
Title

binspwc — Data-Driven Nonparametric Pairwise Group Comparison using Binscatter.

Syntax

```
binspwc \underline{depvar} indvar [othercovs] [\underline{if}] [\underline{in}] [\underline{weight}] , by(varname) [ 2024
```

```
estmethod(cmdname) deriv(v) at(position) nolink
absorb(absvars) reghdfeopt(reghdfe_option)
pwc(pwcopt) testtype(type) lp(metric)
bins(p s) bynbins(bynbinsopt) binspos(position) binsmethod(method)
nbinsrot(#) samebinsby randcut(#)
pselect(numlist) sselect(numlist)
nsims(#) simsgrid(#) simsseed(seed)
dfcheck(n1 n2) masspoints(masspointsoption)
vce(vcetype) asyvar(on/off) estmethodopt(cmd_option)
usegtools(on/off) ]
```

where <u>depvar</u> is the dependent variable, <u>indvar</u> is the independent variable for binning, and <u>othercovs</u> are other covariates to be controlled for.

The degree of the piecewise polynomial p, the number of smoothness constraints s, and the derivative order v are integers satisfying $\emptyset \le s,v \le p$, which can take different values in each case.

fweights, aweights and pweights are allowed; see weight.

Description

binspwc implements binscatter-based hypothesis testing procedures for
 pairwise group comparison of binscatter estimators, following the
 results in <u>Cattaneo, Crump, Farrell and Feng (2024a)</u> and <u>Cattaneo,</u>
 <u>Crump, Farrell and Feng (2024b)</u>. If the binning scheme is not set by
 the user, the companion command <u>binsregselect</u> is used to implement
 binscatter in a data-driven (optimal) way and inference procedures are
 based on robust bias correction. Binned scatter plots based on
 different models can be constructed using the companion commands
 binsreg, binsgreg, binslogit and binsprobit.

A detailed introduction to this command is given in Cattaneo, Crump,



<u>Farrell and Feng (2024c)</u>. Companion R and Python packages with the same capabilities are available (see website below).

Companion commands: <u>binsreg</u> for binscatter least squares regression with robust inference procedures and plots, <u>binsqreg</u> for binscatter quantile regression with robust inference procedures and plots, <u>binslogit</u> for binscatter logit estimation with robust inference procedures and plots, <u>binsprobit</u> for binscatter probit estimation with robust inference procedures and plots, and <u>binsregselect</u> for data-driven (optimal) binning selection.

Related Stata, R and Python packages are available in the following website:

https://nppackages.github.io/

Options

Estimand

by(varname) specifies the variable containing the group indicator to perform subgroup analysis; both numeric and string variables are supported. When by(varname) is specified, binspwc implements estimation for each subgroup separately and then conduct all pairwise comparison tests. By default, the binning structure is selected for each subgroup separately, but see the option samebinsby below for imposing a common binning structure across subgroups. This option is required.

estmethod(cmdname) specifies the binscatter model. The default is
 estmethod(reg), which corresponds to the binscatter least squares
 regression. Other options are: estmethod(qreg #) for binscatter
 quantile regression where # is the quantile to be estimated,
 estmethod(logit) for binscatter logistic regression and
 estmethod(probit) for binscatter probit regression.

deriv(v) specifies the derivative order of the regression function for estimation, testing and plotting. The default is deriv(0), which corresponds to the function itself.

at(position) specifies the values of othercovs at which the estimated
function is evaluated for plotting. The default is at(mean), which
corresponds to the mean of othercovs. Other options are: at(median) for
the median of othercovs, at(0) for zeros, and at(filename) for
particular values of othercovs saved in another file.



- Note: When at(mean) or at(median) is specified, all factor variables in othercovs (if specified) are excluded from the evaluation (set as zero).
- nolink specifies that the function within the inverse link (logistic)
 function be reported instead of the conditional probability function.
 This option is used only if logit or probit model is specified in
 estmethod().

| Г | | 1 |
|---|---------|---|
| | Reahdfe | L |

- absorb(absvars) specifies categorical variables (or interactions)
 representing the fixed effects to be absorbed. This is equivalent to
 including an indicator/dummy variable for each category of each absvar.
 When absorb() is specified, the community-contributed command reghdfe
 instead of the command regress is used.
- reghdfeopt(reghdfe_option) options to be passed on to the command reghdfe.
 Important: absorb() and vce() should not be specified within this
 option.
- For more information about the community-contributed command **reghdfe**, please see http://scorreia.com/software/reghdfe/.

| Pairwise Group | Comparison | Testing | L |
|--------------------|------------|---------|---|

- pwc(pwcopt) sets the degree of polynomial and the number of smoothness
 constraints for pairwise group comparison. If pwc(p s) is specified, a
 piecewise polynomial of degree p with s smoothness constraints is used.
 If pwc(T) or pwc() is specified, pwc(1 1) is used unless the degree p
 or smoothness s selection is requested via the option pselect() or
 sselect() (see more details in the explanation of pselect() and
 sselect()). The default is pwc().
- **testtype**(*type*) specifies the type of pairwise comparison test. The default is **testtype**(2), which corresponds to a two-sided test of the form H0: $mu_{-}1(x)=mu_{-}2(x)$. Other options are: **testtype**(l) for the one-sided test of the form H0: $mu_{-}1(x) <= mu_{-}2(x)$ and **testtype**(r) for the one-sided test of the form H0: $mu_{-}1(x) >= mu_{-}2(x)$.
- lp(metric) specifies an Lp metric used to test for the difference between
 two groups. The default is lp(inf), which corresponds to the sup-norm.
 Other options are lp(q) for a positive number q no less than 1. Note
 that lp(inf) ("sup norm") has to be used for one-sided tests.



Binning/Degree/Smoothness Selection

- bins(p s) sets a piecewise polynomial of degree p with s smoothness constraints for data-driven (IMSE-optimal) selection of the partitioning/binning scheme. The default is bins(0 0), which corresponds to the piecewise constant.
- bynbins(bynbinsopt) sets the number of bins for partitioning/binning of
 indvar. If bynbins(numlist) is specified, the number in the numlist is
 applied to the binscatter estimation for each group. The ordering of
 the group follows the result of tabulate. If a single number of bins is
 specified, it applies to the estimation for all groups. If bynbins(T)
 or bynbins() (default) is specified, the number of bins is selected via
 the companion command binsregselect in a data-driven, optimal way
 whenever possible.
- Note: If a *numlist* with more than one number is supplied within **bynbins()**, it is understood as the number of bins applied to binscatter estimation for each subgroup rather than the range for selecting the number of bins.
- binspos(position) specifies the position of binning knots. The default is binspos(qs), which corresponds to quantile-spaced binning (canonical binscatter). Other options are: es for evenly-spaced binning, or a numlist for manual specification of the positions of inner knots (which must be within the range of indvar).
- binsmethod(method) specifies the method for data-driven selection of the number of bins via the companion command <u>binsregselect</u>. The default is binsmethod(dpi), which corresponds to the IMSE-optimal direct plug-in rule. The other option is: rot for rule of thumb implementation.
- nbinsrot(#) specifies an initial number of bins value used to construct the DPI number of bins selector. If not specified, the data-driven ROT selector is used instead.
- samebinsby forces a common partitioning/binning structure across all
 subgroups specified by the option by(). The knots positions are
 selected according to the option binspos() and using the full sample.
 If nbins() is not specified, then the number of bins is selected via
 the companion command binsregselect and using the full sample.
- randcut(#) specifies the upper bound on a uniformly distributed variable
 used to draw a subsample for bins/degree/smoothness selection.
 Observations for which runiform()<=# are used. # must be between 0 and</pre>

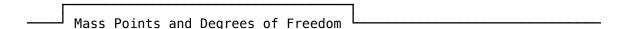


- 1. By default, max(5000, 0.01n) observations are used if the samples size n>5000.
- pselect(numlist) specifies a list of numbers within which the degree of polynomial p for point estimation is selected. If the selected optimal degree is p, then piecewise polynomials of degree p+1 are used to conduct pairwise group comparison.
- sselect(numlist) specifies a list of numbers within which the number of
 smoothness constraints s for point estimation is selected. If the
 selected optimal smoothness is s, then piecewise polynomials with s+1
 smoothness constraints are used to conduct pairwise group comparison.
 If not specified, for each value p supplied in the option pselect(),
 only the piecewise polynomial with the maximum smoothness is
 considered, i.e., s=p.
- Note: To implement the degree or smoothness selection, in addition to pselect() or sselect(), bynbins(numlist) must be specified.

| 1 | | 7 |
|---|------------|---|
| | Simulation | 1 |

- **nsims(#)** specifies the number of random draws for hypothesis testing. The default is nsims(500), which corresponds to 500 draws from a standard Gaussian random vector of size [(p+1)*J (J-1)*s]. Setting at least nsims(2000) is recommended to obtain the final results.
- simsgrid(#) specifies the number of evaluation points of an evenly-spaced
 grid within each bin used for evaluation of the supremum (infimum or Lp
 metric) operation needed to construct confidence bands and hypothesis
 testing procedures. The default is simsgrid(20), which corresponds to
 20 evenly-spaced evaluation points within each bin for approximating
 the supremum (infimum or Lp metric) operator. Setting at least
 simsgrid(50) is recommended to obtain the final results.

simsseed(#) sets the seed for simulations.



dfcheck(n1 n2) sets cutoff values for minimum effective sample size checks,
 which take into account the number of unique values of indvar (i.e.,
 adjusting for the number of mass points), number of clusters, and
 degrees of freedom of the different statistical models considered. The
 default is dfcheck(20 30). See Cattaneo, Crump, Farrell and Feng
 (2024c) for more details.



masspoints(masspointsoption) specifies how mass points in indvar are handled. By default, all mass point and degrees of freedom checks are implemented. Available options:

masspoints(noadjust) omits mass point checks and the corresponding
effective sample size adjustments.

masspoints(nolocalcheck) omits within-bin mass point and degrees of freedom checks.

masspoints(off) sets masspoints(noadjust) and masspoints(nolocalcheck)
simultaneously.

masspoints(veryfew) forces the command to proceed as if indvar has only a few number of mass points (i.e., distinct values). In other words, forces the command to proceed as if the mass point and degrees of freedom checks were failed.

Other Options

vce(<u>vcetype</u>) specifies the vcetype for variance estimation used by the commands <u>regress</u>, <u>logit</u>, <u>logit</u>, <u>qreg</u> or **reghdfe**. The default is vce(robust).

asyvar(on/off) specifies the method used to compute standard errors. If
asyvar(on) is specified, the standard error of the nonparametric
component is used and the uncertainty related to other control
variables othercovs is omitted. Default is asyvar(off), that is, the
uncertainty related to othercovs is taken into account.

estmethodopt(cmd_option) options to be passed on to the estimation command specified in estmethod(). For example, options that control for the optimization process can be added here.

usegtools(on/off) forces the use of several commands in the community-distributed Stata package gtools to speed the computation up, if on is specified. Default is usegtools(off).

For more information about the package **gtools**, please see https://gtools.readthedocs.io/en/latest/index.html.

Examples

Setup

sysuse auto

Generate two groups

gen group=price>5000

Test for the difference between two groups



binspwc mpg weight foreign, by(group)

Stored results

```
Scalars
  e(N)
                   number of observations
  e(p)
                   degree of polynomial for bin selection
                   smoothness of polynomial for bin selection
  e(s)
                   degree of polynomial for testing
  e(pwc p)
  e(pwc_s)
                   smoothness of polynomial for testing
Macros
  e(byvalue)
                   name of groups found in by()
Matrices
  e(N by)
                   number of observations for each group
  e(Ndist_by)
                   number of distinct values for each group
                   number of clusters for each group
  e(Nclust_by)
                   number of bins for each group
  e(nbins_by)
  e(stat)
                   test statistics for all pairwise comparisons
  e(pval)
                   p values for all pairwise comparisons
  e(imse_var_rot) variance constant in IMSE, ROT selection
  e(imse_bsq_rot) bias constant in IMSE, ROT selection
  e(imse_var_dpi) variance constant in IMSE, DPI selection
  e(imse_bsq_dpi) bias constant in IMSE, DPI selection
```

References

```
Cattaneo, M. D., R. K. Crump, M. H. Farrell, and Y. Feng. 2024a. On Binscatter. American Economic Review 114(5): 1488–1514.
```

Cattaneo, M. D., R. K. Crump, M. H. Farrell, and Y. Feng. 2024b. <u>Nonlinear Binscatter Methods</u>. Working Paper.

Cattaneo, M. D., R. K. Crump, M. H. Farrell, and Y. Feng. 2024c.

<u>Binscatter Regressions</u>. Working Paper.

<u>Authors</u>

Matias D. Cattaneo, Princeton University, Princeton, NJ. cattaneo@princeton.edu.

Richard K. Crump, Federal Reserve Band of New York, New York, NY. richard.crump@ny.frb.org.

Max H. Farrell, UC Santa Barbara, Santa Barbara, CA. mhfarrell@gmail.com.



Yingjie Feng, Tsinghua University, Beijing, China. fengyingjiepku@gmail.com.

