



## Title

**lprobust** — Local Polynomial Regression Estimation with Robust Bias-Corrected Confidence Intervals and Inference Procedures.

## Syntax

```
lprobust yvar xvar [if] [in] [, eval(gridvar) neval(#) deriv(#) p(#) h(hvar)  
b(bvar) rho(#) kernel(kernelfn) bwselect(bwmethod) bwcheck(#) imsegrid(#)  
vce(vcetype [vcdept]) level(#) bwregul(#) separator(#) interior genvars  
covgrid plot graph_options(gphopts) ]
```

## Description

**lprobust** implements local polynomial regression point estimators with robust bias-corrected confidence intervals and inference procedures developed in [Calonico, Cattaneo and Farrell \(2018\)](#). See also [Calonico, Cattaneo and Farrell \(2020\)](#) for related optimality results. It also implements other estimation and inference procedures available in the literature. See Wand and Jones (1995) and Fan and Gijbels (1996) for background references.

A detailed introduction to this command is given in [Calonico, Cattaneo and Farrell \(2019\)](#).

Companion command is: [lpbwselect](#) for data-driven bandwidth selection.

Related Stata and R packages useful for empirical analysis are described in the following website:

<https://sites.google.com/site/nppackages/>

## Options

**eval**(*gridvar*) specifies the grid of evaluation points for *xvar*. By default it uses 30 equally spaced points over to support of *xvar*.

**neval**(#) specifies the number of evaluation points to estimate the regression functions. Default is 30 evaluation points.

**deriv**(#) specifies the order of the derivative of the regression functions to be estimated. Default is **deriv**(0).

**p**(#) specifies the order of the local polynomial used to construct the point estimator. Default is **p**(1) (local linear regression).

**h**(*hvar*) specifies the main bandwidth (*h*) used to construct the point estimator for each evaluation point. If not specified, it is computed by the companion command [lpbwselect](#).

**b**(*bvar*) specifies the bias bandwidth (*b*) used to construct the bias-correction estimator for each evaluation point. If not specified, it is computed by the companion command [lpbwselect](#).

**rho**(#) specifies the value of *rho*, so that the bias bandwidth *b* equals  $b=h/\rho$ . Default is **rho**(1) if *h* is specified but *b* is not.

**kernel**(*kernelfn*) specifies the kernel function used to construct the local-polynomial estimator(s). Options are: **triangular**, **epanechnikov**, **uniform** and **gaussian**. Default is **kernel**(*epanechnikov*).

**bwselect**(*bwmethod*) bandwidth selection procedure to be used. By default it computes both  $h$  and  $b$ , unless  $\rho$  is specified, in which case it only computes  $h$  and sets  $b=h/\rho$ . Options are:  
**mse-dpi** second-generation DPI implementation of MSE-optimal bandwidth. Default choice.  
**mse-rot** ROT implementation of MSE-optimal bandwidth.  
**imse-dpi** second-generation DPI implementation of IMSE-optimal bandwidth.  
**imse-rot** ROT implementation of IMSE-optimal bandwidth.  
**ce-dpi** second generation DPI implementation of CE-optimal bandwidth.  
**ce-rot** ROT implementation of CE-optimal bandwidth.  
Note: MSE = Mean Square Error; IMSE = Integrated Mean Squared Error; CE = Coverage Error; DPI = Direct Plug-in; ROT = Rule-of-Thumb.  
Default is **bwselect(mse-dpi)**. For details on implementation see [Calonico, Cattaneo and Farrell \(2019\)](#).

**bwcheck**(#) specifies an optional positive integer so that the selected bandwidth is enlarged to have at least # effective observations available for each evaluation point.

**imsegrid**(#) number of evaluations points used to compute the IMSE bandwidth selector. Default is 30 points.

**vce**(*vcetype* [*vceopt1*]) specifies the procedure used to compute the variance-covariance matrix estimator. Options are:  
**vce**(*nn* [*nnmatch*]) for heteroskedasticity-robust nearest neighbor variance estimator with *nnmatch* indicating the minimum number of neighbors to be used.  
**vce**(*hc0*) for heteroskedasticity-robust plug-in residuals variance estimator without weights.  
**vce**(*hc1*) for heteroskedasticity-robust plug-in residuals variance estimator with *hc1* weights.  
**vce**(*hc2*) for heteroskedasticity-robust plug-in residuals variance estimator with *hc2* weights.  
**vce**(*hc3*) for heteroskedasticity-robust plug-in residuals variance estimator with *hc3* weights.  
**vce**(**nncluster** *clustervar* [*nnmatch*]) for cluster-robust nearest neighbor variance estimation using with *clustervar* indicating the cluster ID variable and *nnmatch* matches indicating the minimum number of neighbors to be used.  
**vce**(**cluster** *clustervar*) for cluster-robust plug-in residuals variance estimation with degrees-of-freedom weights and *clustervar* indicating the cluster ID variable.  
Default is **vce(nn 3)**.

**level**(#) specifies confidence level for confidence intervals. Default is **level(95)**.

**bwregul**(#) specifies scaling factor for the regularization term added to the denominator of the bandwidth selectors. Setting **bwregul(0)** removes the regularization term from the bandwidth selectors. Default is **bwregul(1)**.

**separator**(#) draws separator line after every # variables; default is **separator(5)**.

**interior** option to set all evaluation points to be interior points. This option affects only data-driven bandwidth selection via [lpbwselect](#).

**covgrid** option to compute two covariance matrices (*cov\_us* and *cov\_rb*) for classical and robust covariances across point estimators over the grid of evaluation points.)

**plot** generates the local polynomial regression plot.

`genvars` generates new variables storing the following results.

- `lprobust_eval` evaluation points.
- `lprobust_h` bandwidth  $h$ .
- `lprobust_b` bandwidth  $b$ .
- `lprobust_nh` effective sample size.
- `lprobust_gx_us` conventional local polynomial estimate.
- `lprobust_se_us` conventional standard error for the local polynomial estimator.
- `lprobust_gx_bc` bias-corrected local polynomial regression estimate.
- `lprobust_se_rb` robust standard error for the local polynomial estimator.
- `lprobust_ci_l_rb` lower end value of the robust confidence interval.
- `lprobust_ci_r_rb` upper end value of the robust confidence interval.

`graph_options` (`gphopts`) specifies graphical options to be passed on to the underlying graph command.

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Setup

`. webuse motorcycle`

Local linear regression with second-generation DPI implementation of MSE-optimal bandwidth

`. lprobust accel time`

Same as above, but generating a plot and the corresponding output variables

`. lprobust accel time, plot genvars`

### Saved results

`lprobust` saves the following in `e()`:

Scalars

<code>e(N)</code>	original number of observations
<code>e(p)</code>	order of the polynomial used for estimation of the regression function

Macros

<code>e(varname)</code>	name of variable
<code>e(clustvar)</code>	name of cluster variable
<code>e(bwselect)</code>	bandwidth selection choice
<code>e(kernel)</code>	kernel choice
<code>e(vce)</code>	vce choice

Matrices

<code>e(Result)</code>	estimation result
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### References

- Calonico, S., M. D. Cattaneo, and M. H. Farrell. 2018. [On the Effect of Bias Estimation on Coverage Accuracy in Nonparametric Inference](#). *Journal of the American Statistical Association*, 113(522): 767-779.
- Calonico, S., M. D. Cattaneo, and M. H. Farrell. 2019. [nprobust: Nonparametric Kernel-Based Estimation and Robust Bias-Corrected Inference](#). *Journal of Statistical Software*, 91(8): 1-33. doi: 10.18637/jss.v091.i08.
- Calonico, S., M. D. Cattaneo, and M. H. Farrell. 2020. [Coverage Error Optimal Confidence Intervals for Local Polynomial Regression](#), working paper.
- Fan, J., and Gijbels, I. 1996. *Local Polynomial Modelling and Its Applications*, London: Chapman and Hall.
- Wand, M., and Jones, M. 1995. *Kernel Smoothing*, Florida: Chapman & Hall/CRC.

### Authors

Sebastian Calonico, Columbia University, New York, NY.  
[sebastian.calonico@columbia.edu](mailto:sebastian.calonico@columbia.edu).

Matias D. Cattaneo, Princeton University, Princeton, NJ. [cattaneo@princeton.edu](mailto:cattaneo@princeton.edu).

Max H. Farrell, University of Chicago, Chicago, IL. [max.farrell@chicagobooth.edu](mailto:max.farrell@chicagobooth.edu).