5)

$$E = X/\Delta t$$

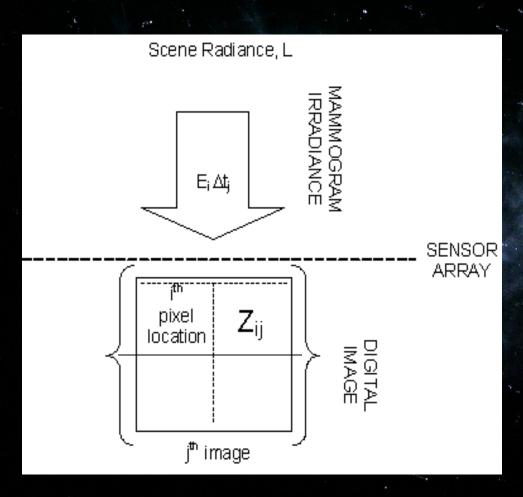
(6)

$$E = f^{-1} (Z)/\Delta t$$

**(7)** 

## **High Dynamic Range Imaging**

Debevec-Malik Algorithm – Response Function Recovery



$$Zij = f(Ei \Delta tj)$$
 (8)

$$f^{-1}(Zij) = Ei\Delta tj$$
 (9)



## **High Dynamic Range Imaging**

**Debevec-Malik Algorithm – Response Function Recovery** 

$$ln[f^{-1}(Zij)] = ln(Ei \Delta tj)$$
 (10)

$$g(Zij) = In(Ei) + In(\Delta tj)$$
 (11)

i ranges over pixels and j ranges over the different exposure durations

Zij and  $\Delta t$ j are known quantities and Ei, and g, are the unknowns.

To determine the estimate values of irradiances Ei's by recovering the function g satisfying Equation (11) in a least square error sense.



## **High Dynamic Range Imaging**

**Debevec-Malik Algorithm – Response Function Recovery** 

Letting Zmax and Zmin be the maximum and minimum integer values of the pixel, N be the number of pixel locations in the image and P the numbers of images, leads to the minimization of the following objective function

$$O = \sum_{i=1}^{N} \sum_{j=1}^{P} \left[ g(Z_{ij}) - \ln E_i - \ln \Delta t_j \right]^2 + \lambda \sum_{z=Z_{min}+1}^{Z_{max}-1} g''(z)^2, (12)$$
optimum least-square error smoothing term

where,

$$g'' = g(z-1) - 2g(z) + g(z+1)$$
 (13)





Debevec-Malik Algorithm – Response Function Recovery

To reduce the influence of saturated pixels and pixel values overridden by the noise of the camera, a weighting function w(Zij) that gives more importance towards the middle gray values is introduced.

$$w(z) = \begin{cases} z - Z_{min} & \text{for } z \leq \frac{1}{2} (Z_{min} + Z_{max}) \\ Z_{max} - z & \text{for } z > \frac{1}{2} (Z_{min} + Z_{max}) \end{cases}$$
(14)



Debevec-Malik Algorithm – Response Function Recovery

$$O = \sum_{i=1}^{N} \sum_{j=1}^{P} \{w(Z_{ij}) [g(Z_{ij}) - InE_{i} - In\Delta t_{j}]\}^{2}$$

$$+ \lambda \sum_{z=Z_{min}+1}^{Z_{max}-1} (w(Z_{ij})g''(z))^{2}$$
(15)

The best possible solutions to the objective function that is quadratic in g(z)'s and Ei's are obtained using singular value decomposition (SVD), which is a method of choice for solving most linear least-squares problems.



Debevec-Malik Algorithm – HDR Image Pixel Values

After solving g,

$$InEi = g(Zij) - In\Delta tj$$
 (16)

To recover the irradiance per pixel, P images of varying exposures are obtained and combined. Since parts of these images will once again have saturated or underexposed values, we employ once again a weighted average over P images using w(Zij) to Equation (16) to obtain a more reliable estimate of Ei, that is,

$$InE_{i} = \frac{\sum_{j=1}^{P} w(Z_{ij}) (g(Z_{ij}) - In \Delta t_{j})}{\sum_{j=1}^{P} w(Z_{ij})}$$
(17)





**HDR Optical Density Image** 

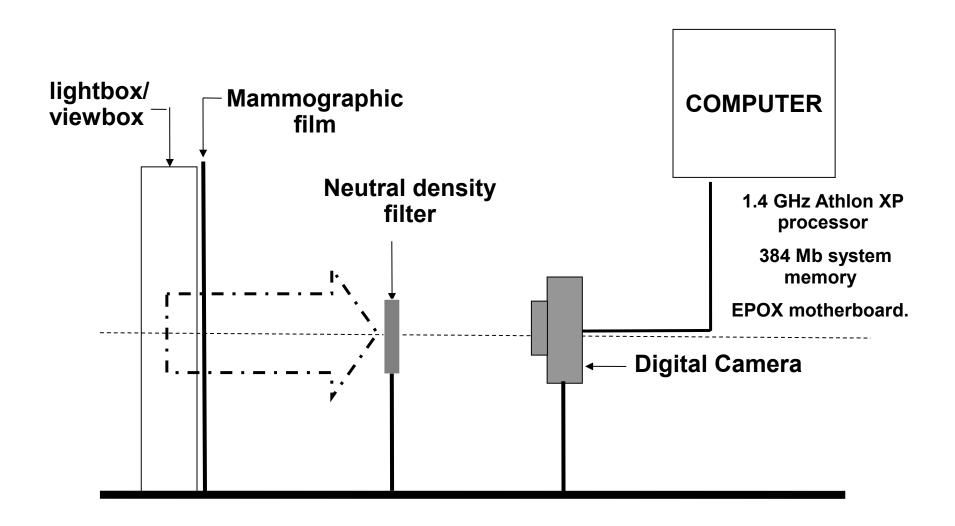
From equation (17)

$$OD = log10(Eo/Ei)$$
 (18)

**Pixel OD values** 

ODi = 
$$log10(Eo,i) - log10(Ei)$$
 (19)

# METHODOLOGY Mammographic Film Digitization/ Image Acquisition



Imaging/ Digitizer set-up schematic diagram.

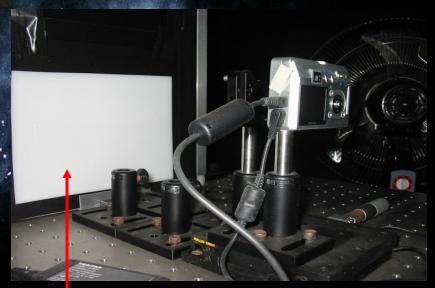
## **METHODOLOGY**



Parameter	Setting
F-number	5.6
ISO speed ratings	400
Subject distance range	Macro
Metering Mode	Pattern
Pixel Dimension	1028 x768 pixels
<b>Exposure Values</b>	(-)2 to (+)2, 1/3EV increment

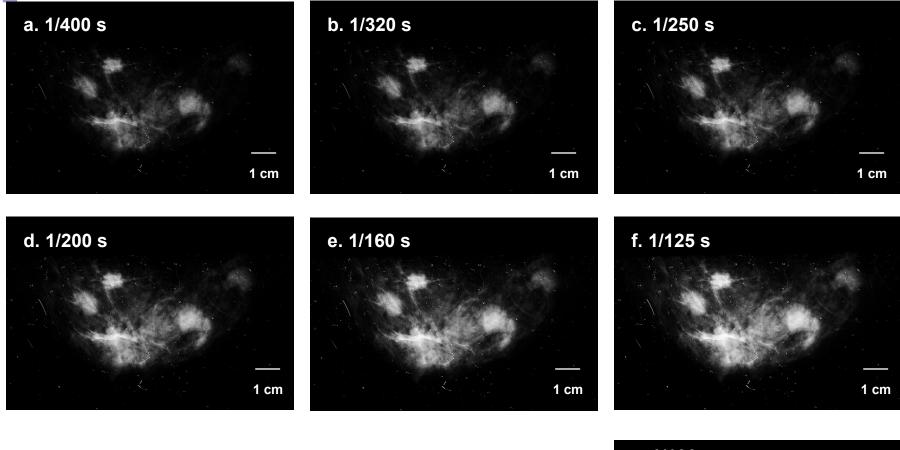
Pentax Optio \$50 Digital Camera

ND filter optical mount

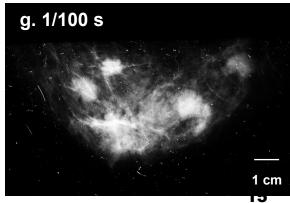


Lightbox/ Viewbox

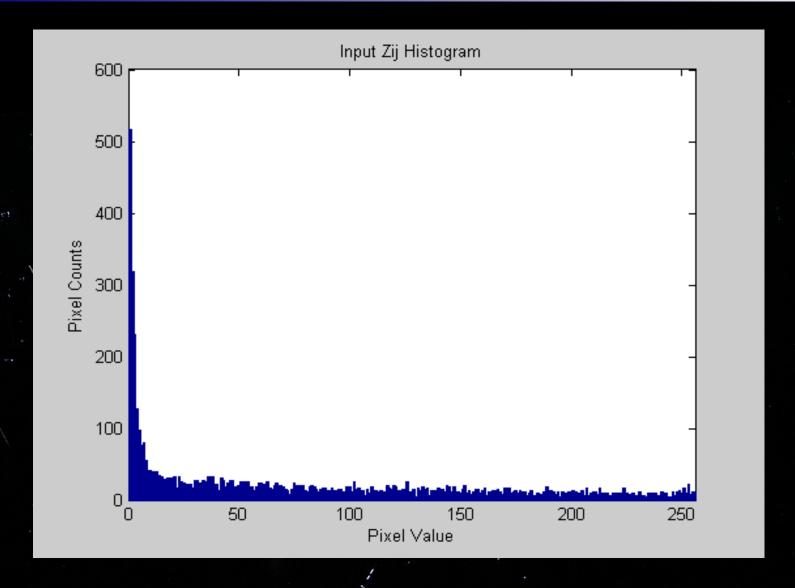
#### RESULTS



Figures (a-g). Grayscale digital images of the mammogram captured in order of increasing exposure time. DSC f-number is f/5.6 for all images. Cropped image size is 500 x 800 pixels.

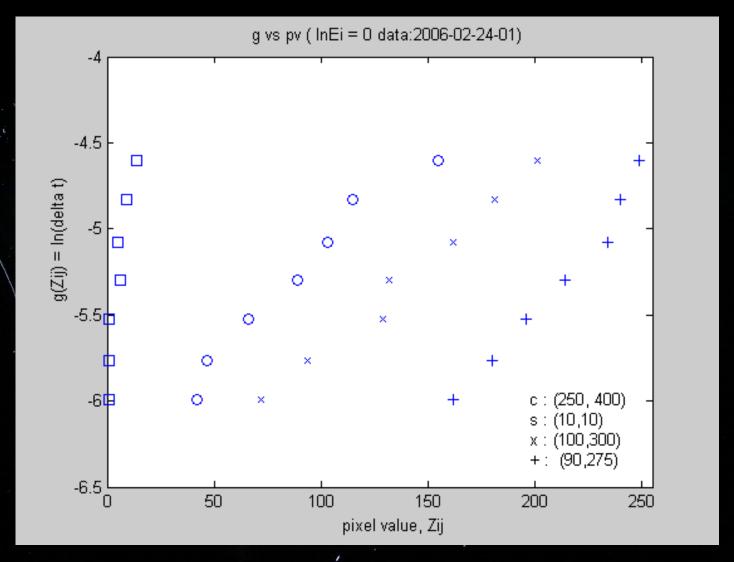






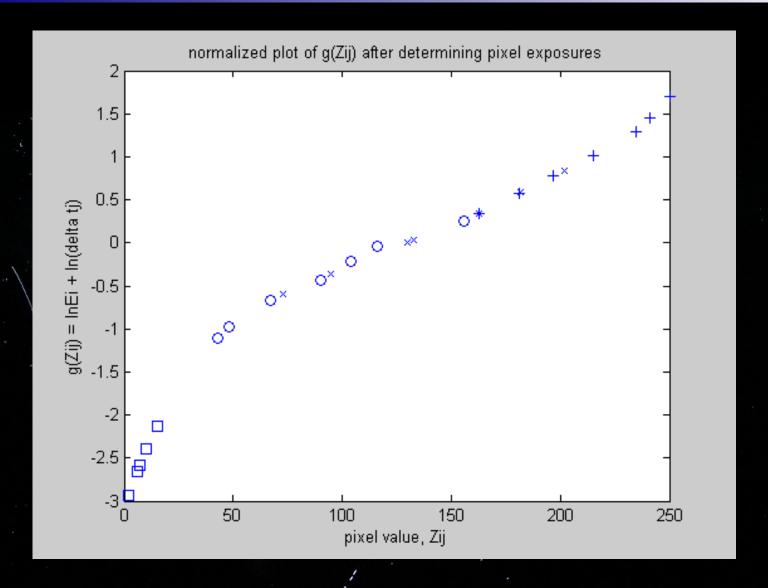
Histogram of the input pixel matrix from the selected pixels of each image.





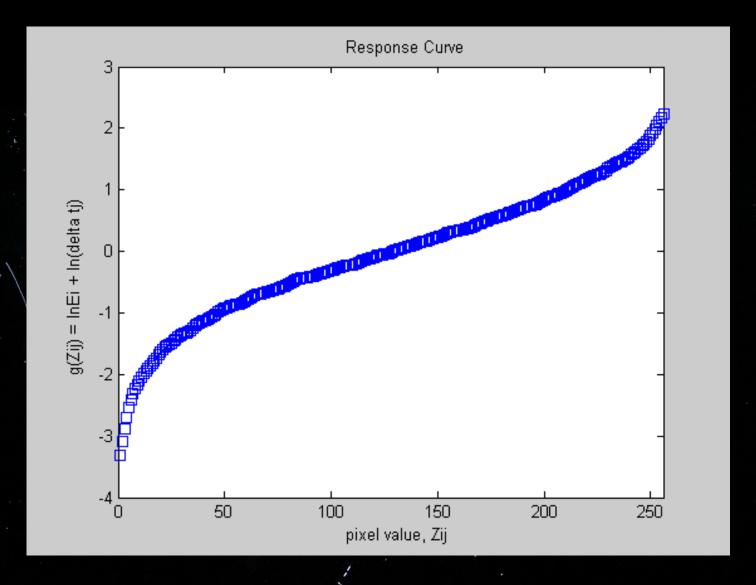
Samples of the response curve derived from the digital values of 4 pixel locations for 7 different known exposures using the equation  $g(Zij) = log(Ei) + log(\Delta tj)$  where logEi = 0 initially.





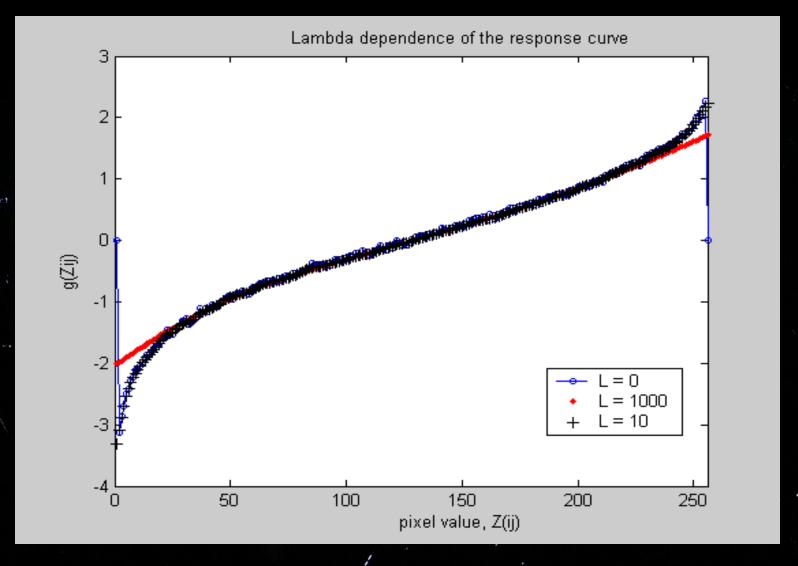
Aligned response curve of the segments in Figure 3.4 after determining Ei's.



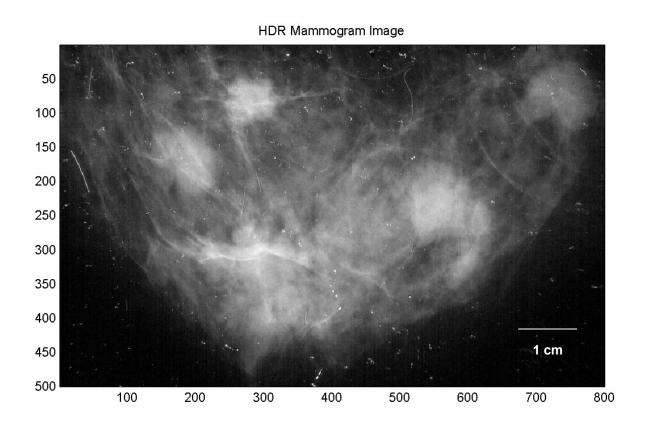


The system response curve determined by the Debevec-Malik algorithm.

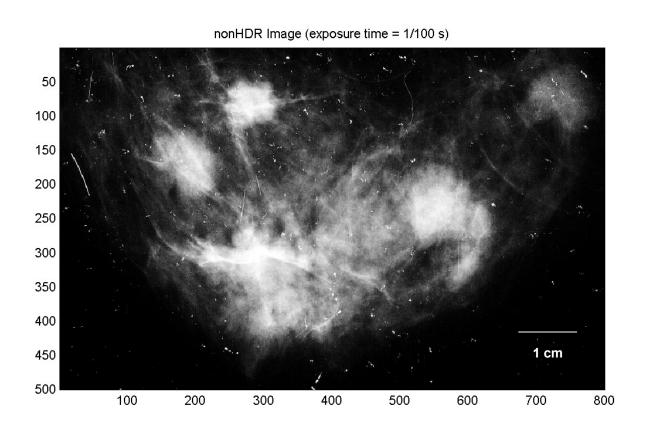




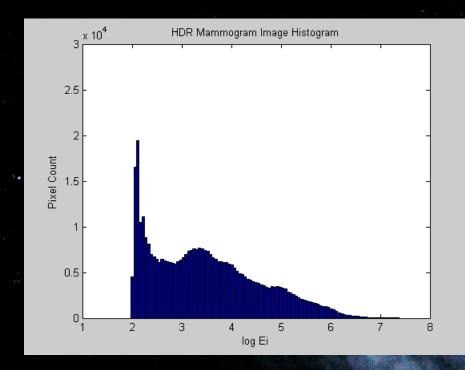
Smoothness factor, lambda, dependence of the response curve.

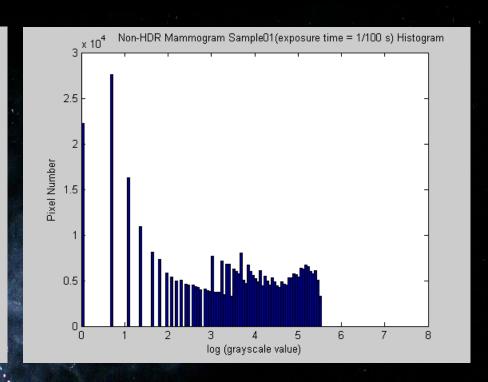


Reconstructed HDR mammogram image mapped into grayscale. Computed relative Ei values = [7.2549, 1.6117e+003].

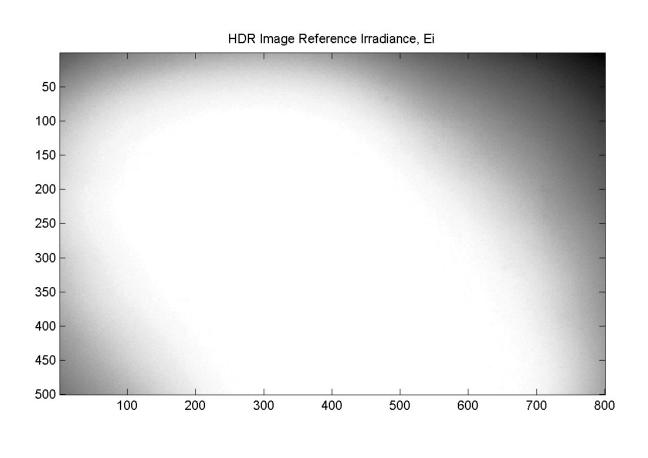


Non-HDR mammogram JPEG image format represented by 8-bit intensity gray levels. DSC exposure time is 1/100 s.



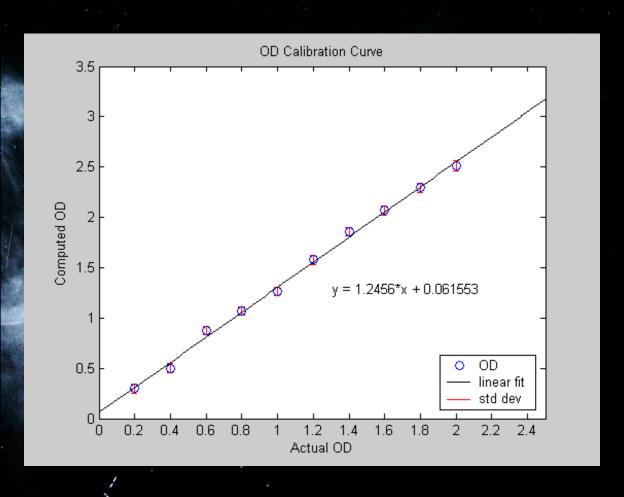


Mammogram Image Histograms. (a) HDR-OD image (b) LDR JPEG image



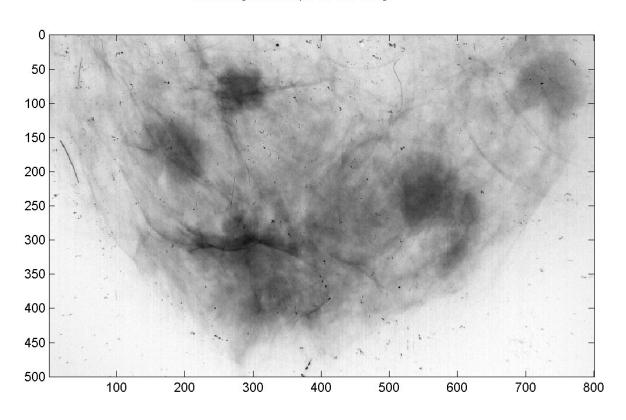
HDR image of the reference irradiance. Eo values [5.9838e+003, 1.7228e+004].

Actual OD	Computed Mean OD
0.2	0.2998 ± 0.0443
0.4	0.4992 ± 0.0436
0.6	0.8734 ± 0.0429
0.8	1.0733 ± 0.0418
1.0	1.2641 ± 0.0422
1.2	1.5769 ± 0.0420
1.4	1.8547 ± 0.0420
1.6	2.0711 ± 0.0457
1.8	2.2940 ± 0.0486
2.0	2.5104 ± 0.0526

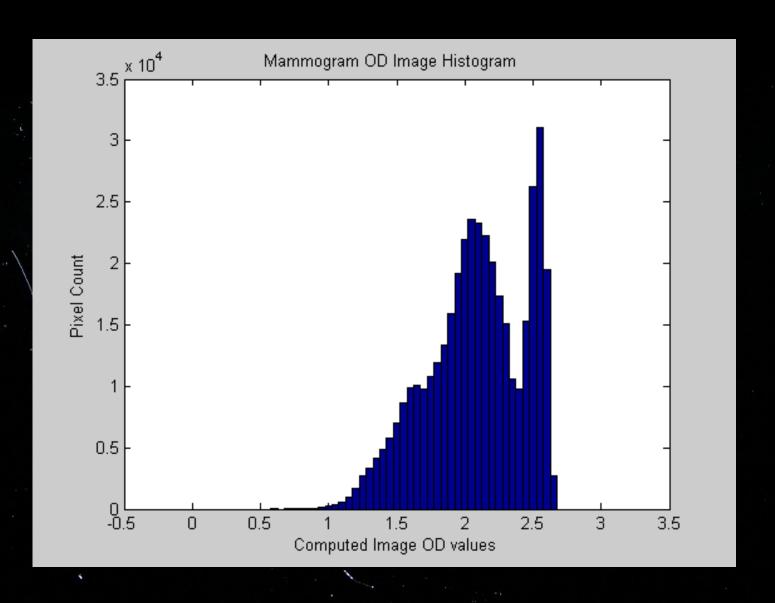


Optical density calibration curve.





Calibrated OD image of an HDR mammogram image.



HDR-OD image histogram.

## High Dynamic Range Imaging of Magnetized Sheet Plasma

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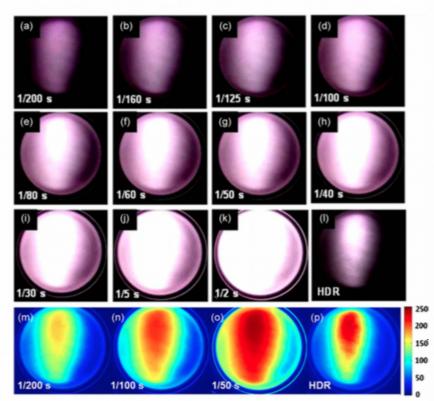


Fig. 1. Contrast-stretch ed LDR images of a magnetized sheet plasma tak en at various shutter speeds: (a) 1/200, (b) 1/160, (c) 1/125, (d) 1/100, (e) 1/80, (f) 1/60, (g) 1/50, (h) 1/40, (i) 1/30, (j) 1/5, and (k) 1/2 s. (l) False-color images of (m) 1/200, (n) 1/100, and (o) 1/50 s, and (p) HDR image. A jet color map is us ed for the scalin g of the intensity values of the images.

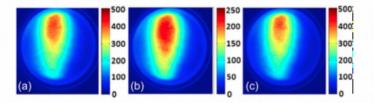


Fig. 2. Radiance maps obtained from the response functions for various channels: (a) red, (b) green, and (c) blue.

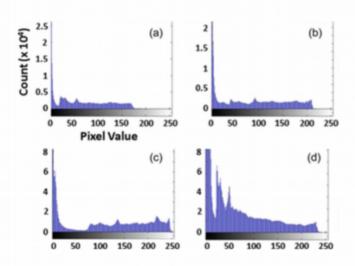


Fig. 3. Intensity histograms of LDR images taken at various shutter speeds of (a) 1/200, (b) 1/100, and (c) 1/50 s and (d) of linear tone mapped HDR image.

https://www.youtube.com/watch?v=nPfcwT4Fcy8

NASA's New High Dynamic Range Camera Records Rocket Test