EES216: Circuit Analysis
Midterm Mock Exam

curated by The Peanuts

Name. Nonprawich I. ID. 6622772422 Section. . . . . Seat No. . . . . .

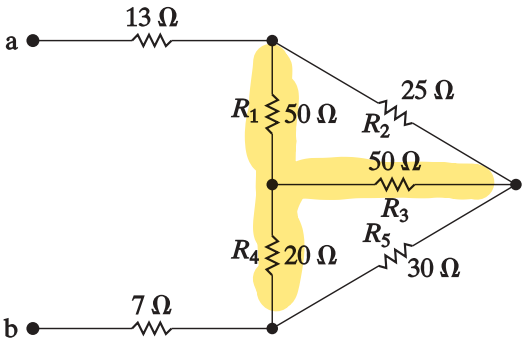
Conditions: Semi-Closed Book

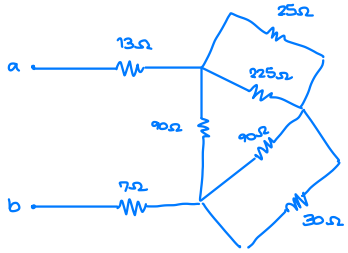
Directions:

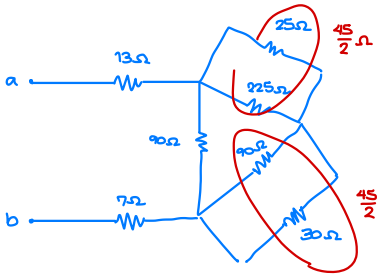
1. This exam has 15 pages (including this page).
2. Calculators are permitted (You may bring 100 of them. Haha)
3. Write your name clearly at the top of each page.
4. Reading the problem is optional but highly recommended.
5. You may bring one A3 sheet of note, which will magically become illegible the moment the exam begins.
6. Tears shed on your answer sheet may cause short circuits. Please cry responsibly.

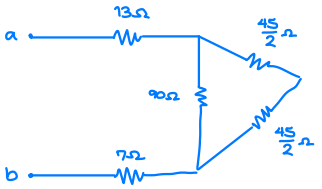
Problem 1

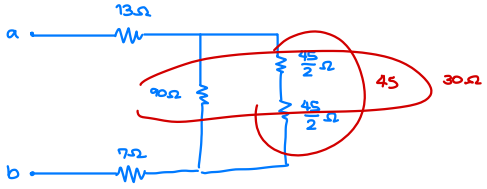
Find the equivalent resistance R_{ab} in the circuit.











$\therefore R_{ab} = 13 + 30 + 7 = 50\ \Omega$ #

Problem 2

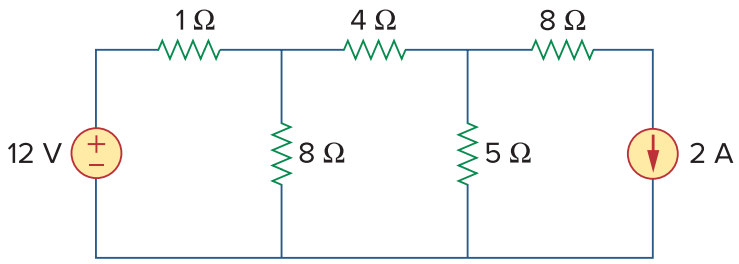
For an ideal operational amplifier (op-amp), state the values of the following characteristics and briefly explain their significance:

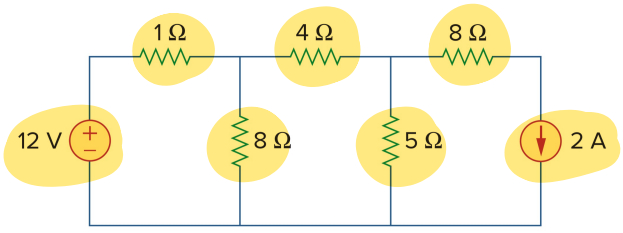
1. Open-loop voltage gain (A) $\infty \rightarrow$ Voltage difference between output is zero.
2. Input resistance (R_i) $\infty \rightarrow$ Current does NOT flow in the op-amp
3. Output resistance (R_o) $0 \rightarrow$ Current to the load is 100%. (No drop)

Problem 3

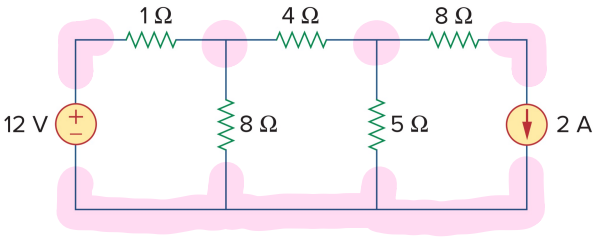
Let a be the number of branches in the circuit, b be the number of nodes, and c be the number of meshes. Then, compute the value of:

$$a^2 + b^2 - c$$

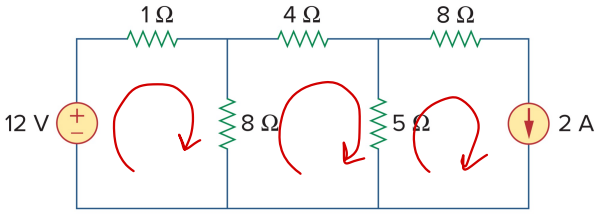




#Branches = a = 7



#Nodes = b = 5



#Mesh = c = 3

$\therefore a^2 + b^2 - c = 7^2 + 5^2 - 3$

$= 49 + 25 - 3$

$= 71$ #

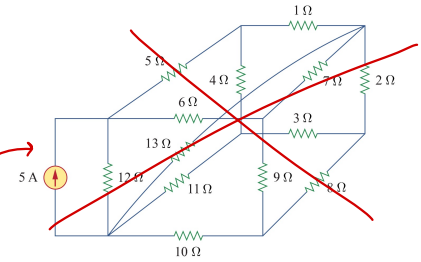
Problem 4

Take the last digit of your student ID and compute:

$$(\text{last digit}) \mod 3$$

Based on the result:

- If the result is 0, find a limitation of **Mesh Analysis**.
- If the result is 1, find a limitation of **Node Analysis**.
- If the result is 2, find a limitation of **Superposition Theorem**.



Limitation of Mesh Analysis

- Not applicable to non-planar circuits
- Becomes complex with many loops
- Difficult with current sources (require transformation) หรือใช้ supermesh

Limitation of Node Analysis

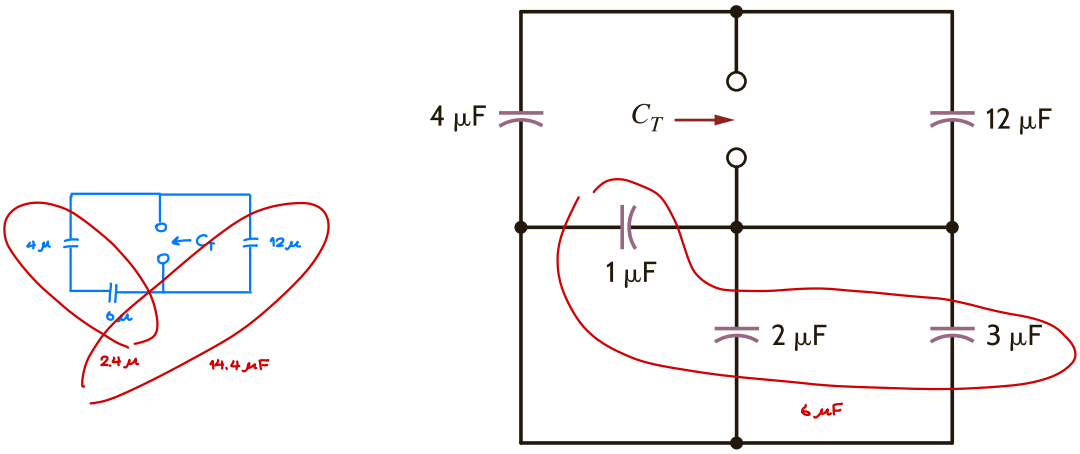
- Not ideal for voltage sources (require transformation) or supernode
- Inefficient for circuits with many nodes

Limitation of Superposition

- Only works for linear circuits → Power is not linear
- Time-consuming for multiple sources
- Does not work for power calculations directly

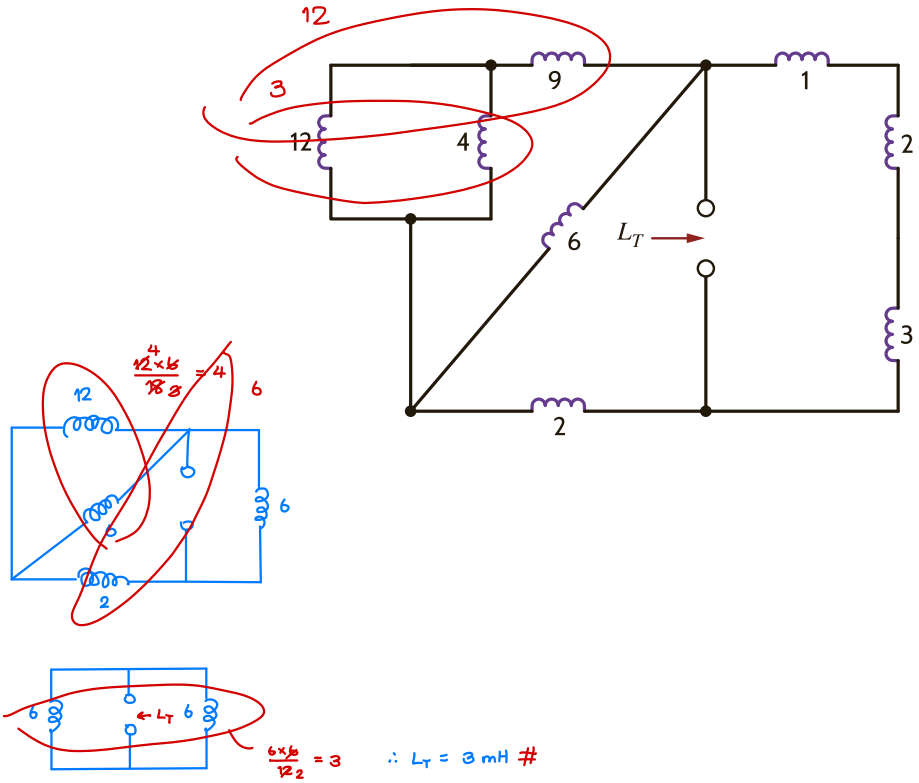
Problem 5

Determine the value of C_T in the circuit



$\therefore C_T = 14.4\ \mu F$ #

Find the total inductance L_T in the circuit, All inductors are in millihenrys.



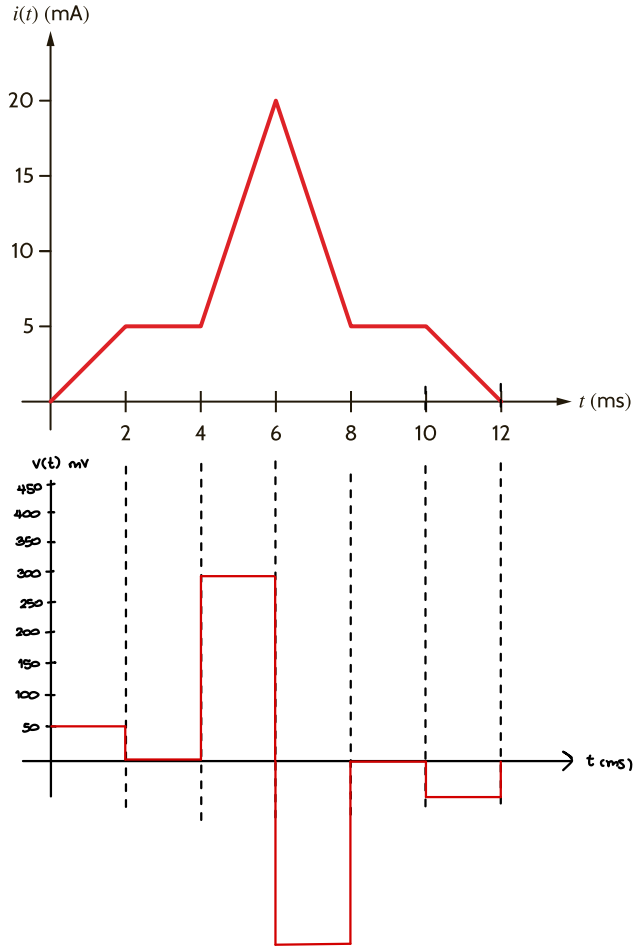
$\therefore L_T = 3\ mH$ #

Problem 6

The current waveform in a 40-mH inductor is shown below. Derive the waveform for the inductor voltage.

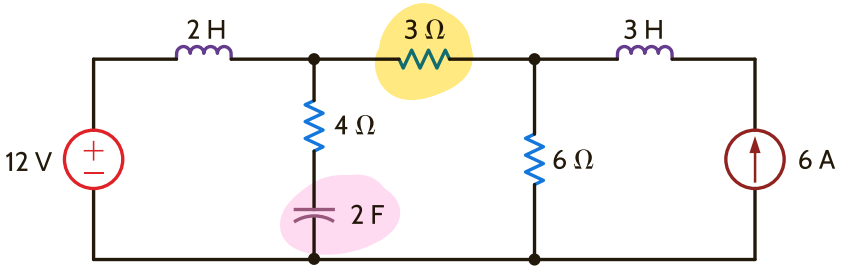
$v = L \frac{di}{dt}$

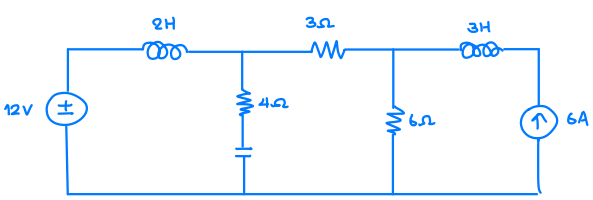
$v = 40$ (Slope)



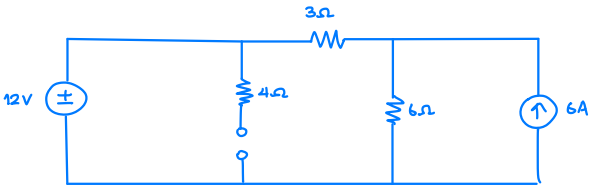
Problem 7

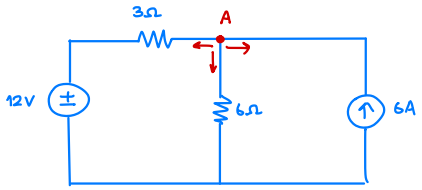
Given the circuit, find the power dissipated in the 3-Ω resistor and the energy stored in the capacitor.





⇒ under DC condition

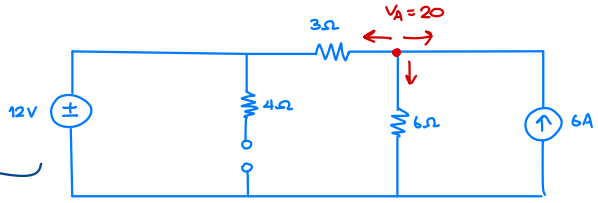




Find power dissipated in $R_{3\Omega}$ from $P = I^2R$

$$\frac{V_A - 12}{3} + \frac{V_A}{6} - 6 = 0$$

$$V_A = 20 \text{ Volt}$$

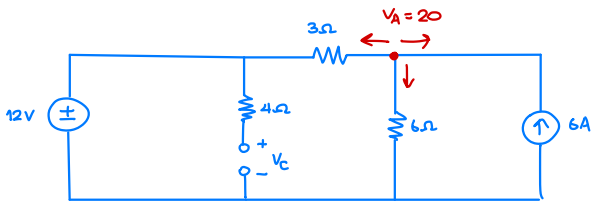


$$I = \frac{V_A - 12}{3} = \frac{20 - 12}{3} = \frac{8}{3} \text{ A}$$

$$\therefore P = I^2R = \left(\frac{8}{3}\right)^2 (3)$$

$$= \frac{64}{3} \text{ watt } \#$$

$W = \frac{1}{2}CV^2$ Find energy stored in the capacitor



$V_C + V_{4\Omega} = V_{6\Omega}$ (Not so sure)

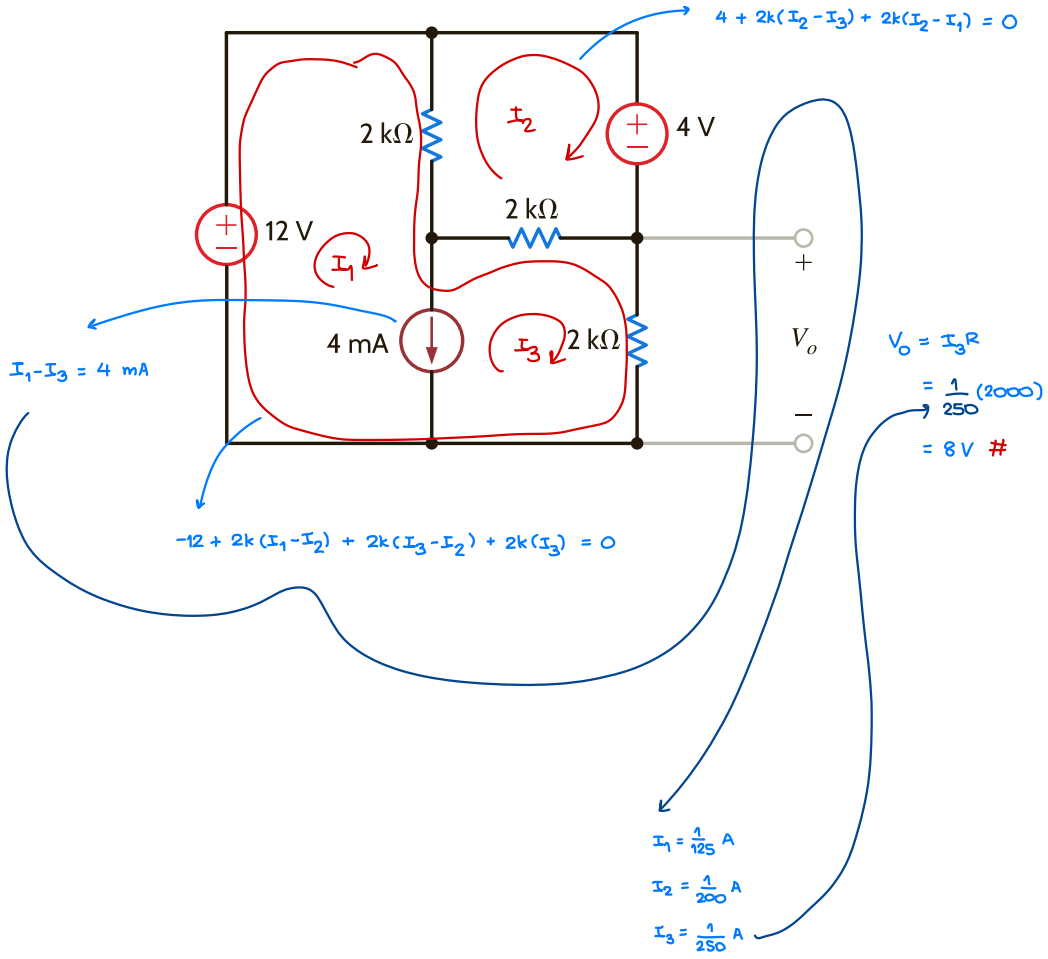
$V_C + 0 = 20$

$V_C = 20$

$W = \frac{1}{2}(2)(20)^2 = 400$ watt #

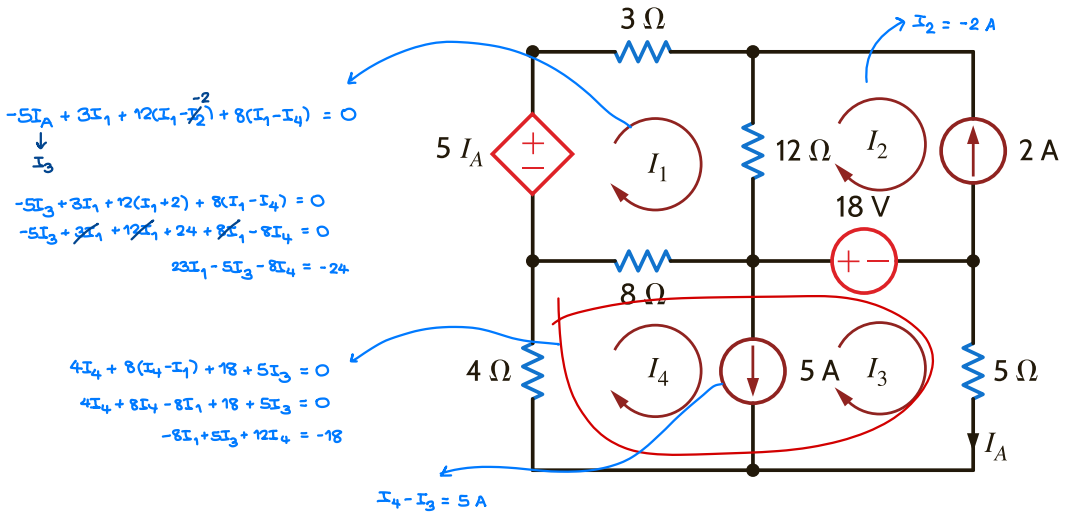
Problem 8

Find V_o in the circuit.



Problem 9

Determine the loop currents I_1, I_2, I_3, I_4 in the given electrical circuit and express the solution in matrix form.



$-5I_A + 3I_1 + 12(I_1 - I_2) + 8(I_1 - I_4) = 0$, with $I_2 = -2$, $I_A = I_3$

$-5I_3 + 3I_1 + 12(I_1 + 2) + 8(I_1 - I_4) = 0$

$-5I_3 + 3I_1 + 12I_1 + 24 + 8I_1 - 8I_4 = 0$

$23I_1 - 5I_3 - 8I_4 = -24$

$4I_4 + 8(I_4 - I_1) + 18 + 5I_3 = 0$

$4I_4 + 8I_4 - 8I_1 + 18 + 5I_3 = 0$

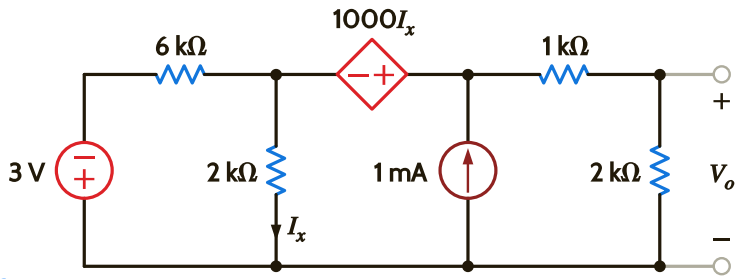
$-8I_1 + 5I_3 + 12I_4 = -18$

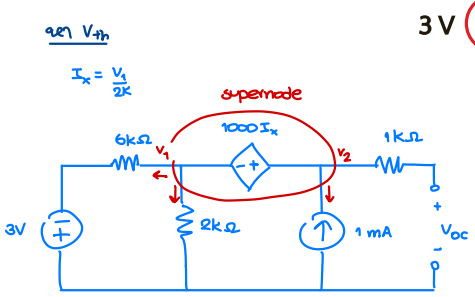
$$\begin{bmatrix} 0 & 0 & -1 & 1 \\ 0 & 1 & 0 & 0 \\ -8 & 0 & 5 & 12 \\ 23 & 0 & -5 & -8 \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \\ I_3 \\ I_4 \end{bmatrix} = \begin{bmatrix} 5 \\ -2 \\ -18 \\ -24 \end{bmatrix}$$

#

Problem 10

Obtain the Thevenin equivalent circuit at terminal.





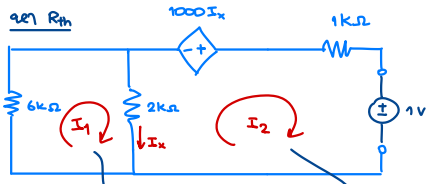
$\frac{V_1+3}{6k} + \frac{V_1}{2k} - 1m = 0$

$V_1 = \frac{3}{4}$ V

$V_2 - V_1 = 1000 I_x$

$V_2 - V_1 = 1000 \left(\frac{V_1}{2k}\right)$

$V_2 = \frac{3}{4} + \frac{3}{4} = \frac{6}{4}$ V $= V_{th}$



$6k(I_1) + 2k(I_1 - I_2) = 0$

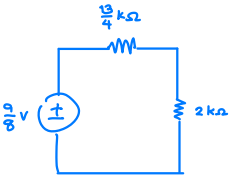
$2k(I_2 - I_1) - 1000 I_x + 1k(I_2) + 1 = 0$

$2k(I_2 - I_1) - 1000(I_1 - I_2) + 1k(I_2) + 1 = 0$

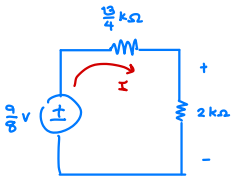
$I_1 = -\frac{1}{13}$ mA

$I_2 = -\frac{1}{3.25}$ mA

$R = \frac{V}{I} = \frac{1}{I} = \frac{1}{-\frac{1}{3.25}\,m} = -\frac{13}{4}$ kΩ



Find V_o in the circuit.



$I = \frac{V}{R}$

$I = \frac{\frac{6}{21}}{\frac{21}{4}} = \frac{3}{14}$ A

$V_{2\Omega} = IR$

$= \frac{3}{14}(2)$

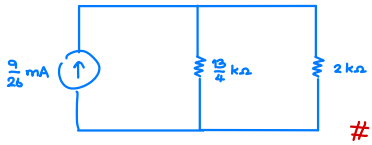
$= \frac{3}{7}$ V #

Find Norton equivalent circuit.

$I = \frac{V}{R}$

$= \frac{\frac{6}{21}}{\frac{13}{4}\,k}$

$= \frac{6}{26}$ mA



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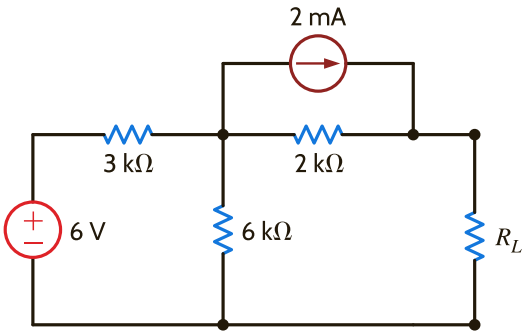
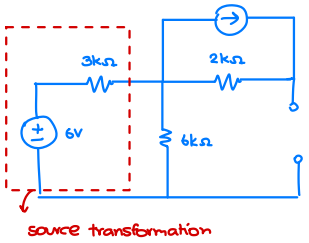
Problem 11

$R_L = R_{th} \rightarrow P_{max}$

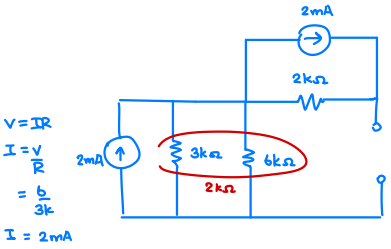
Find R_L for maximum power transfer and the maximum power that can be transferred to the load.



get V_{th}



source transformation

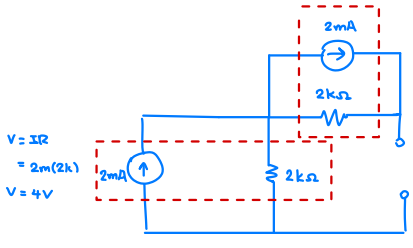


$V = IR$

$I = \frac{V}{R}$

$= \frac{6}{3k}$

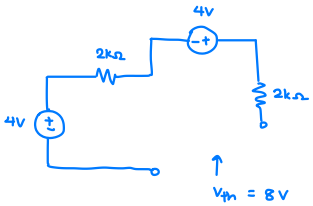
$I = 2mA$



$V = IR$

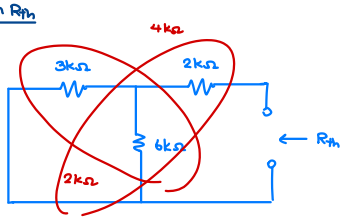
$= 2m(2k)$

$V = 4V$



$V_{th} = 8\,V$

get R_{th}



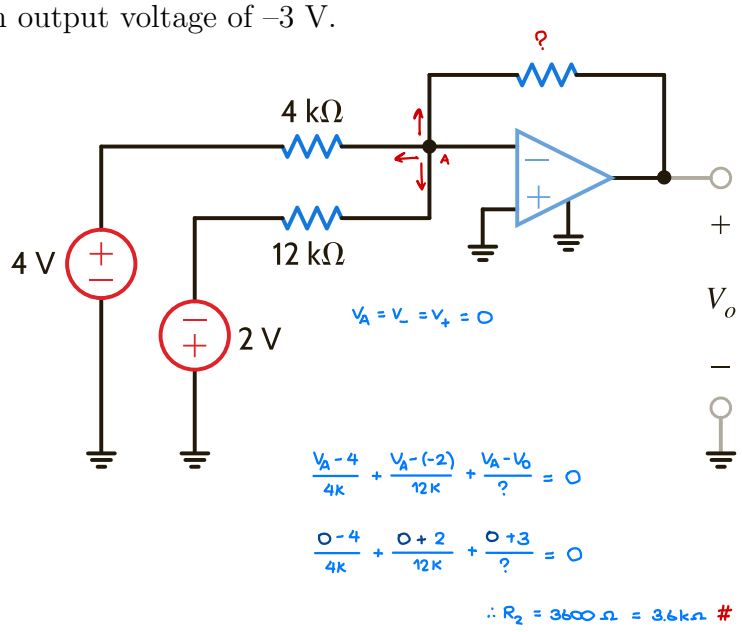
$\therefore R_{th} = 4\,k\Omega$

$\therefore R_L$ for $P_{max} = 4\,k\Omega$ #

$\therefore$ Maximum power $= \frac{V_{th}^2}{4R_{th}} = \frac{8^2}{4(4k)} = 4\,mW$ #

Problem 12

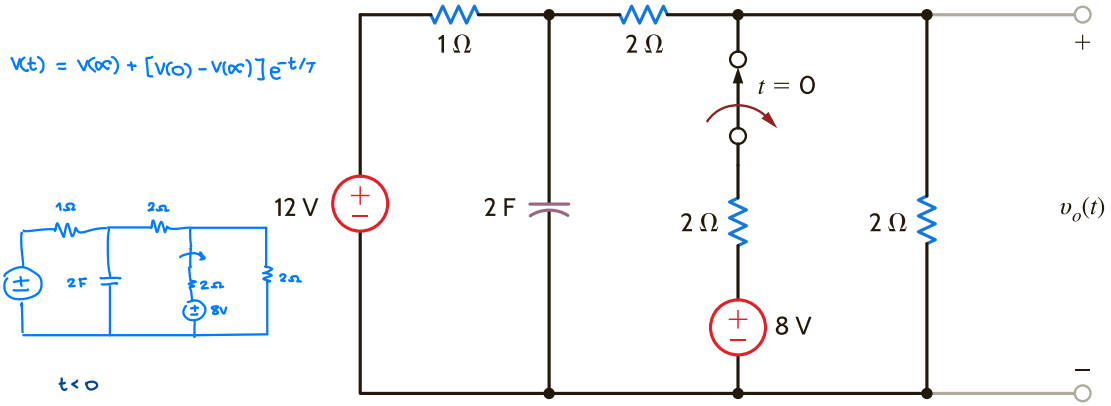
Given the summing amplifier shown below, find the values of R_2 that will produce an output voltage of –3 V.



$v(t) = v(\infty) + [v(0) - v(\infty)]e^{-t/\tau}$

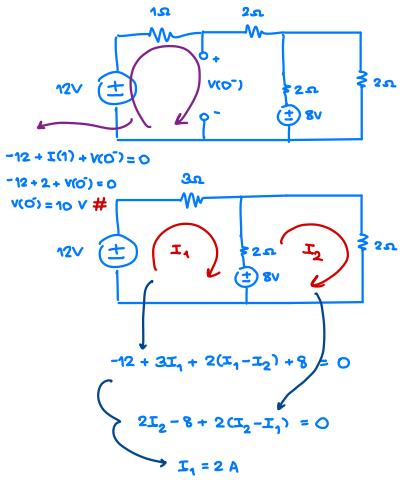
Problem 13

Consider the circuit. The switch opens at t = 0. Find $v_o(t)$ for $t > 0$.

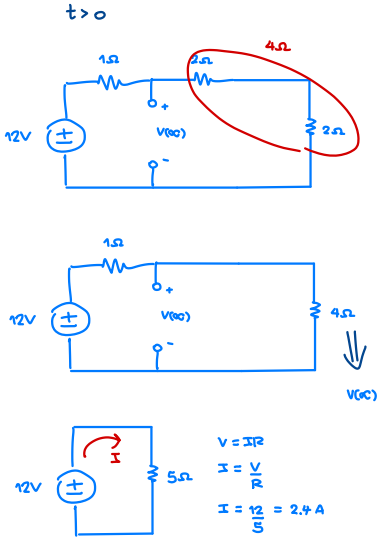


$v(t) = v(\infty) + [v(0) - v(\infty)]e^{-t/\tau}$

t < 0

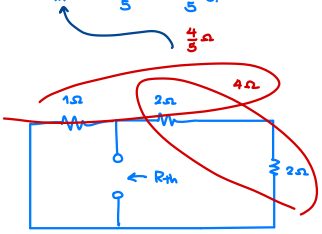


t > 0



Time Constant

$\tau = R_{th}C = \frac{4}{5}(2) = \frac{8}{5}$ s.



$v(t) = v(\infty) + [v(0) - v(\infty)]e^{-t/\tau}$

$= 9.6 + [10 - 9.6]e^{-5t/8}$

$= 9.6 + 0.4e^{-5t/8}$ #

Assume that the circuit reaches steady state after a duration equal to five times the time constant. **Calculate the exact time at which the circuit reaches steady state.**

$\tau = \frac{8}{5}$ s

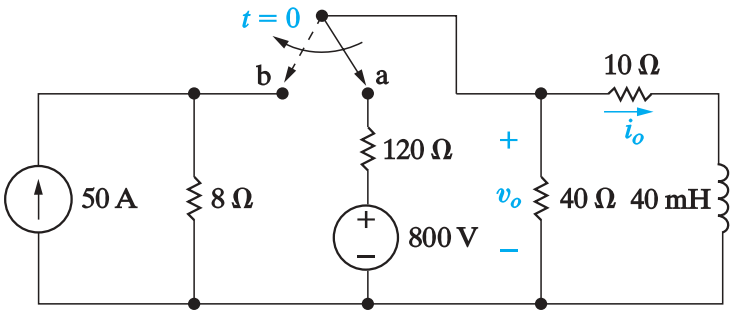
$\therefore 5\tau = 5\left(\frac{8}{5}\right) = 8$ seconds #

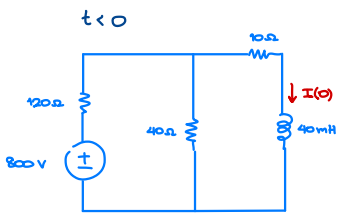
$I(t) = I(\infty) + [I(0) - I(\infty)]e^{-t/\tau}$

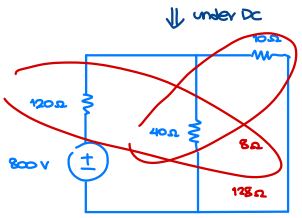
Problem 14

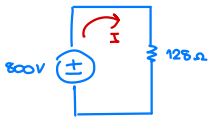
The switch in the circuit shown below has been in position a for a long time. At $t = 0$, the switch moves instantaneously to position b.

- ✓ Find the numerical expression for $i_o(t)$ when $t \geq 0$.
- ✓ Find the numerical expression for $v_o(t)$ when $t \geq 0^+$.





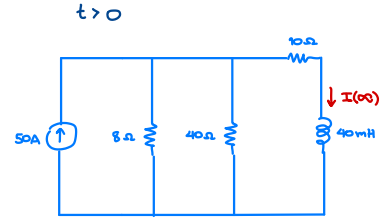


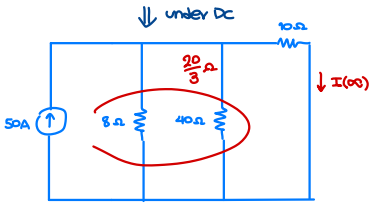


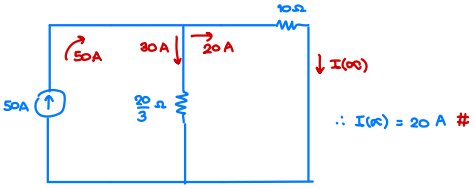
$V = IR$

$I = \frac{800}{128}$

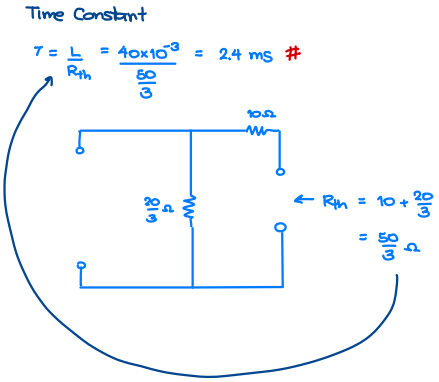
$I = 6.25$ A







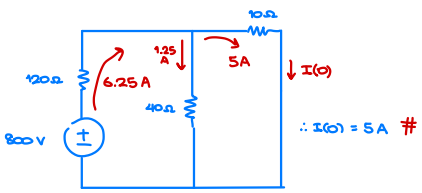
$\therefore I(\infty) = 20$ A #



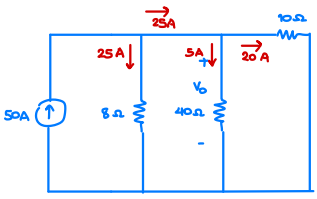
$I(t) = I(\infty) + [I(0) - I(\infty)]e^{-t/\tau}$

$= 20 + [5 - 20]e^{-t/2.4m}$

$= 20 - 15e^{-t/2.4m}$ #



$\therefore I(0) = 5$ A #



$\therefore V_o = IR = 5(40) = 200$ volt #