

# The yielding transition in periodically sheared binary glasses at finite temperature

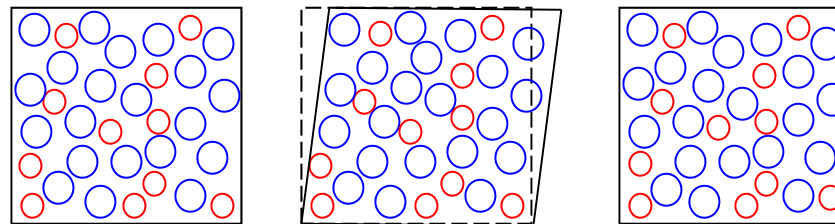
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<http://www.wright.edu/~nikolai.priezjev/>



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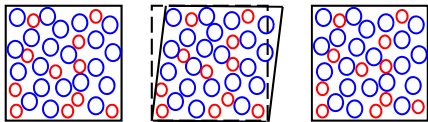
# Structural relaxation and dynamical heterogeneities in deformed glasses

Metallic glasses: mechanical properties include high strength and low ductility



Sun, Concustell, and Greer, Thermomechanical processing of metallic glasses: extending the range of the glassy state, *Nature Reviews Materials* **1**, 16039 (2016).

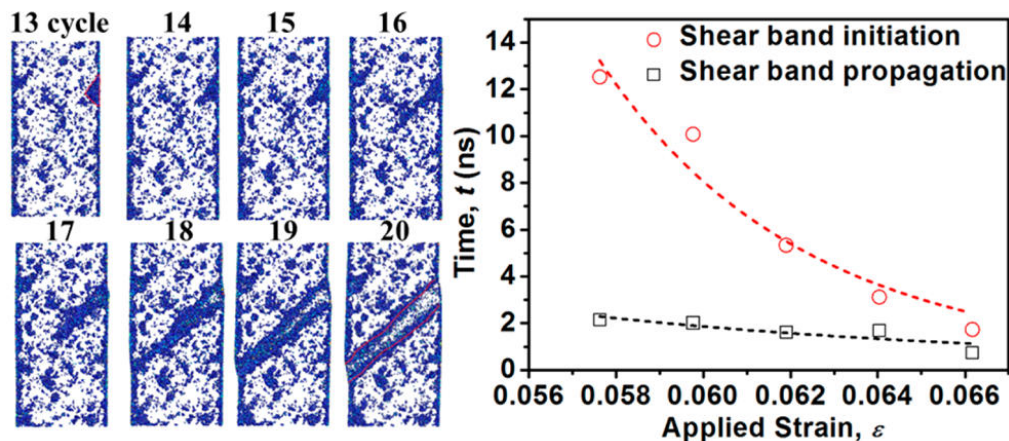
Cyclic loading: yielding transition, fatigue lifetime, failure mechanism, nonaffine motion (??)



Candelier, Dauchot, and Biroli, Dynamical heterogeneity in the cyclic shear experiment on dense 2D granular media, *Phys. Rev. Lett.* **102**, 088001 (2009).

Knowlton, Pine, and Cipelletti, A microscopic view of the yielding transition in concentrated emulsions, *Soft Matter* **10**, 6931 (2014).

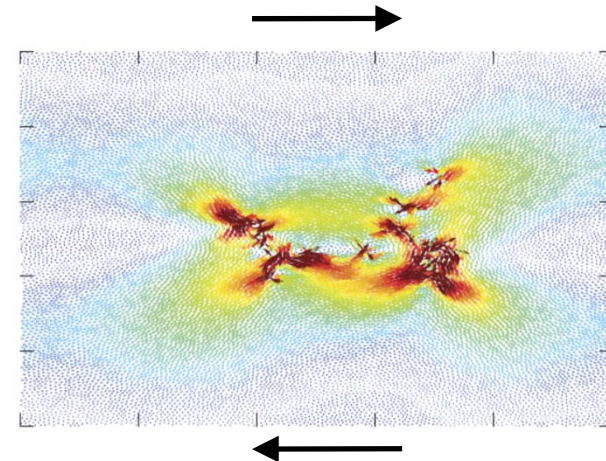
Tension-compression cyclic loading of metallic glasses:



Shear band due to accumulation of STZs at boundary

Sha, Qu, Liu, Wang, and Gao, *Nano Lett.* (2015)

Reversible avalanches in 2D amorphous solids:



Large particle displacements are completely reversed

Regev, Weber, Reichhardt, Dahmen, Lookman, *Nature* (2015)

# Details of molecular dynamics simulations and parameter values

Binary Lennard-Jones Kob-Andersen mixture:

$$V_{LJ}(r) = 4\epsilon_{\alpha\beta} \left[ \left( \frac{\sigma_{\alpha\beta}}{r} \right)^{12} - \left( \frac{\sigma_{\alpha\beta}}{r} \right)^6 \right] \quad \text{Ni}_{80}\text{P}_{20}$$

Parameters for  $\alpha\beta = A$  and  $B$  particles:

$$\epsilon_{AA} = 1.0, \epsilon_{AB} = 1.5, \epsilon_{BB} = 0.5, m_A = m_B$$

$$\sigma_{AA} = 1.0, \sigma_{AB} = 0.8, \sigma_{BB} = 0.88$$

$$\text{Monomer density: } \rho = \rho_A + \rho_B = 1.20 \sigma^{-3}$$

$$\text{Temperature: } T_{LJ} = 0.1 \epsilon/k_B < T_g = 0.435 \epsilon/k_B$$

$$\text{System size: } L = 36.84 \sigma, N_p = 60,000$$

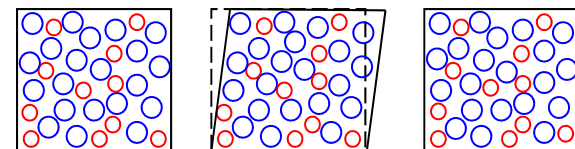
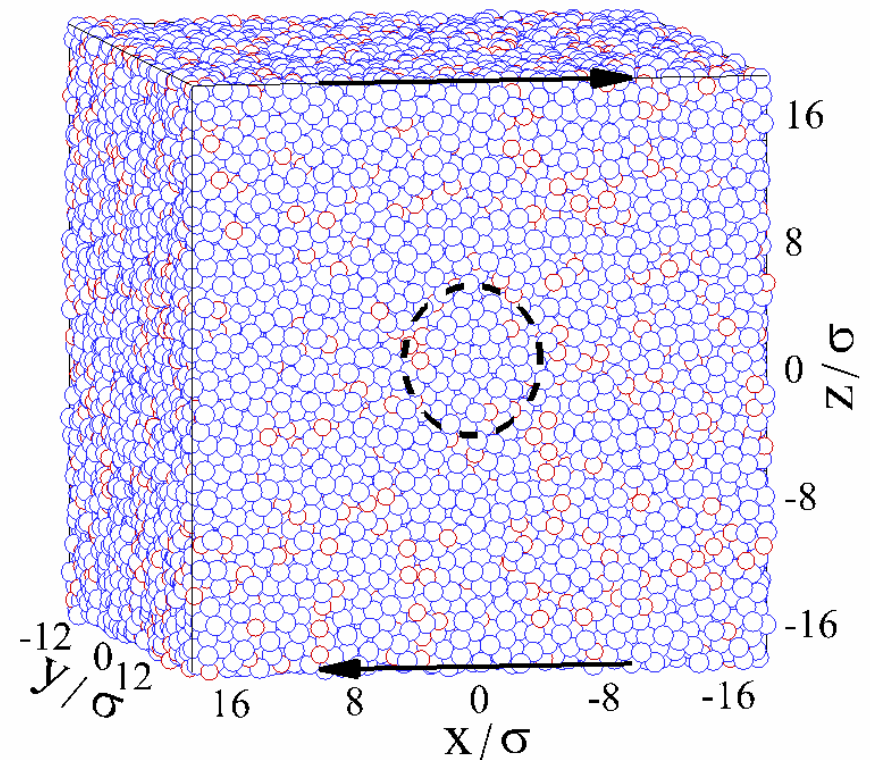
Lees-Edwards periodic boundary conditions

$$\text{LAMMPS, DPD thermostat, } \Delta t_{MD} = 0.005 \tau$$

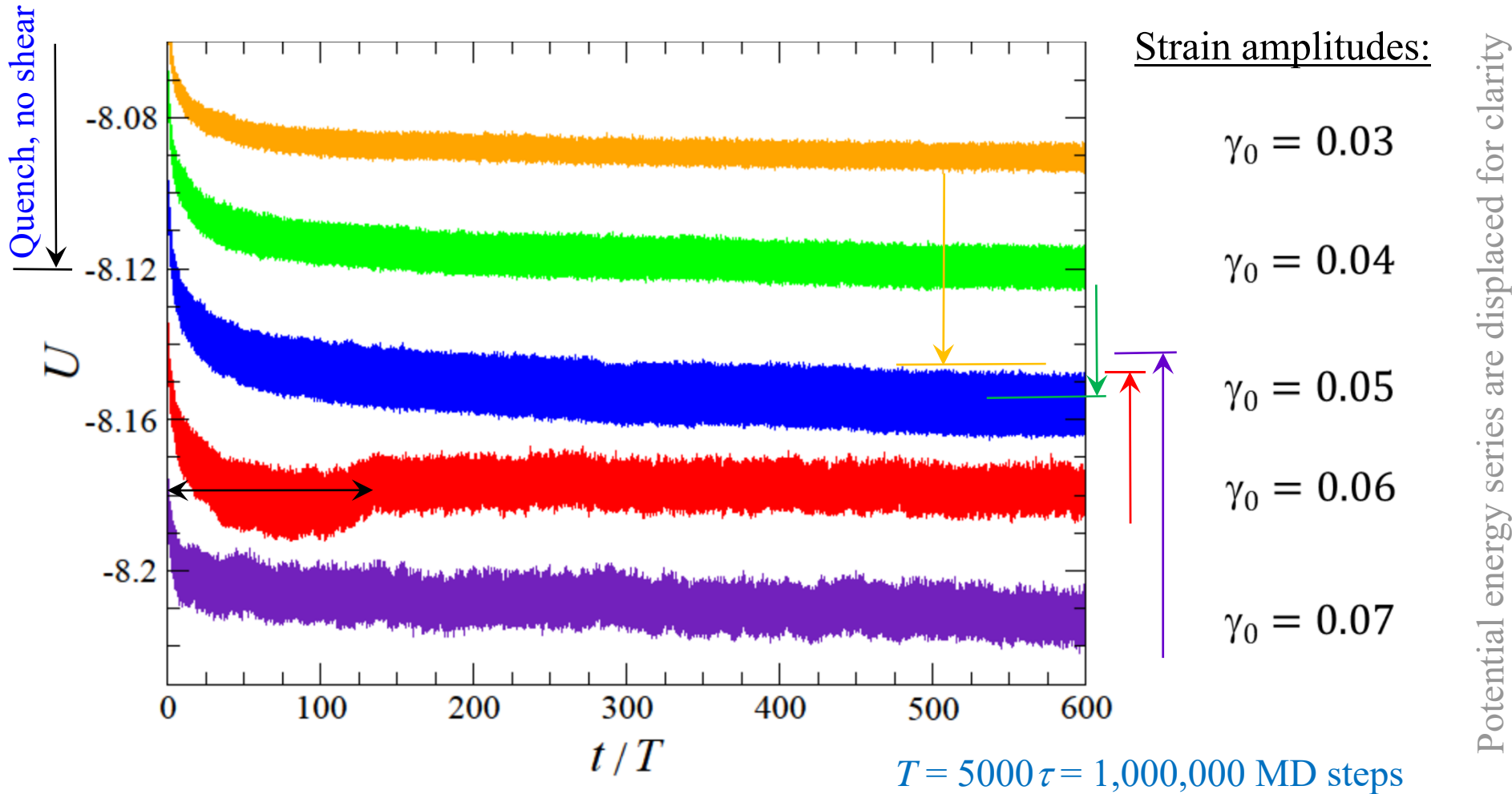
Instantaneous quenching to  $T_{LJ} = 0.1 \epsilon/k_B$

Oscillatory shear strain:  $\gamma(t) = \gamma_0 \sin(\omega t)$

Oscillation period:  $T = 2\pi / \omega = 5000 \tau$



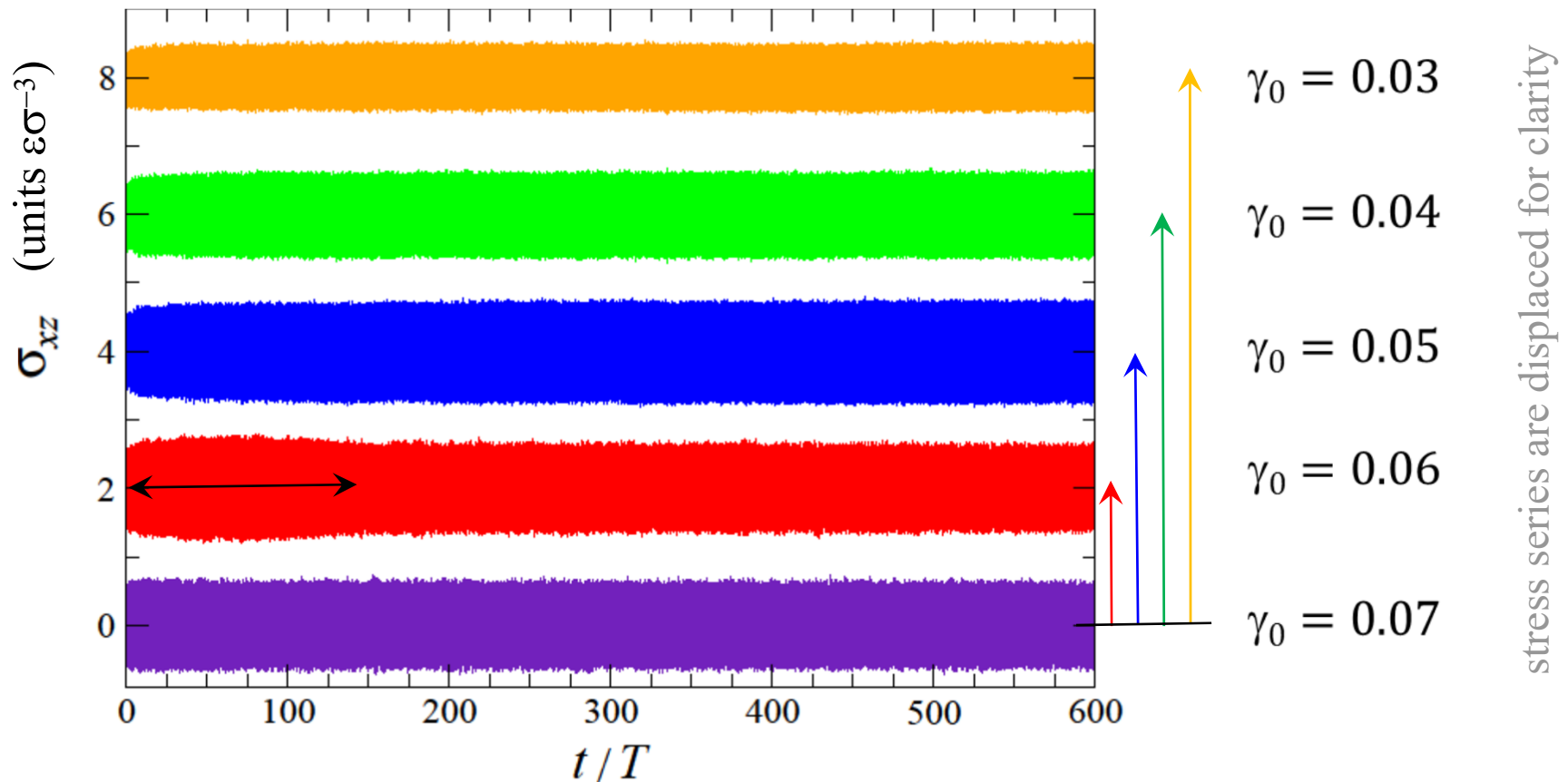
Potential energy per particle  $U/\varepsilon$  during 600 oscillation cycles for different  $\gamma_0$



At small strain amplitudes,  $\gamma_0 \leq 0.05$ , the potential energy acquires progressively lower minima with increasing strain amplitude. **Minimum potential energy is at  $\gamma_0 = 0.05$ .**

Near the yield transition,  $\gamma_0 = 0.06$ , shallow minimum in potential energy during first 150 cycles.

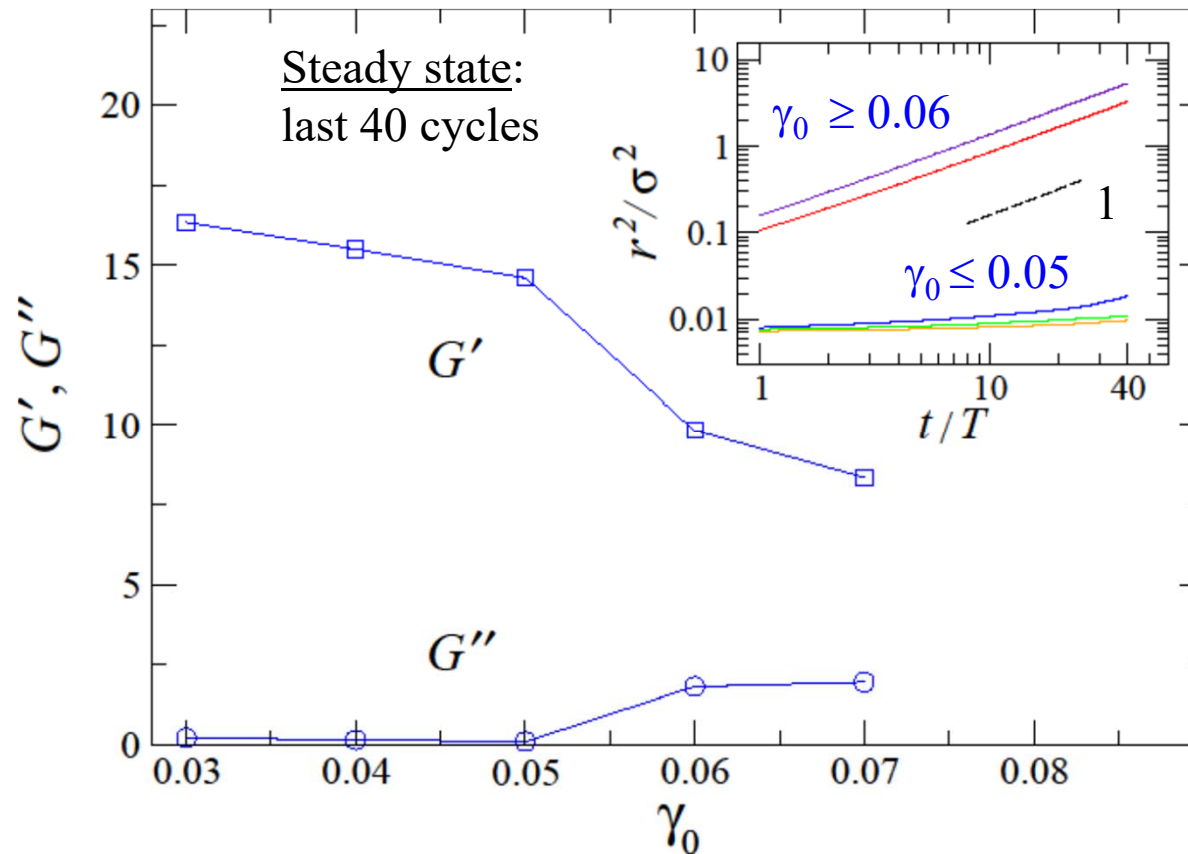
## Shear stress during 600 oscillation cycles for different strain amplitudes $\gamma_0$



At small strain amplitudes,  $\gamma_0 \leq 0.05$ : the amplitude of stress oscillations becomes larger with increasing strain amplitude; nearly reversible particle dynamics.

Near the critical strain amplitude,  $\gamma_0 = 0.06$ : shallow maximum in the amplitude of stress oscillations during first 150 cycles; then stress amplitude is reduced at  $t > 150T$ .

## Storage and loss moduli and mean-square displacements for different $\gamma_0$



At small strain amplitudes,  $\gamma_0 \leq 0.05$ , the storage modulus  $G'$  dominates the response; nearly reversible particle dynamics.

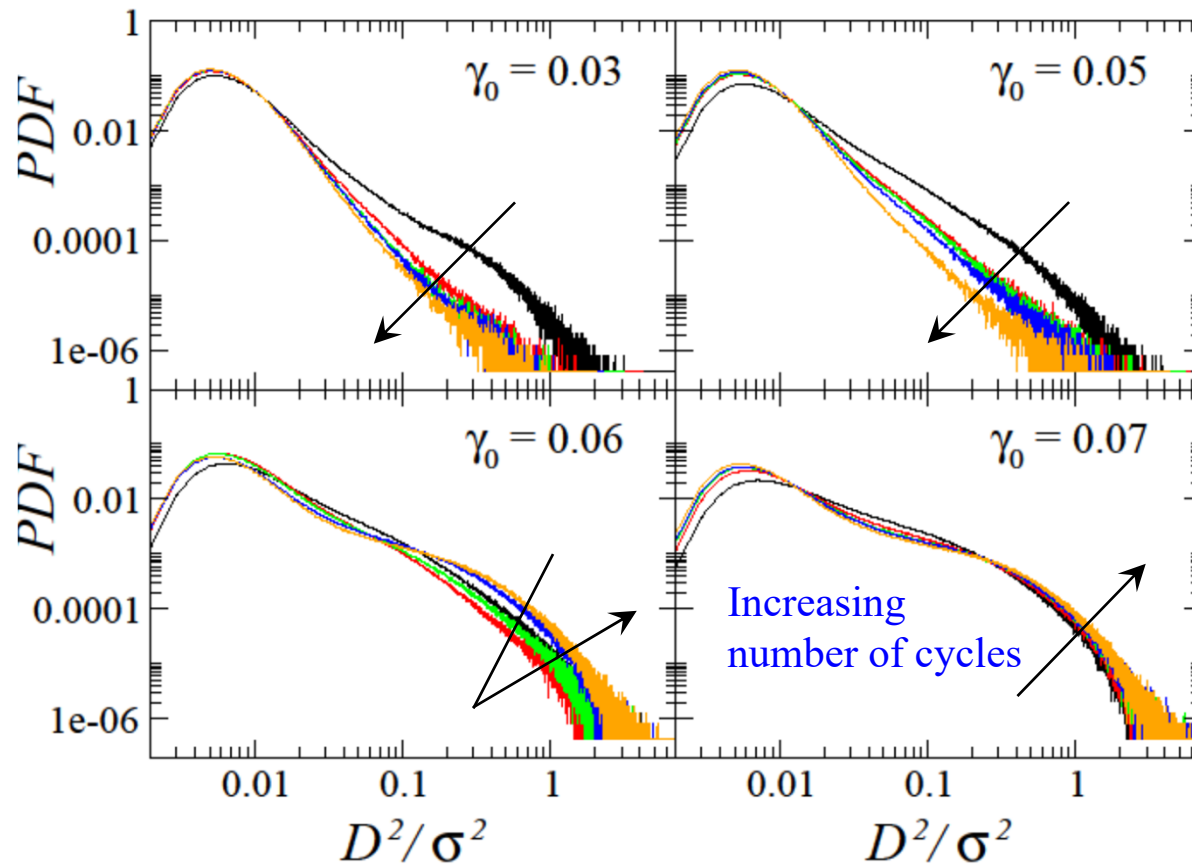
At large strain amplitudes,  $\gamma_0 \geq 0.06$ , the loss modulus  $G''$  increases; irreversible particle diffusion; formation of shear band.

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The critical strain amplitude,  $G'=G''$ ,  $\gamma_x > \gamma_c$ , onset of diffusion. Kawasaki & Berthier, *PRE* (2016).



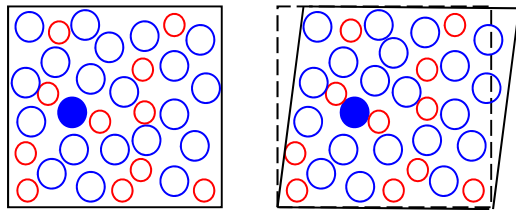
# Probability distribution function of the nonaffine measure $D^2(t,T)$ after one cycle



At small strain amplitudes,  $\gamma_0 \leq 0.05$ , width of PDF is more narrow as the number of cycles increases; the system dynamics is nearly reversible after 600 cycles.

At large strain amplitudes,  $\gamma_0 \geq 0.06$ , PDFs become wider as the number of cycles increases; formation of shear band; enhanced particle diffusion.

$$D^2(t, \Delta t = T)$$



$t \longrightarrow t + \Delta t$

$$D^2(t, \Delta t) = \frac{1}{N_i} \sum_{j=1}^{N_i} \left\{ \mathbf{r}_j(t + \Delta t) - \mathbf{r}_i(t + \Delta t) - J_i[\mathbf{r}_j(t) - \mathbf{r}_i(t)] \right\}^2$$

Excellent diagnostic for identifying particle rearrangements

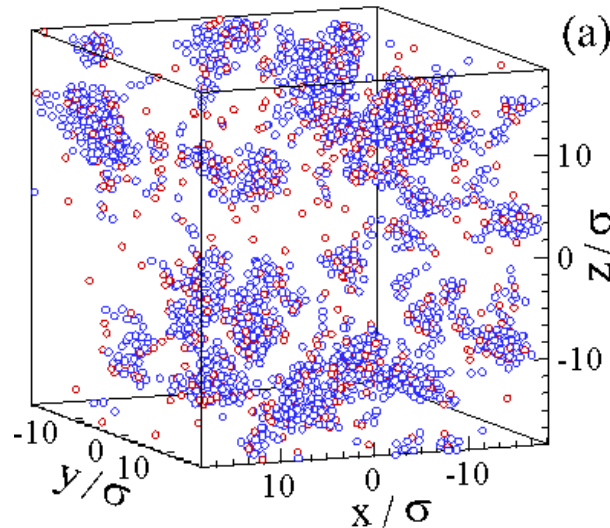
Falk and Langer, *Phys. Rev. E* **57**, 7192 (1998).

# Spatial configurations of atoms with large nonaffine displacements at $\gamma_0=0.03$

$$D^2(t, T) > 0.04 \sigma^2$$

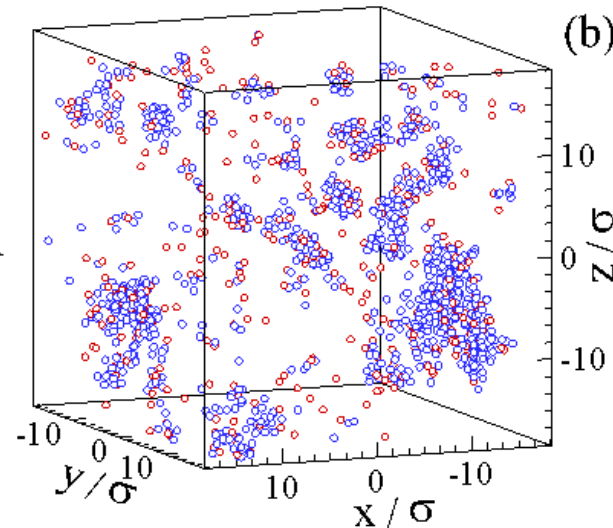
After 20-th cycle

Disconnected  
sparse clusters



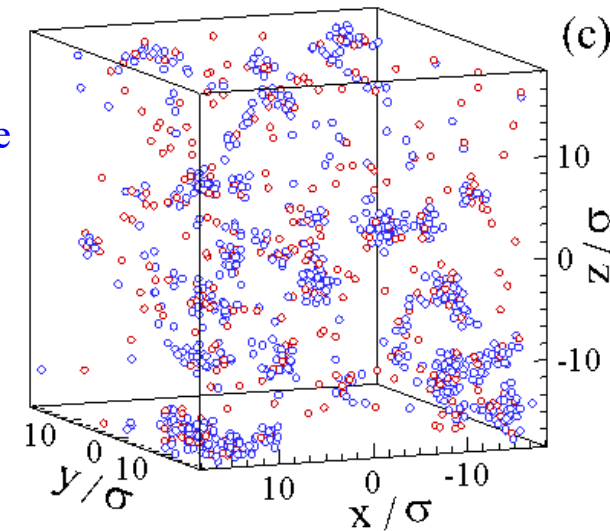
(a)

After 80-th cycle



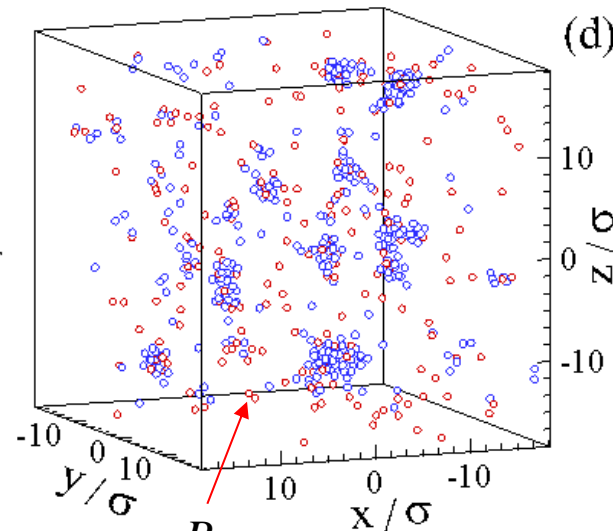
(b)

After 200-th cycle



(c)

After 600-th cycle



(d)

Nearly reversible  
particle dynamics

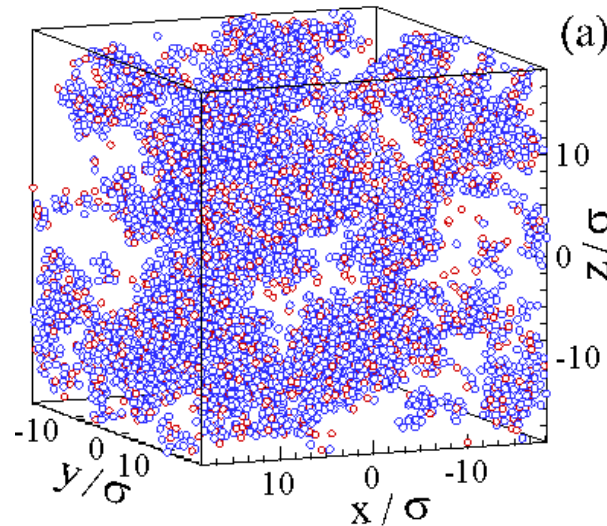


# Spatial configurations of atoms with large nonaffine displacements at $\gamma_0=0.05$

$$D^2(t, T) > 0.04 \sigma^2$$

After 20-th cycle

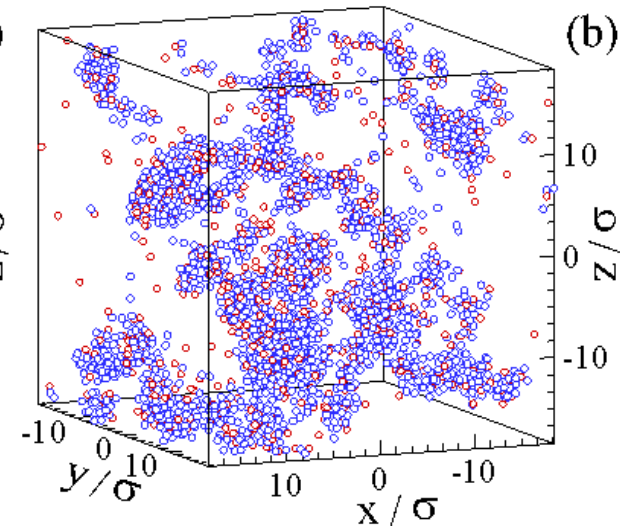
Large clusters  
of nonaffine  
displacements



(a)

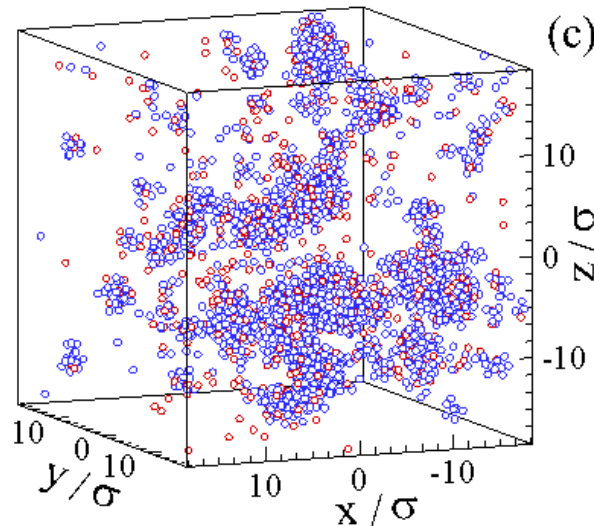
(b)

After 80-th cycle



After 200-th cycle

Small clusters  
of nonaffine  
displacements

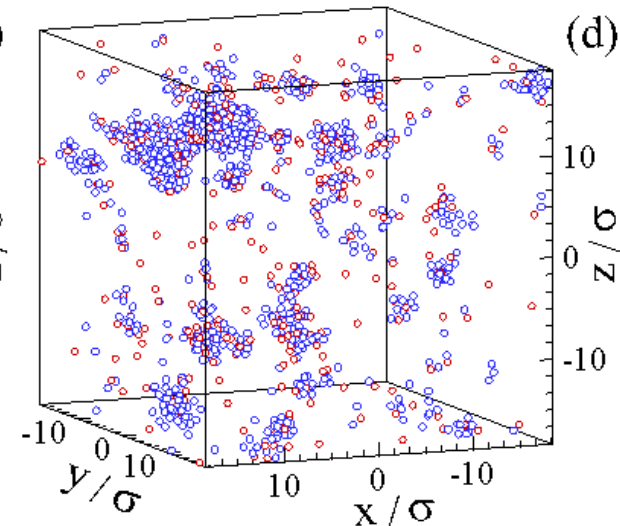


(c)

(d)

After 600-th cycle

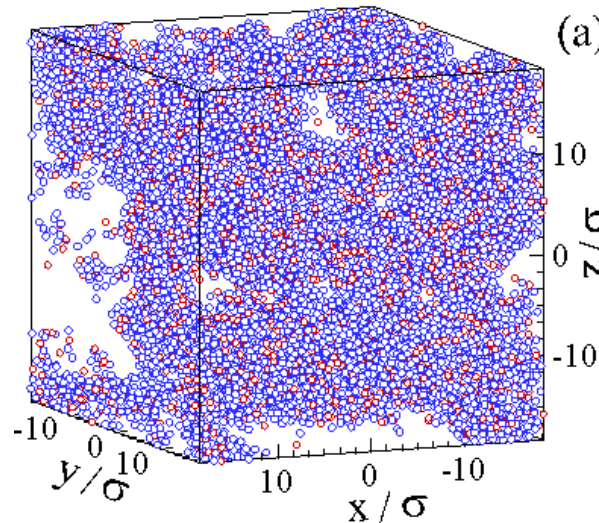
Nearly reversible  
particle dynamics



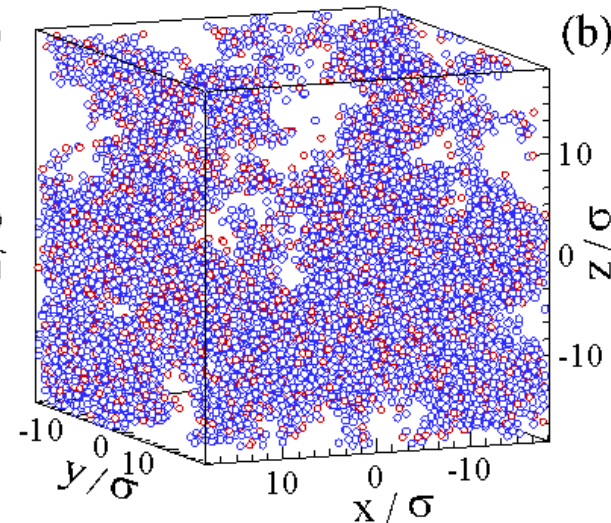
# Spatial configurations of atoms with large nonaffine displacements at $\gamma_0=0.06$

$$D^2(t, T) > 0.04 \sigma^2$$

After 20-th cycle



(a)



(b)

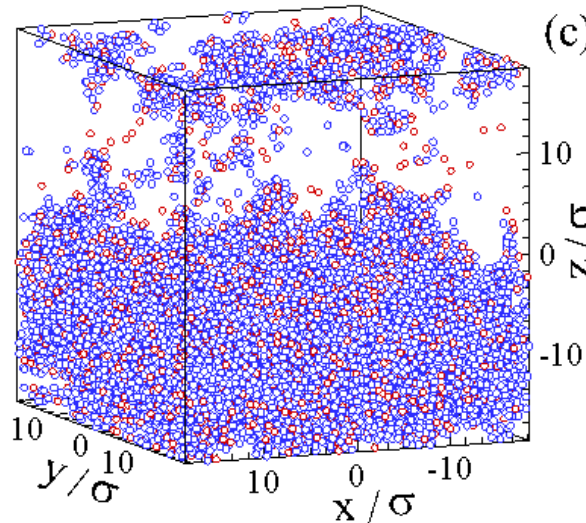
After 80-th cycle

Large shear  
stress amplitude

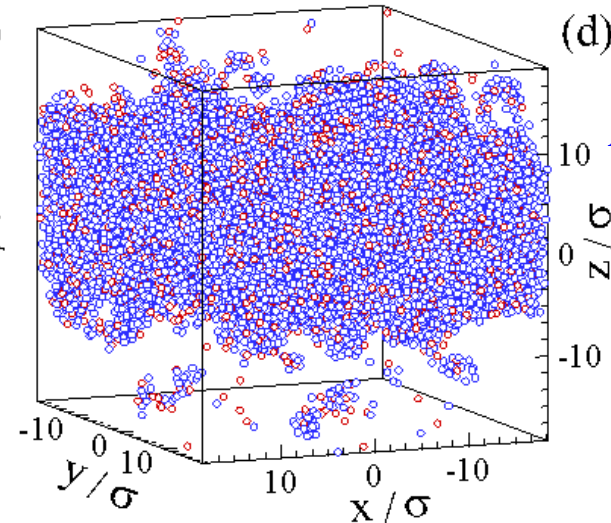
After 200-th cycle

Reduced shear  
stress amplitude

Shear band  
formation



(c)



(d)

After 600-th cycle

Finite width  
of shear band

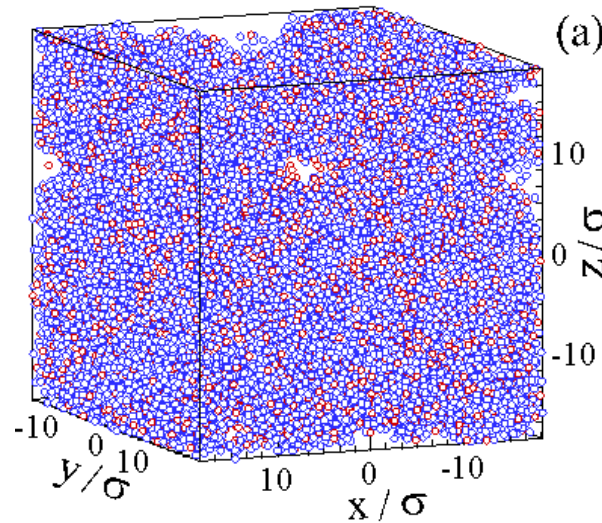
Enhanced  
diffusion



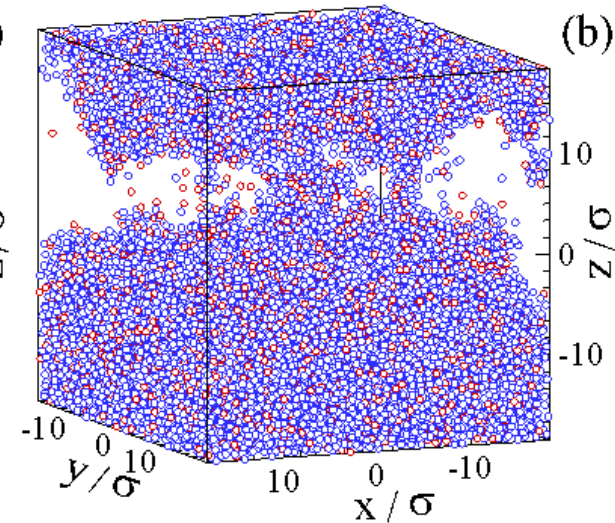
# Spatial configurations of atoms with large nonaffine displacements at $\gamma_0=0.07$

$$D^2(t, T) > 0.04 \sigma^2$$

After 20-th cycle



(a)

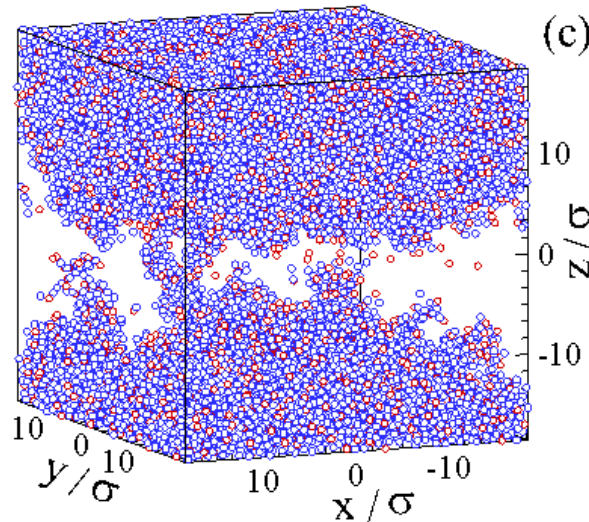


(b)

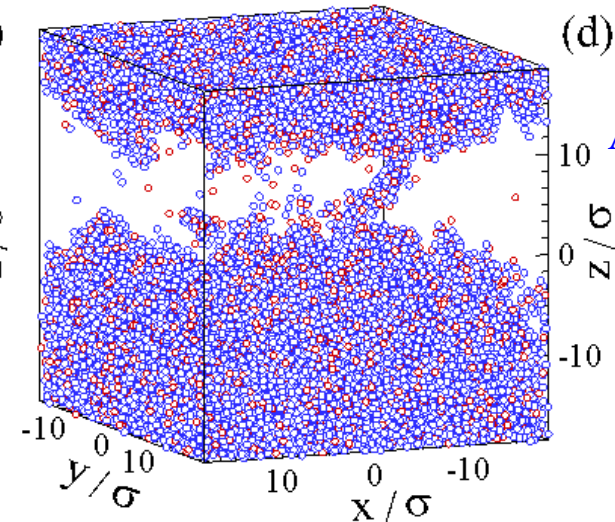
After 80-th cycle

Reduced shear  
stress amplitude  
Shear band  
formation

After 200-th cycle



(c)



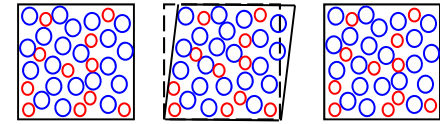
(d)

After 600-th cycle

Finite width  
of shear band

The width of shear band increases with  $\gamma_0$

## Conclusions:



600 cycles

- MD simulations of binary 3D Lennard-Jones glasses under periodic shear at finite  $T_{LJ}$ .
- At small strain amplitudes,  $\gamma_0 \leq 0.05$ : the potential energy acquires progressively lower minima; stress amplitude increases with  $\gamma_0$ ; sparse transient clusters of atoms with large nonaffine displacements; nearly reversible particle dynamics.
- Near the critical strain amplitude,  $\gamma_0 = 0.06$ : the dynamic transition from disconnected clusters to a shear band of large nonaffine displacements: leads to drop in shear stress amplitude.
- At large strain amplitudes,  $\gamma_0 \geq 0.07$ : diffusive particle dynamics; quick formation and growth of shear bands; irreversible particle displacements lead to hysteresis & increase in the potential energy. **The width of shear band increases with  $\gamma_0$**

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