

Package ‘lpcde’

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Type Package

Title Boundary Adaptive Local Polynomial Conditional Density Estimator

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Description Tools for estimation and inference of conditional densities, derivatives and functions. This is the companion software for Cattaneo, Chandak, Jansson and Ma (2022).

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basis_vec	<i>Unit basis vector</i>
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Description

Function to generate unit basis vector according to polynomial order and derivative order. This function returns unit vector that is the same size as the vector returned by `poly_base(x, p)`.

Usage

```
basis_vec(x, p, mu)
```

Arguments

x	sample input scalar or vector.
p	polynomial order.
mu	derivative order.

Value

Vector of appropriate length with ones corresponding to entries of order mu.

Examples

```
basis_vec(x = 2, p = 5, mu = 1)
```

coef.lpbwcde	<i>Coef Method for Local Polynomial Density Bandwidth Selection</i>
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Description

The coef method for local polynomial density bandwidth selection objects.

Usage

```
## S3 method for class 'lpbwcd'
coef(object, ...)
```

Arguments

object	Class "lpbwcd" object, obtained by calling lpbwcd .
...	Other arguments.

Value

Estimates A matrix containing y_grid points and selected bandwidths.

Author(s)

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Xinwei Ma, University of California San Diego. <x1ma@ucsd.edu>.

See Also

[lpbwcd](#) for data-driven bandwidth selection.

Supported methods: [coef.lpbwcd](#), [print.lpbwcd](#), [summary.lpbwcd](#).

coef.lpcde	<i>Coef Method</i>
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Description

The coef method for local polynomial conditional density objects.

Usage

```
## S3 method for class 'lpcde'
coef(object, ...)
```

Arguments

object Class "lpcde" object, obtained by calling [lpcde](#).
 ... Additional options.

Details

Coef Method for Local Polynomial Density Conditional Estimation and Inference

Value

outputs A matrix containing the estimates

Author(s)

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Michael Jansson, University of California Berkeley. <mjansson@econ.berkeley.edu>.

Xinwei Ma, University of California San Diego. <x1ma@ucsd.edu>.

See Also

[lpcde](#) for local polynomial conditional density estimation.

Supported methods: [coef.lpcde](#), [confint.lpcde](#), [plot.lpcde](#), [print.lpcde](#), [summary.lpcde](#), [vcov.lpcde](#)

confint.lpcde	<i>Confint Method for Local Polynomial Density Conditional Estimation and Inference</i>
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Description

The confint method for local polynomial conditional density objects.

Usage

```
## S3 method for class 'lpcde'
confint(
  object,
  parm = NULL,
  level = NULL,
  CIuniform = FALSE,
  CIsimul = 2000,
  alpha = 0.05,
  ...
)
```

Arguments

object	Class "lpcde" object, obtained by calling lpcde .
parm	Integer, indicating which parameters are to be given confidence intervals.
level	Numeric scalar between 0 and 1, the significance level for computing confidence intervals
CIuniform	TRUE or FALSE (default), plotting either pointwise confidence intervals (FALSE) or uniform confidence bands (TRUE).
CIsimul	Positive integer, specifies the number of simulations used to construct critical values (default is 2000). This option is ignored if CIuniform=FALSE.
alpha	Numeric scalar between 0 and 1, specifies the significance level for plotting confidence intervals/bands.
...	Additional options, including (i) grid specifies a subset of grid points to display the bandwidth; (ii) gridIndex specifies the indices of grid points to display the bandwidth (this is the same as parm);(iii) CIuniform specifies whether displaying pointwise confidence intervals (FALSE, default) or the uniform confidence band (TRUE); (iv) CIsimul specifies the number of simulations used to construct critical values (default is 2000).

Value

Estimate	A matrix containing grid points, estimates and confidence interval end points using p- and q-th order local polynomials as well as bias-corrected estimates and corresponding confidence intervals.
crit_val	the critical value used in computing the confidence interval end points.

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See Also

[lpcde](#) for local polynomial conditional density estimation.

Supported methods: [coef.lpcde](#), [confint.lpcde](#), [plot.lpcde](#), [print.lpcde](#), [summary.lpcde](#), [vcov.lpcde](#)

lpbwcde

Data-driven Bandwidth Selection for Local Polynomial Conditional Density Estimators

Description

[lpbwcde](#) implements the bandwidth selection methods for local polynomial based conditional density (and derivatives) estimation proposed and studied in Cattaneo, Chandak, Jansson and Ma (2021).

Companion command: [lpcde](#) for estimation and robust bias-corrected inference.

Related Stata and R packages useful for nonparametric estimation and inference are available at <https://nppackages.github.io/>.

Usage

```
lpbwcde(
  y_data,
  x_data,
  x,
  y_grid = NULL,
  p = NULL,
  q = NULL,
  mu = NULL,
  nu = NULL,
  kernel_type = c("epanechnikov", "triangular", "uniform"),
  bw_type = c("mse-rot", "imse-rot")
)
```

Arguments

y_data	Numeric matrix/data frame, the raw data of independent.
x_data	Numeric matrix/data frame, the raw data of covariates.
x	Numeric, specifies the evaluation point in the x-direction. Default is median of the dataset.
y_grid	Numeric, specifies the grid of evaluation points. When set to default, grid points will be chosen as 0.05-0.95 percentiles of the data, with a step size of 0.05.

p	Nonnegative integer, specifies the order of the local polynomial for Y used to construct point estimates. (Default is 2.)
q	Nonnegative integer, specifies the order of the local polynomial for X used to construct point estimates. (Default is 1.)
mu	Nonnegative integer, specifies the derivative with respect to Y of the distribution function to be estimated. 0 for the distribution function, 1 (default) for the density function, etc.
nu	Nonnegative integer, specifies the derivative with respect to X of the distribution function to be estimated.
kernel_type	String, specifies the kernel function, should be one of "triangular", "uniform" or "epanechnikov".
bw_type	String, specifies the method for data-driven bandwidth selection. This option will be ignored if bw is provided. Implementable with "mse-rot" (default, mean squared error-optimal bandwidth selected for each grid point)

Value

BW	A matrix containing (1) y_grid (grid point), (2) bw (bandwidth)
opt	A list containing options passed to the function.

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Examples

```
# Generate a random sample
set.seed(42);
x_data = rnorm(2000)
y_data = rnorm(2000, mean=x_data)
x = 0

# Construct bandwidth
bw1 <- lpbwcd(y_data = y_data, x_data = x_data, x=x, bw_type = "mse-rot")
summary(bw1)

# Display bandwidths for a subset of y_grid points
summary(bw1, y_grid=bw1$BW[2:5, "y_grid"])
```

lpcde

*Local Polynomial Conditional Density Estimation***Description**

`lpcde` implements the local polynomial regression based conditional density (and derivatives). The estimator proposed in Chandak, Cattaneo, Jansson and Ma. Robust bias-corrected inference methods, both pointwise (confidence intervals) and uniform (confidence bands), are also implemented.

Usage

```
lpcde(
  x_data,
  y_data,
  y_grid = NULL,
  x = NULL,
  bw = NULL,
  p = NULL,
  q = NULL,
  p_RBC = NULL,
  q_RBC = NULL,
  mu = NULL,
  nu = NULL,
  rbc = TRUE,
  ng = NULL,
  kernel_type = c("epanechnikov", "triangular", "uniform"),
  bw_type = "mse-rot"
)
```

Arguments

<code>x_data</code>	Numeric matrix/data frame, the raw data of covariates.
<code>y_data</code>	Numeric matrix/data frame, the raw data of independent.
<code>y_grid</code>	Numeric, specifies the grid of evaluation points in the y-direction. When set to default, grid points will be chosen as 0.05-0.95 percentiles of the data, with a step size of 0.05 in y-direction.
<code>x</code>	Numeric, specifies the grid of evaluation points in the x-direction. When set to default, the evaluation point will be chosen as the median of the x data.
<code>bw</code>	Numeric, specifies the bandwidth used for estimation. Can be (1) a positive scalar (common bandwidth for all grid points); or (2) a positive numeric vector/matrix specifying bandwidths for each grid point (should be the same dimension as <code>grid</code>).
<code>p</code>	Nonnegative integer, specifies the order of the local polynomial for Y used to construct point estimates. (Default is 2.)
<code>q</code>	Nonnegative integer, specifies the order of the local polynomial for X used to construct point estimates. (Default is 1.)
<code>p_RBC</code>	Nonnegative integer, specifies the order of the local polynomial for Y used to construct bias-corrected point estimates. (Default is $p+1$.)

q_RBC	Nonnegative integer, specifies the order of the local polynomial for X used to construct bias-corrected point estimates. (Default is q+1.)
mu	Nonnegative integer, specifies the derivative with respect to Y of the distribution function to be estimated. 0 for the distribution function, 1 (default) for the density function, etc.
nu	Nonnegative integer, specifies the derivative with respect to X of the distribution function to be estimated. Default value is 0.
rbc	Boolean. TRUE (default) for rbc calculations, required for valid uniform inference.
ng	int. number of grid points to be used. generates evenly space points over the support of the data.
kernel_type	String, specifies the kernel function, should be one of "triangular", "uniform", and "epanechnikov"(default).
bw_type	String, specifies the method for data-driven bandwidth selection. This option will be ignored if bw is provided. Implementable with "mse-dpi" (default, mean squared error-optimal bandwidth selected for each grid point)

Details

Bias correction is only used for the construction of confidence intervals/bands, but not for point estimation. The point estimates, denoted by `est`, are constructed using local polynomial estimates of order p and q , while the centering of the confidence intervals/bands, denoted by `est_RBC`, are constructed using local polynomial estimates of order p_RBC and q_RBC . The confidence intervals/bands take the form: $[\text{est_RBC} - cv * SE(\text{est_RBC}), \text{est_RBC} + cv * SE(\text{est_RBC})]$, where cv denotes the appropriate critical value and $SE(\text{est_RBC})$ denotes an standard error estimate for the centering of the confidence interval/band. As a result, the confidence intervals/bands may not be centered at the point estimates because they have been bias-corrected. Setting p_RBC equal to p and q_RBC to q , results on centered at the point estimate confidence intervals/bands, but requires undersmoothing for valid inference (i.e., (I)MSE-optimal bandwidth for the density point estimator cannot be used). Hence the bandwidth would need to be specified manually when $q=p$, and the point estimates will not be (I)MSE optimal. See Cattaneo, Jansson and Ma (2020a, 2020b) for details, and also Calonico, Cattaneo, and Farrell (2018, 2020) for robust bias correction methods.

Sometimes the density point estimates may lie outside of the confidence intervals/bands, which can happen if the underlying distribution exhibits high curvature at some evaluation point(s). One possible solution in this case is to increase the polynomial order p or to employ a smaller bandwidth.

Value

Estimate	A matrix containing (1) grid (grid points), (2) bw (bandwidths), (3) est (point estimates with p -th and q -th order local polynomial), (4) est_RBC (point estimates with p_RBC -th and q_RBC -th order local polynomial), (5) se (standard error corresponding to est). (6) se_RBC (standard error corresponding to est_RBC).
CovMat	The variance-covariance matrix corresponding to est.
opt	A list containing options passed to the function.

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Supported methods: [coef.lpcde](#), [confint.lpcde](#), [plot.lpcde](#), [print.lpcde](#), [summary.lpcde](#), [vcov.lpcde](#)

plot.lpcde	<i>Plot Method for Local Polynomial Density Conditional Estimation and Inference</i>
------------	--

Description

The plot method for local polynomial density objects. A standard ggplot2 object is returned, hence can be used for further customization.

Usage

```
## S3 method for class 'lpcde'
plot(
  ...,
  alpha = NULL,
  type = NULL,
  lty = NULL,
  lwd = NULL,
  lcol = NULL,
  pty = NULL,
  pwd = NULL,
  pcol = NULL,
  y_grid = NULL,
  CIttype = NULL,
  CIuniform = FALSE,
  CIsimul = 2000,
  CIsshade = NULL,
  CIcol = NULL,
  title = NULL,
  xlabel = NULL,
  ylabel = NULL,
  legendTitle = NULL,
  legendGroups = NULL
)
```

Arguments

...	Class "lpcde" object, obtained from calling lpcde .
alpha	Numeric scalar between 0 and 1, specifies the significance level for plotting confidence intervals/bands.

type	String, one of "line" (default), "points" and "both", specifies how the point estimates are plotted. If more than one is provided, they will be applied to each data series accordingly.
lty	Line type for point estimates, only effective if type is "line" or "both". 1 for solid line, 2 for dashed line, 3 for dotted line. For other options, see the instructions for ggplot2 . If more than one is provided, they will be applied to each data series accordingly.
lwd	Line width for point estimates, only effective if type is "line" or "both". Should be strictly positive. For other options, see the instructions for ggplot2 . If more than one is provided, they will be applied to each data series accordingly.
lcol	Line color for point estimates, only effective if type is "line" or "both". 1 for black, 2 for red, 3 for green, 4 for blue. For other options, see the instructions for ggplot2 . If more than one is provided, they will be applied to each data series accordingly.
pty	Scatter plot type for point estimates, only effective if type is "points" or "both". For options, see the instructions for ggplot2 . If more than one is provided, they will be applied to each data series accordingly.
pwd	Scatter plot size for point estimates, only effective if type is "points" or "both". Should be strictly positive. If more than one is provided, they will be applied to each data series accordingly.
pcol	Scatter plot color for point estimates, only effective if type is "points" or "both". 1 for black, 2 for red, 3 for green, 4 for blue. For other options, see the instructions for ggplot2 . If more than one is provided, they will be applied to each data series accordingly.
y_grid	Numeric vector, specifies a subset of grid points to plot point estimates. This option is effective only if type is "points" or "both"; or if CItpe is "ebar" or "all".
CItpe	String, one of "region" (shaded region, default), "line" (dashed lines), "ebar" (error bars), "all" (all of the previous) or "none" (no confidence region), how the confidence region should be plotted. If more than one is provided, they will be applied to each data series accordingly.
CIuniform	TRUE or FALSE (default), plotting either pointwise confidence intervals (FALSE) or uniform confidence bands (TRUE).
CIsimul	Positive integer, specifies the number of simulations used to construct critical values (default is 2000). This option is ignored if CIuniform=FALSE.
Cishade	Numeric, specifies the opaqueness of the confidence region, should be between 0 (transparent) and 1. Default is 0.2. If more than one is provided, they will be applied to each data series accordingly.
CIcol	Color of the confidence region. 1 for black, 2 for red, 3 for green, 4 for blue. For other options, see the instructions for ggplot2 . If more than one is provided, they will be applied to each data series accordingly.
title, xlabel, ylabel	Strings, specifies the title of the plot and labels for the x- and y-axis.
legendTitle	String, specifies the legend title.
legendGroups	String vector, specifies the group names used in legend.

Value

Figure A standard ggplot2 object is returned, hence can be used for further customization.

Author(s)

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See Also

[lpcde](#) for local polynomial density estimation. Supported methods: [coef.lpcde](#), [confint.lpcde](#), [plot.lpcde](#), [print.lpcde](#), [summary.lpcde](#), [vcov.lpcde](#)

poly_base	<i>Polynomial basis vector expansion</i>
-----------	--

Description

Generate polynomial basis vector up to order p. has multivariate functionality as described in the main paper normalized by factorials in denominator. NOTE: currently works only up to 4th degree polynomial expansion for multivariate x.

Usage

```
poly_base(x, p)
```

Arguments

x a number or vector.

p a number (integer).

Value

polynomial basis of x up to degree p.

Examples

```
poly_base(x = 2, p = 5)
```

print.lpbwcd	<i>Print Method for Local Polynomial Conditional Density Bandwidth Selection</i>
--------------	--

Description

The print method for local polynomial conditional density bandwidth selection objects.

Usage

```
## S3 method for class 'lpbwcd'
print(x, ...)
```

Arguments

x	Class "lpbwcd" object, obtained by calling lpbwcd .
...	Other arguments.

Value

Display output A list of specified options provided to the function.

Author(s)

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 Rajita Chandak (maintainer), Princeton University. <rchandak@princeton.edu>.
 Michael Jansson, University of California Berkeley. <mjansson@econ.berkeley.edu>.
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See Also

[lpbwcd](#) for data-driven bandwidth selection.
 Supported methods: [coef.lpbwcd](#), [print.lpbwcd](#), [summary.lpbwcd](#).

print.lpcde	<i>Print Method for Local Polynomial Conditional Density Estimation and Inference</i>
-------------	---

Description

The print method for local polynomial conditional density objects.

Usage

```
## S3 method for class 'lpcde'
print(x, ...)
```

Arguments

`x` Class "lpcde" object, obtained from calling [lpcde](#).
`...` Additional options.

Value

Display output summary of inputs to lpcde

Author(s)

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See Also

[lpcde](#) for local polynomial conditional density estimation. Supported methods: [coef.lpcde](#), [confint.lpcde](#), [plot.lpcde](#), [print.lpcde](#), [summary.lpcde](#), [vcov.lpcde](#)

summary.lpbwcde	<i>Summary Method for Local Polynomial Conditional Density Bandwidth Selection</i>
-----------------	--

Description

The summary method for local polynomial conditional density bandwidth selection objects.

Usage

```
## S3 method for class 'lpbwcd'
summary(object, ...)
```

Arguments

`object` Class "lpbwcd" object, obtained by calling [lpbwcd](#).
`...` Additional options, including (i) `y_grid` specifies a subset of `y_grid` points to display the bandwidth; (ii) `gridIndex` specifies the indices of `y_grid` points to display the bandwidth.

Value

Display output A list of specified options and a matrix of grid points, bandwidth, and effective sample size.

Author(s)

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See Also

[lpbwcd](#) for data-driven bandwidth selection.

Supported methods: [coef.lpbwcd](#), [print.lpbwcd](#), [summary.lpbwcd](#).

Examples

```
n=100
x_data = as.matrix(rnorm(n, mean=0, sd=1))
y_data = as.matrix(rnorm(n, mean=0, sd=1))
y_grid = stats::quantile(y_data, seq(from=0.1, to=0.9, by=0.1))
# bandwidth selection
y_grid = stats::quantile(y_data, seq(from=0.1, to=0.9, by=0.1))
model2 = lpcde::lpbwcd(y_data=y_data, x_data=x_data, x=0, y_grid = y_grid, bw_type = "mse-rot")
summary(model2)
```

summary.lpcde

Summary Method for Local Polynomial Density Conditional Estimation and Inference

Description

The summary method for local polynomial conditional density objects.

Usage

```
## S3 method for class 'lpcde'
summary(object, ...)
```

Arguments

object	Class "lpcde" object, obtained from calling lpcde .
...	Additional options, including (i) <code>y_grid</code> specifies a subset of grid points in y-directions to display results; (ii) <code>gridIndex</code> specifies the indices of grid points to display results; (iii) <code>alpha</code> specifies the significance level; (iv) <code>CIuniform</code> specifies whether displaying pointwise confidence intervals (FALSE, default) or the uniform confidence band (TRUE); (v) <code>CIsimul</code> specifies the number of simulations used to construct critical values (default is 2000).

Value

Display output A list of specified options and a matrix of grid points and estimates.

Author(s)

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See Also

[lpcde](#) for local polynomial conditional density estimation. Supported methods: [coef.lpcde](#), [confint.lpcde](#), [plot.lpcde](#), [print.lpcde](#), [summary.lpcde](#), [vcov.lpcde](#)

Examples

```
n=100
x_data = as.matrix(rnorm(n, mean=0, sd=1))
y_data = as.matrix(rnorm(n, mean=0, sd=1))
y_grid = stats::quantile(y_data, seq(from=0.1, to=0.9, by=0.1))
# density estimation
model1 = lpcde::lpcde(x_data=x_data, y_data=y_data, y_grid=y_grid, x=0, bw=0.5)
summary(model1)
```

vcov.lpcde	<i>Variance-Covariance</i>
------------	----------------------------

Description

The vcov method for local polynomial conditional density objects.

Usage

```
## S3 method for class 'lpcde'
vcov(object, ...)
```

Arguments

object	Class "lpdensity" object, obtained by calling lpcde .
...	Additional options.

Details

Vcov Method for Local Polynomial Density Conditional Estimation and Inference

Value

stdErr	A matrix containing grid points and standard errors using p- and q-th order local polynomials.
CovMat	The variance-covariance matrix corresponding to est.
CovMat_RBC	The variance-covariance matrix corresponding to est_RBC.

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See Also

[lpcde](#) for local polynomial conditional density estimation.

Supported methods: [plot.lpcde](#), [print.lpcde](#), [summary.lpcde](#),

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