# Assignment-1

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October 3, 2020

### 1 Problem

Find the coordinates of the point where the line through  $\begin{pmatrix} 3 \\ -4 \\ -5 \end{pmatrix}$  and  $\begin{pmatrix} 2 \\ -3 \\ 1 \end{pmatrix}$  crosses the plane  $\begin{pmatrix} 2 \\ 1 \end{pmatrix}$   $\begin{pmatrix} 1 \\ 1 \end{pmatrix}$   $\begin{pmatrix} 2 \\ 1 \end{pmatrix}$   $\begin{pmatrix} 1 \\ 1 \end{pmatrix}$   $\begin{pmatrix} 1 \\ 1 \end{pmatrix}$   $\begin{pmatrix} 1 \\ 1 \end{pmatrix}$ 

## 2 Explanation

We know that vector equation of line passing through two points , say A and B is

$$\mathbf{x} = \vec{A} + \lambda \left( \vec{B} - \vec{A} \right) \tag{2.1}$$

We also know that equation of a plane is

$$\mathbf{n}^T \mathbf{x} = c \tag{2.2}$$

Substituting 2.1 in 2.2 as line passes through the plane we can get the point of contact.

### 3 Solution

### Step 1

Let us first findout the equation of line passing through two given points using 2.1

$$\mathbf{x} = \begin{pmatrix} 3 \\ -4 \\ -5 \end{pmatrix} + \lambda \begin{pmatrix} 2-3 \\ -3+4 \\ 1+5 \end{pmatrix}$$
 (3.1)

$$\mathbf{x} = \begin{pmatrix} 3 \\ -4 \\ -5 \end{pmatrix} + \lambda \begin{pmatrix} -1 \\ 1 \\ 6 \end{pmatrix} \tag{3.2}$$

#### Step 2

Now let us construct the equation of plane from the given data.

Using the values we can construct

$$\mathbf{n} = \begin{pmatrix} 2\\1\\1 \end{pmatrix} \tag{3.3}$$

#### Step 3

Now using 3.2, 3.3 in 2.2

$$(2 1 1) \left( \begin{pmatrix} 3 \\ -4 \\ -5 \end{pmatrix} + \lambda \begin{pmatrix} -1 \\ 1 \\ 6 \end{pmatrix} \right) = 7 (3.4)$$

solving 3.4 we get

$$6 - 4 - 5 - 2\lambda + \lambda + 6\lambda = 7 \tag{3.5}$$

$$5\lambda = 10\tag{3.6}$$

$$\lambda = 2 \tag{3.7}$$

Now substituting the value of  $\lambda$  in 2.1 we get

$$\mathbf{x} = \begin{pmatrix} -2+3\\ 2-4\\ 12-5 \end{pmatrix} \tag{3.8}$$

Therefore the point of contact of line on plane is

$$\mathbf{x} = \begin{pmatrix} 1 \\ -2 \\ 7 \end{pmatrix} \tag{3.9}$$



