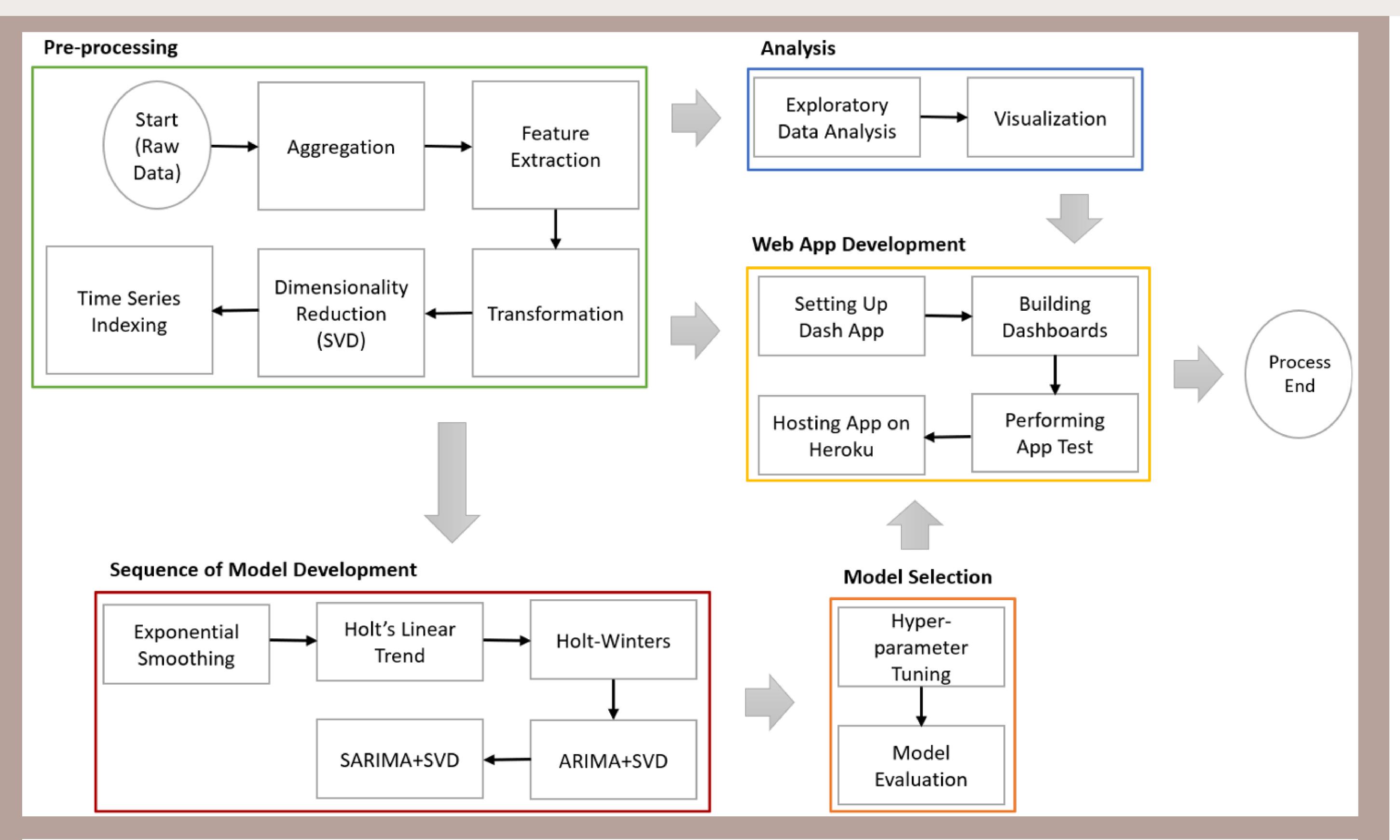
Web Application to Evaluate Statistical Time Series Forecast Models: Application to Walmart Sales

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MULTIPLICATIVE HOLT-WINTERS

Level	$\ell_t = \alpha(y_t/sn_{t-L}) + (1-\alpha)(\ell_{t-1} + b_{t-1})$	
Growth Rate	$b_t = \gamma(\ell_t - \ell_{t-1}) + (1 - \gamma)(b_{t-1})$	
Seasonal Factor	$sn_t = \delta(y_t/\ell_t) + (1 - \delta)(sn_{t-L})$	
In-sample Forecast	$\hat{y}_t = (\ell_{t-1} + b_{t-1}) s n_{t-L}$	
Out-of-sample Forecast	$\hat{y}_{T+\tau} = (\ell_T + \tau b_T) s n_{T+\tau-L}$ for $\tau = 1, 2, \cdots$	
Relative Standard Error	$s_r = \sqrt{\frac{\sum_{t=1}^{T} \left[\frac{y_t - (\ell_{t-1} + b_{t-1}) s n_{t-L}}{(\ell_{t-1} + b_{t-1}) s n_{t-L}} \right]^2}{T - 3}}$	
95% Prediction Interval	$\left[\hat{y}_{T+\tau}(T) \pm z_{[.025]} s_r(\sqrt{c_\tau}) (sn_{T+\tau-L})\right]$ • If $\tau=1$ then $c_1=(\ell_T+b_T)^2$	
	• If $2 \le \tau \le L$ then $c_{\tau} = \sum_{j=1}^{\tau-1} \alpha^2 (1 + [\tau - j] \gamma)^2 (\ell_T + jb_T)^2 + (\ell_T + \tau b_T)^2$	

EXPONENTIAL SMOOTHING

Level	$\ell_t = \alpha y_t + (1 - \alpha)\ell_{t-1}$
In-sample Forecast	$\hat{y}_t = \ell_{t-1}$
Out-of-sample Forecast	$\hat{y}_{T+\tau} = \ell_T \text{for} \tau = 1, 2, \cdots$
Standard Error	$s = \sqrt{\frac{SSE}{T - 1}}$
95% Prediction Interval	$\left[\ell_T \pm z_{[.025]} s \sqrt{1 + (\tau - 1)\alpha^2}\right]$

HOLT'S LINEAR TREND

Level	$\ell_t = \alpha y_t + (1 - \alpha)(\ell_{t-1} - b_{t-1})$
Growth Rate	$b_{t} = \gamma(\ell_{t} - \ell_{t-1}) + (1 - \gamma)b_{t-1}$
In-sample Forecast	$\hat{y}_t = \ell_{t-1} + b_{t-1}$
Out-of-sample Forecast	$\hat{y}_{T+\tau} = \ell_T + \tau b_T$ for $\tau = 1, 2, \cdots$
Standard Error	$s = \sqrt{\frac{SSE}{T-2}}$

95% Prediction Interval

If $\tau = 1$:

$$[(\ell_T + b_T) \pm z_{[.025]}s]$$

If $\tau \geq 2$:

$$\left[(\ell_T + \tau b_T) \pm z_{[.025]} s \sqrt{1 + \sum_{j=1}^{\tau-1} \alpha^2 (1 + j\gamma)^2} \right]$$

REFERENCES

- [1] Bowerman, B. L., O'connell, R. T., & Koehler, A. B. (2005). Forecasting, time series, and regression: an applied approach. Thomson Brooks/Cole.
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