

<u>Title</u>

scpi — Estimation and Inference for Synthetic Control Methods.

Syntax

```
scpi , dfname(string) [p(#) direc(string) Q(#) lb(#) name(string) u_missp)
    u_sigma(string) u_order(#) u_lags(#) u_alpha(#) sims(#) e_method(string)
    e_order(#) e_lags(#) e_alpha(#) rho(#) rho_max(#) opt_est(string)]
    opt_inf(string)]
```

Description

scpi implements estimation and inference procedures for Synthetic Control (SC) methods using least squares, lasso, ridge, or simplex-type constraints according to Cattaneo, Feng, and Titiunik (2021). The command is a wrapper of the companion Python package. As such, the user needs to have a running version of Python with the package installed. A tutorial on how to install Python and link it to Stata can be found here.

Companion \underline{R} and \underline{Python} packages are described in $\underline{Cattaneo}$, \underline{Feng} , $\underline{Palomba}$ and $\underline{Titiunik}$ (2022).

Companion commands are: \underline{scdata} for data preparation, \underline{scest} for estimation procedures, and \underline{scplot} for SC plots.

Related Stata, R, and Python packages useful for inference in SC designs are described in the following website:

https://nppackages.github.io/scpi/

Options

dfname(string) specifies the name of the Python object containing the processed
 data created with <u>scdata</u>.

```
Constraint
```

These options let the user specify the type of constraint to be imposed to estimate the SC weights. The user controls the norm of the weights to be constrained (option **p**), the direction of the constraint on the norm (option **dir**), and the size of the constraint on the norm (option **q**). Alternatively, some popular constraints can be selected through the option **name**. A detailed description of the popular constraints implemented can be found in <u>Cattaneo</u>, <u>Feng</u>, <u>Palomba</u> and <u>Titiunik</u> (2022).

name(string) specifies the name of the constraint to be used. Options are:
 simplex classic SC estimator as proposed in <u>Abadie (2021)</u>. Estimated weights
 are constrained to be non-negative and their L1 norm must be equal to 1.
 lasso weights are estimated using a Lasso-type penalization
 ridge weights are estimated using a Ridge-type penalization.
 ols weights are estimated without constraints using least squares

- p(#) sets the type of norm to be constrained. Options are:
 - O no constraint on the norm of the weights is imposed.
 - $oldsymbol{1}$ a constraint is imposed on the L1 norm of the weights (the default).
 - 2 a constraint is imposed on the L2 norm of the weights.
- direc(string) specifies the direction of the constraint on the norm of the
 weights. Options are:
 - <= the constraint on the norm of the weights is an inequality constraint.
 - == the constraint on the norm of the weights is an equality constraint (the default).
- \mathbf{Q} (#) specifies the size of the constraint on the norm of the weights.
- 1b(#) specifies the lower bound on the weights. The default is 1b(0).

```
In-sample Uncertainty
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This set of options allows the user to specify her preferred approach to model in-sample uncertainty, that is uncertainty that stems from the estimation the weights.

 $\mathbf{u}_{\underline{}}$ missp if specified indicates that model misspecification should be taken into account.

 $u_sigma(string)$ specifies the type of variance-covariance estimator to be used when estimating the conditional variance of the pseudo-residuals. Options are: HCO, HC1 (default), HC2, and HC3.

 $u_order(\#)$ specifies the order of the polynomial in the predictors used to estimate conditional moments of the pseudo-residuals. Default is ${\bf u_order(1)}$.

 \mathbf{u} _lags(#) specifies the lags of the predictors used to estimate conditional

moments of the pseudo-residuals. Default is **u_lags(0)**. **u_alpha(#)** specifies the confidence level for in-sample uncertainty. Default is $u_alpha(0.05)$.

sims(#) specifies the number of simulations to be used in quantifying in-sample uncertainty. Default is sims (200).

```
^{
m J} Out-of-sample Uncertainty ^{
m L}
```

This set of options allows the user to specify her preferred approch to model out-of-sample uncertainty.

e_method(#) specifies the method to be used to quantify out-of-sample uncertainty. Options are:

gaussian conditional subgaussian bounds.

1s location-scale model.

qreg quantile regression.

all all of the above (the default).

e_order(#) specifies the order of the polynomial in the predictors used to estimate conditional moments of the out-of-sample error. Default is e_order(1).

e_lags(#) specifies the lags of the predictors used to estimate conditional moments of the out-of-sample error. Default is $e_{lags}(0)$.

e_alpha(#) specifies the confidence level for out-fo-sample uncertainty. Default is e alpha (0.05).

```
\dashv Regularization ^{\mathsf{L}}
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rho(#) specifies the regularizing parameter that imposes sparsity on the estimated
 vector of weights. If unspecified, the tuning parameter is computed based on optimization inequalities.

rho_max(#) specifies the maximum value attainable by the tuning parameter rho.

```
J <sub>Others</sub>
```

opt_est(string) a string specifying the stopping criteria used by the underling optimizer (nlopt) for point estimation. The default is a sequential quadratic programming (SQP) algorithm for nonlinearly constrained gradient-based optimization ('SLSQP'). In case a lasso-type constraint is implemented, the method of moving asymptotes (MMA) is used. The default value is opt("'maxeval' = 5000, 'xtol_rel' = 1e-8, 'xtol_abs' = 1e-8, 'ftol_rel' = 1e-12, 'ftol_abs' = 1e-12, 'tol_eq' = 1e-8, 'tol_ineq' = 1e-8").

opt_inf(string) a string specifying the stopping criteria used by the underling optimizer (nlopt) for point estimation. The default is a sequential quadratic programming (SQP) algorithm for nonlinearly constrained gradient-based optimization ('SLSQP'). In case a lasso-type constraint is implemented, the method of moving asymptotes (MMA) is used. The default value is opt("'maxeval' = 5000, 'xtol_rel' = le-8, 'xtol_abs' = le-8, 'ftol_rel' = le-4, 'ftol_abs' = le-4, 'tol_eq' = le-8, 'tol_ineq' = le-8").

Example: Cattaneo, Feng and Titiunik (2021) Germany Data

```
Setup
         . use scpi_germany.dta
    Prepare data
         scdata gdp, dfname("python_scdata") id(country) outcome(gdp) time(year)
        treatment(status) cointegrated
    Estimate Synthetic Control with a simplex constraint and quantify uncertainty
        . scpi, dfname("python_scdata") name(simplex) u_missp
marker stored_results}Stored_results
    scpi stores the following in e():
    Scalars
                                number of features number of covariates used for adjustment
      e (M)
      e (KM)
      e (J)
                                number of donors
      e(T1)
                                number of post-treatment periods
                                size of the constraint on the norm
      e (a)
                                post-estimation regularization parameter
      e(rho)
    Macros
      e(features)
                                name of features
                                name of outcome variable
      e(outcomevar)
      e(constant)
                                logical indicating the presence of a common constant
                                  across features
      e(cointegrated_data)
                                logical indicating cointegration
      e (p)
                                type of norm of the weights used in constrained
                                   estimation
      e(dir)
                                direction of the constraint on the norm of the
                                  weights
                                 name of constraint used in estimation
      e (name)
      e(u_missp)
                                a logical indicating whether the model has been
                                  treated as misspecified or not
      e(u_order)
                                order of the polynomial in the predictors used to
                                  estimate conditional moments of the
                                  pseudo-residuals
                                lags of the predictors used to estimate conditional
      e(u lags)
                                 moments of the pseudo-residuals
      e(u_sigma)
                                estimator of the conditional variance-covariance
                                  matrix of the pseudo-residuals
                                confidence level for in-sample uncertainty
      e(u_alpha)
                                method used to quantify out-of-sample uncertainty order of the polynomial in the predictors used to
      e(e method)
      e(e_order)
                                   estimate conditional moments of the out-of-sample
                                   error
      e(e_lags)
                                order of the polynomial in the predictors used to
                                   estimate conditional moments of the out-of-sample
                                   error
      e(e_alpha)
                                confidence level for out-of-sample uncertainty
    Matrices
      e(T0)
                                number of pre-treatment periods per feature
                                pre-treatment features of the treated unit
      e (A)
                                pre-treatment features of the control units
      e (B)
      e (C)
                                 covariates used for adjustment
                                predicted values of the features of the treated unit
      e (pred)
                                residuals e(A) - e(pred)
      e(res)
                                weights of the controls
      e(w)
                                coefficients of the covariates used for adjustment
      e(r)
      e (beta)
                                stacked version of e(w) and e(r)
      e(Y_post)
                                post-treatment outcome of the treated unit
      e(Y_post_fit)
                                estimated post-treatment outcome of the treated unit pre-treatment outcome of the treated unit
      e(Y_pre)
      e(Y_pre_fit)
                                estimate pre-treatment outcome of the treated unit
      e(CI_in_sample)
                                prediction intervals taking only in-sample
                                  uncertainty into account
      e(CI_all_gaussian)
                                prediction intervals taking in- and out-of-sample
```

uncertainty into account

e(CI_all_ls)	<pre>prediction intervals taking in- and out-of-sample uncertainty into account</pre>
e(CI_all_qreg)	prediction intervals taking in- and out-of-sample uncertainty into account
e(e_mean)	estimated conditional mean of the out-of-sample error
e(e_var)	estimated conditional variance of the out-of-sample error
e(Sigma)	estimated conditional variance-covariance of the pseudo-residuals
e(failed_sims)	percentage of failed simulations per post-treatment period to estimate lower and upper bounds.

References

Abadie, A. 2021. <u>Using synthetic controls: Feasibility, data requirements, and methodological aspects.</u> Journal of Economic Literature, 59(2), 391-425.

Cattaneo, M. D., Feng, Y., and Titiunik, R. 2021. <u>Prediction Intervals for Synthetic Sontrol Methods</u>. *Journal of the American Statistical Association*, 116(536), 1865-1880.

Cattaneo, M. D., Feng, Y., Palomba F., and Titiunik, R. 2022. script-uncertainty-output-control-extimators.

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