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- Run the code by using Run all cells.
- Only cell 15, you can predict values by inputting the number of the degree of weight you want to use.
- All non-code questions are also answered in this file and in the correct order.
- Limitation: Because those model choices were made by me, a person that does not have enough knowledge, it might be a bit different from other's work.

Task 1: Systolic Pressure (12 point)

Question 1: Explore and Manipulate the data

```
In [6]: import numpy as np
          import pandas as pd
          import matplotlib.pyplot as plt
 In [7]: # Task 1
          from sklearn.linear_model import LinearRegression, LogisticRegression, Ridge
          from sklearn.preprocessing import PolynomialFeatures
          from sklearn.pipeline import Pipeline
          from sklearn.model selection import cross val score # Calculate MSE
          # Task 2
          from sklearn.decomposition import PCA
          from sklearn.model_selection import train_test_split
          from sklearn.metrics import confusion matrix, precision score, accuracy score
 In [8]: # Import data in Pandas form, make sure having the same namefile
          pressure = pd.read_csv("bloodpressure.csv")
          pressure.head()
 Out[8]:
                               ED-
                                    SMOKING
                                                                  SERUM-
                                                                                                            MARITAL-
                                              EXERCISE WEIGHT
                                                                          SYSTOLIC
                                                                                      IQ SODIUM GENDER
                                                                                                                          NAME
             NUMBER
                                     STATUS
                                                                    CHOL
                                                                                                                         Braund,
          0
                                 2
                                                             120
                                                                      193
                                                                                126
                                                                                    118
                                                                                              136
                                                                                                                       Mr. Owen
                                                                                                                          Harris
                                                                                                                       Cumings,
                                                                                                                       Mrs. John
                                                                                                                         Bradley
          1
                    2
                        18
                                           0
                                                      1
                                                             145
                                                                      210
                                                                                120
                                                                                    105
                                                                                              137
                                                                                                         Μ
                                                                                                                       (Florence
                                                                                                                          Briggs
                                                                                                                           Th...
                                                                                                                       Heikkinen,
                                           0
                                                             118
                                                                                                         F
                                                                                              135
                                                                                                                           Miss.
                                                                                                                          Laina
                                                                                                                        Futrelle,
                                                                                                                           Mrs.
                                                                                                                        Jacques
          3
                                 2
                                           0
                                                             162
                                                                      208
                        24
                                                      1
                                                                                129
                                                                                    108
                                                                                              142
                                                                                                         M
                                                                                                                          Heath
                                                                                                                        (Lily May
                                                                                                                           Peel)
                                                                                                                       Allen, Mr.
                    5
                        19
                                                             106
                                                                      188
                                                                                119
                                                                                    106
                                                                                              133
                                                                                                                         William
                                                                                                                          Henry
 In [9]:
          systolic = pressure['SYSTOLIC']
          systolic = systolic.to numpy().reshape(-1, 1)
In [10]:
          pressure predictor = pressure.drop(["ID-NUMBER", "SYSTOLIC", "NAME"], axis=1)
          pressure_predictor.head()
Out[10]:
             AGE ED-LEVEL SMOKING STATUS EXERCISE WEIGHT SERUM-CHOL
                                                                                  IQ
                                                                                     SODIUM GENDER
                                                                                                       MARITAL-STATUS
                          2
                                                              120
                                                                                                     F
          0
               27
                                                       1
                                                                            193 118
                                                                                          136
                                                                                                                      M
               18
                                            0
                                                              145
                                                                            210 105
                                                                                          137
                                                                                                                      S
          1
                          1
                                                                                                    M
          2
                          2
                                            0
                                                       0
                                                                                                     F
                                                              118
                                                                            196
                                                                                115
                                                                                          135
                                                                                                                      Μ
                          2
          3
               24
                                            0
                                                              162
                                                                            208
                                                                                 108
                                                                                          142
                                                                                                                      M
                                                                                                     F
                          1
                                            2
                                                       0
                                                                                                                      S
               19
                                                              106
                                                                            188 106
                                                                                          133
```

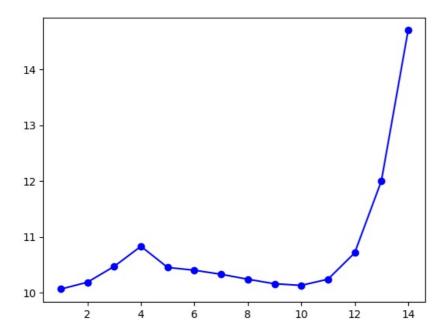
```
pressure_predictor = pd.get_dummies(pressure_predictor, drop_first=True)
# To keep all values in the numeric value
# Change categorical value to integer to use the linear regression (categorical value do not work)
pressure_predictor["GENDER_M"] = pressure_predictor["GENDER_M"].astype(np.int8)
pressure_predictor["MARITAL-STATUS_M"] = pressure_predictor["MARITAL-STATUS_S"].astype(np.int8)
pressure_predictor["MARITAL-STATUS_W"] = pressure_predictor["MARITAL-STATUS_W"].astype(np.int8)
pressure_predictor.head()
```

it[11]:		AGE	ED- LEVEL	SMOKING STATUS	EXERCISE	WEIGHT	SERUM- CHOL	IQ	SODIUM	GENDER_M	MARITAL- STATUS_M		MARITAL- STATUS_W
	0	27	2	1	1	120	193	118	136	0	1	0	0
	1	18	1	0	1	145	210	105	137	1	0	1	0
	2	32	2	0	0	118	196	115	135	0	1	0	0
	3	24	2	0	1	162	208	108	142	1	1	0	0
	4	19	1	2	0	106	188	106	133	0	0	1	0

Question 2: Polynomial Regression

- a. Create polynomial regression models using the whole dataset to predict systolic pressure using the "WEIGHT" feature, for polynomial degrees ranging from 1 to 14.
- b. Perform 10-fold cross-validation
- . c. Compute and display the mean RMSEs of the 10-fold cross-validation for each of the 14 polynomial degrees
- d. Produce a cross-validation error plot showing the mean RMSE for polynomial degrees from 1 to 14

```
In [13]: X = pressure predictor["WEIGHT"].to numpy().reshape(-1, 1) # Change into numpy value with 1 column and as many
         y = systolic
In [14]: poly List models = {} # Store polynomial models
         poly positive mse 10foldcv = {} # Store MSE
         poly_rmse = {} # Store mean of RMSE of each model
         for degree in range(1,15):
             # a. Create polynomial regression models to predict Systolic using "Weight", from degree 1 to 14
             poly_features = PolynomialFeatures(degree = degree, include_bias = False) # Set a standard polynomial features
             model = Pipeline([
                 ("poly_features", poly_features), # X will be transformed into X_poly with corresponding degree
                 ("lin reg", LinearRegression()), # Then X poly will be put in the LinearRegression
             1)
             model.fit(X,y) # Transforming then Fitting
             poly_List_models[f'model{degree}'] = model # Storing
             # b. 10-fold cross validation
             positive mse scores = -cross_val_score(model, # Fitted from Pipeline
                                                     X, y, scoring='neg_mean_squared_error', cv=10)
             poly positive mse 10foldcv[f'MSE{degree}'] = positive mse scores # Storing
             # c. RMSEs of 10-fold CV for each degree
             rmse_scores = np.sqrt(positive_mse_scores)
             mean rmse scores = np.mean(rmse scores)
             poly_rmse[f'RMSE{degree}'] = mean_rmse_scores # Storing
In [15]: # Testing for prediction a random degree
         testing degree = input('Enter a degree from 1-14:')
         model_degree = 'model'+testing_degree
         testing_model = poly_List_models[model_degree]
         X_{\text{new}} = [[120], [100], [150]]
         testing model.predict(X new)
Out[15]: array([[123.26079107],
                 [113.37949757]
                 [131.72119164]])
In [16]: # d. Visualisation
         print('RMSE of 14 models', poly_rmse.values())
         plt.plot(range(1,15), poly_rmse.values(), "bo-")
        RMSE of 14 models dict values([10.063566348213604, 10.187166706053542, 10.470321681840364, 10.829963377150463, 1
        0.45133716702582,\ 10.4\overline{0}18597256369,\ 10.329004499108617,\ 10.240305476454346,\ 10.159177954821084,\ 10.1302942634471
        53, 10.240212879403142, 10.712133802678924, 12.002013373747856, 14.697035935941656])
Out[16]: [<matplotlib.lines.Line2D at 0x12ff5db50>]
```



Question 3: Model selection for polynomial regression

- a. Select the best polynomial degree and briefly explain your choice
- b. Print the intercept and coefficients of the selected model

```
In [18]: # a. Choose best model
    list_poly_rmse = np.array(list(poly_rmse.values()))
    index_poly_rmse = np.argsort(list_poly_rmse)+1
    # Index start at 0, plus 1 to make it easier to read
    index_poly_rmse
```

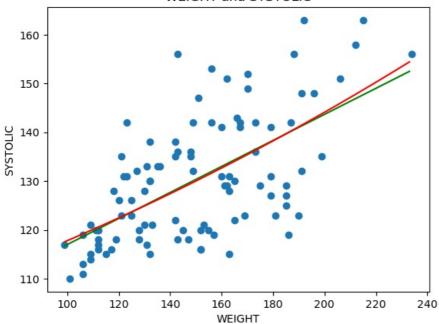
```
Out[18]: array([ 1, 10, 9, 2, 11, 8, 7, 6, 5, 3, 12, 4, 13, 14])
```

Consider first four degree because they give the smallest RMSE among 14 degrees.

- Degree 10 and 9 would be a bit overfitting so they will be ignored
- Then having a look at the below graph to see how degree 1 and 2 work

```
In [20]: X_plot = np.array(range( 99, 234, 1)) # min and max of X
## Take intercepts and coefficients in the draft and only show the best one below
y_degree1 = 90.28431413226751 + 0.2669545938540424*X_plot
y_degree2 = 98.911250919365 + 0.15125235*X_plot + 0.00037347 * X_plot**2
## Visualising
plt.scatter(X, y) # orginal data in blue
plt.plot(X_plot, y_degree1, 'g') # degree 1 in green
plt.plot(X_plot, y_degree2, 'r') # degree 2 in red
plt.xlabel('WEIGHT')
plt.ylabel('SYSTOLIC')
plt.title('WEIGHT and SYSTOLIC')
plt.show()
```

WEIGHT and SYSTOLIC



2 models produce a relatively similar in the the regression line. Although model of degree 1 indeed offers a smaller amount of RMSE, I would rather go to model of degree 2.

- Model 1, which is basically linear, could be underfitting in some extent because when looking at the graph above, we could see there is no clear pattern of a basic linearity.
- On the other hand, despite having a slightly higher number in RMSE, it could still serve the same regression as model 1 does in the particular range. Besides, when the value X (Weight) reach 200-ish, the red model (degree 2) could identify the difference and start moving up in the line graph.
- Therefore, the model with degree 2 will be chosen.

```
In [22]: best_degree = 2
print("Degree", best_degree)

Degree 2
```

```
In [23]: # b. Print intercept and coefficients of the model
    best_model = poly_List_models['model'+str(best_degree)]
    # Result would be the Pipeline with 2 steps: Poly transform and Linear regression
    lin_reg_best_model = best_model.named_steps['lin_reg'] # Only access the Linear Regression step

intercept = lin_reg_best_model.intercept_[0]
    coefficients_1 = lin_reg_best_model.coef_[0,0]
    coefficients_2 = lin_reg_best_model.coef_[0,1]
    print("Intercept", intercept)
    print("Coefficients", coefficients_1, 'and', coefficients_2)
    print(f'Best_equation: Systolic = {intercept} + {coefficients_1} Weight + {coefficients_2} Weight^2')
```

Intercept 98.911250919365
Coefficients 0.15125234579213007 and 0.00037346540241700046
Best equation: Systolic = 98.911250919365 + 0.15125234579213007 Weight + 0.00037346540241700046 Weight^2

Question 4: Multiple Linear Regression

- a. Create a multiple linear regression model to predict systolic pressure using all the other relevant useful features in the dataset.
- b. Print the intercept and coefficients of the model.
- c. Perform 10-fold cross-validation.
- d. Compute and display the mean RMSE for the 10-fold cross-validation

```
multi_intercept = lin_reg_multi.intercept_[0]
         multi_coefficients = lin_reg_multi.coef_
         print("Intercept", multi_intercept)
         print("Coefficients", multi_coefficients)
        Intercept 69.14256088196578
        Coefficients [[ 0.37180203 - 0.83445173 - 0.08319725 - 0.11105294
                                                                             0.3004112
           0.01360296 -0.05463374 0.08452103 -10.87181364 0.60239764
           -0.11053997 -4.47617349]]
In [28]: # c. 10-fold cross-validation
         mse_score_multi = -cross_val_score(lin_reg_multi, X_multi, y_multi, cv=10, scoring='neg_mean_squared_error')
         print("MSE scores for 10-fold:", mse_score_multi)
         # d. mean RMSE
         rmse_multi = np.mean(np.sqrt(mse_score_multi))
         print("Mean RMSE:", rmse_multi)
        MSE scores for 10-fold: [75.42004641 53.94956458 74.57654424 39.51401931 55.51622802 50.61795498
        32.80881046 74.47990128 67.63895163 54.308156 ]
        Mean RMSE: 7.546861673936118
```

Question 5: Ridge Regression

- a. Build a Ridge regression model for the multiple linear regression model created in item 4 with a regularization parameter $\alpha = 0.1$
- b. Print the intercept and coefficients of the model
- . c. Perform 10-fold cross-validation
- d. Compute and display the mean RMSE for the 10-fold cross-validation.

```
In [30]: y ridge = systolic # Different name for different model, but the same value
         X ridge = pressure predictor.to_numpy() # Whole remaining dataset with dummies
         alpha = 0.1
In [31]: # a. Ridge model with alpha = 0.1
         ridge reg = Ridge(alpha = alpha, solver = "cholesky") # Update new alpha
         ridge reg.fit(X ridge, y ridge)
         # b. Intercept and Coefficients
         ridge_intercept = ridge_reg.intercept_[0]
         ridge_coefficients = ridge_reg.coef_
         print("Intercept", ridge_intercept)
         print("Coefficients", ridge coefficients)
        Intercept 69.13966661213357
        Coefficients [[ 0.3722703 -0.83170596 -0.07951758 -0.12025351
                                                                            0.29872371
           0.0134391 -0.05442173 0.08578891 -10.76454194 0.62400999
           -0.09656377 -4.38823966]]
In [32]: # c. 10-fold cross-validation
         mse_score_ridge = -cross_val_score(ridge_reg, X_ridge, y_ridge, cv=10, scoring='neg_mean_squared_error')
         print("MSE scores for 10-fold:", mse score ridge)
         # d. mean RMSE
         rmse ridge = np.mean(np.sqrt(mse score ridge))
         print("Mean RMSE:", rmse_ridge)
        MSE scores for 10-fold: [75.70264387 54.27396138 74.3962837 39.42073141 55.04450843 50.61497325
        32.37145079 74.43886849 67.6710702 54.38217405]
        Mean RMSE: 7.5423410378856115
```

Question 6: Model Comparison

Best RMSE of 3 models to predict Systolic are:

- 10.187166706053542 of Polynomial Regression Model with degree 2 for Weight
- 7.546861673936118 of **Multiple Linear Regression Model** with all features considered
- 7.5423410378856115 of Ridge Regression Model with all features considered

I choose Ridge Regression because of some of following reasons:

- Ridge Regression has the lowest score in terms of Mean RMSE compared to other methods
- · Polynomial Regression only uses 1 variable to predict while Systolic pressure could be derived from multiple factors
- Some features in Multiple Linear Regression may have multicollinearity, for example: EXERCISE and WEIGHT, WEIGHT and SERUM-CHOL, AGE and IQ. Hence using Ridge Regression could handle multicollinearity by adjusting coefficients of those correlated features for better prediction.

Task 2: MNIST Digit Classification (8 point)

1. Load the renowned MNIST ('mnist 784') dataset, which consists of a large collection of handwritten digit images. Your task is to reduce the number of features first, and then build a binary classification model to distinguish between the digit "7" and all other digits (not "7").

```
In [36]: from sklearn.datasets import fetch_openml
          mnist = fetch_openml('mnist_784', version=1, as_frame=False)
         print(list(mnist.keys()))
         ['data', 'target', 'frame', 'categories', 'feature names', 'target names', 'DESCR', 'details', 'url']
In [37]: print(mnist["data"])
         print(mnist["target"]) # type: object
         [[0 \ 0 \ 0 \ \dots \ 0 \ 0]]
          [0 0 0 ... 0 0 0]
          [0 0 0 ... 0 0 0]
         [0 0 0 ... 0 0 0]
          [0\ 0\ 0\ \dots\ 0\ 0\ 0]
          [0 \ 0 \ 0 \ \dots \ 0 \ 0 \ 0]]
        ['5' '0' '4' ... '4' '5' '6']
In [38]: X = mnist["data"]
                                # predictor variables
          y = mnist["target"] # target variable
          y = (y == '7')
                                # '7' is object varible instead of number
          # Change value into True if it is '7'. Otherwise, it will be False
         y = y.astype(np.int8) # 1 when True. 0 when False
          print(y)
         [0 0 0 ... 0 0 0]
```

2. Perform Principal Component Analysis (PCA) on the feature data to reduce its dimensionality while retaining 90% of the overall explained variance.

```
In [40]: pca = PCA(n_components = 0.9)
X_reduced = pca.fit_transform(X)
```

3. Split the data into training and testing sets, using a common split ratio of 80% for training and 20% for testing.

4. Create a Logistic Regression model using the reduced feature dataset.

5. Use this model to predict the labels for both the training and testing dataset.

```
In [47]: train_prediction = log_reg.predict(X_train)
  test_prediction = log_reg.predict(X_test)
```

6. Print the number of principal components preserved. Print the prediction accuracy (proportion of correct predictions) of your model on the training set. Also, print the prediction accuracy, the confusion matrix, and the misclassified digits (i.e. wrong predictions) of your model on the testing set.

```
In [49]: print("PCs preserved:", X_reduced.shape[1], "\n")

print("Training set Prediction \n", confusion_matrix(train_prediction, y_train))
print("Training Precision of classifier:", round(precision_score(y_train, train_prediction),4))
print("Training Accuracy rate:", round(accuracy_score(y_train, train_prediction),4))
```

```
print("\nTesting set Prediction \n", confusion matrix(test prediction, y test))
 print("Testing Precision of classifier:", round(precision score(y test, test prediction),4))
 print("Testing Accuracy rate:", round(accuracy score(y test, test prediction),4))
 index misclassed digits = np.where(test prediction != y test)
 index_string = ', '.join(map(str, index_misclassed_digits[0]))
 print("\nThe model classifies wrong", len(index misclassed digits[0]), "places for testing dataset at indexes:"
PCs preserved: 87
Training set Prediction
[[49897
         5261
 [ 293 5284]]
Training Precision of classifier: 0.9475
Training Accuracy rate: 0.9854
Testing set Prediction
[[12422 146]
 [ 95 1337]]
Testing Precision of classifier: 0.9337
Testing Accuracy rate: 0.9828
```

The model classifies wrong 241 places for testing dataset at indexes: 35, 37, 337, 374, 511, 521, 619, 626, 655, 750, 751, 788, 909, 939, 1025, 1320, 1354, 1476, 1507, 1529, 1533, 1599, 1612, 1654, 1800, 1876, 1999, 2008, 206 1, 2099, 2125, 2195, 2213, 2259, 2309, 2318, 2331, 2339, 2347, 2591, 2621, 2677, 2700, 2758, 2826, 2879, 2888, 2 910, 2921, 3067, 3198, 3314, 3341, 3375, 3391, 3430, 3663, 3761, 3776, 3797, 3821, 3822, 3851, 3925, 3926, 4027, 4033, 4062, 4064, 4072, 4085, 4088, 4129, 4164, 4167, 4368, 4372, 4458, 4482, 4603, 4646, 4751, 4756, 4790, 4846, 4909, 4932, 4993, 5053, 5179, 5232, 5356, 5597, 5598, 5609, 5776, 6013, 6036, 6102, 6144, 6167, 6269, 6281, 63 94, 6455, 6570, 6641, 6655, 6689, 6692, 6767, 6817, 6831, 6946, 6955, 6979, 7109, 7152, 7192, 7220, 7227, 7321, 7338, 7339, 7459, 7515, 7577, 7599, 7626, 7628, 7726, 7742, 7867, 7898, 7915, 7939, 7941, 7974, 8011, 8039, 8086, 8096, 8190, 8278, 8288, 8297, 8426, 8428, 8532, 8583, 8602, 8636, 8657, 8671, 8728, 8759, 8947, 8992, 9132, 92 29, 9234, 9258, 9330, 9421, 9464, 9483, 9488, 9625, 9737, 9767, 9777, 9850, 10000, 10101, 10234, 10238, 10248, 1 0264, 10291, 10325, 10326, 10449, 10458, 10600, 10605, 10642, 10751, 10793, 10855, 10935, 10937, 10949, 10965, 1 0978, 11034, 11142, 11156, 11195, 11296, 11345, 11379, 11460, 11503, 11547, 11776, 11824, 11855, 11931, 12034, 1 2048, 1 2139, 12178, 12263, 12349, 12410, 12459, 12493, 12517, 12651, 12666, 12690, 12818, 12890, 12910, 12984, 1 3085, 13169, 13185, 13206, 13234, 13236, 13391, 13503, 13522, 13623, 13676, 13705, 13741, 13927, 13954, 13983

7. Evaluate the model: What do you think of the model generated (good, underfitting, overfitting)? Briefly explain your reasoning.

In my opinion, this model works well due to the high accuracy rate in both training and validating data. Although I only used PCA with 90% of explained variance (reducing dimension to 87 remaining from 784 original features), it still achieves a high level of predicting accuracy (around 98%), which is really impressive. On top of that, when reducing dimensions, it could keep the model from being overfitting, and 90% is a sufficient number of features to keep the model good, instead of being underfitting.

Processing math: 100%