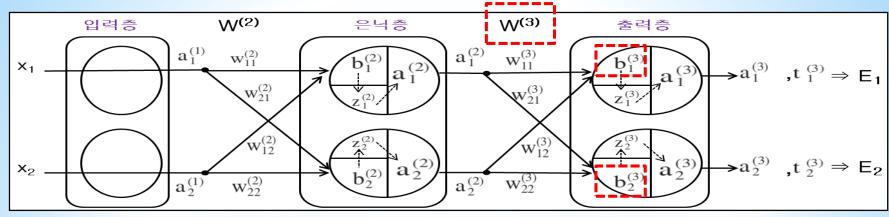
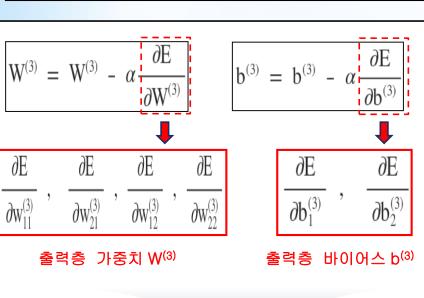
파이썬(Python)으로 구현하는

## 오차역전파 (Back Propagation)

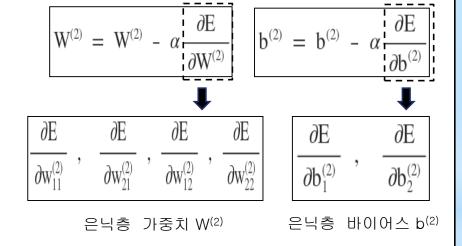
- 출력층에서의 오차역전파-

## 출력층 오차역전파 공식 유도 - 출력층 가중치 W(3) / 출력층 바이어스 b(3)





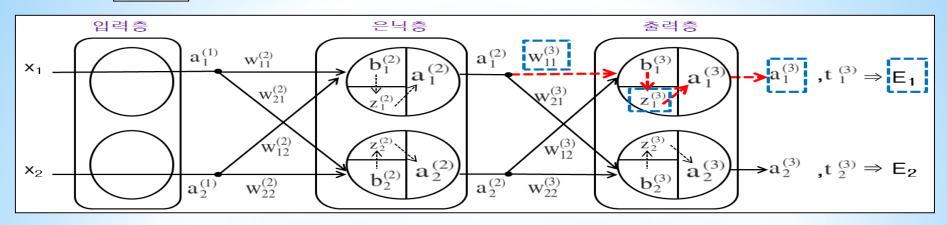
 $\partial E/\partial W^{(3)}$  ,  $\partial E/\partial b^{(3)}$  오차역전파 공식 유도



 $\partial E/\partial W^{(2)}$  ,  $\partial E/\partial b^{(2)}$  오차역전파 공식 유도



 $\frac{\partial E}{\partial w_{11}^{(3)}}$ 



$$\frac{\partial E}{\partial w_{11}^{(3)}} = \frac{\partial E_1}{\partial w_{11}^{(3)}} + \frac{\partial E}{\partial w_{11}^{(3)}}$$

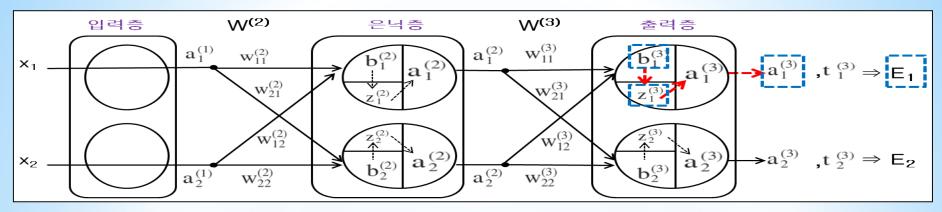
$$= \frac{\partial E_1}{\partial a_1^{(3)}} \times \frac{\partial a_1^{(3)}}{\partial z_1^{(3)}} \times \frac{\partial z_1^{(3)}}{\partial w_{11}^{(3)}}$$

$$= \frac{\partial \left\{ \frac{1}{2} (t_1^{(3)} - a_1^{(3)})^2 \right\}}{\partial a_1^{(3)}} \times \frac{\partial sigmoid(z_1^{(3)})}{\partial z_1^{(3)}} \times \frac{\partial (a_1^{(2)}w_{11}^{(3)} + a_2^{(2)}w_{12}^{(3)} + b_1^{(3)})}{\partial w_{11}^{(3)}}$$

$$= (a_1^{(3)} - t_1^{(3)}) \times sigmoid(z_1^{(3)}) \times (1-sigmoid(z_1^{(3)})) \times a_1^{(2)}$$

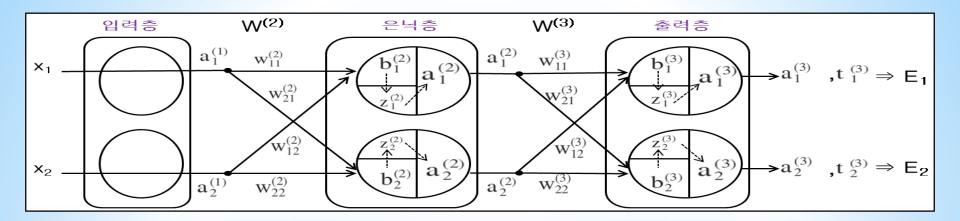
$$= (a_1^{(3)} - t_1^{(3)}) \times a_1^{(3)} \times (1-a_1^{(3)}) \times a_1^{(2)}$$





$$\begin{array}{|c|c|c|c|} \hline \frac{\partial E}{\partial b_1^{(3)}} &=& \frac{\partial E_1}{\partial b_1^{(3)}} &+& \frac{\partial E_2}{\partial b_1^{(3)}} \\ &=& \frac{\partial E_1}{\partial a_1^{(3)}} \times \frac{\partial a_1^{(3)}}{\partial z_1^{(3)}} \times \frac{\partial z_1^{(3)}}{\partial b_1^{(3)}} \\ &=& \frac{\partial \left\{ \frac{1}{2} (t_1^{(3)} - a_1^{(3)})^2 \right\}}{\partial a_1^{(3)}} \times \frac{\partial sigmoid(z_1^{(3)})}{\partial z_1^{(3)}} \times \frac{\partial (a_1^{(2)}w_{11}^{(3)} + a_2^{(2)}w_{12}^{(3)} + b_1^{(3)})}{\partial b_1^{(3)}} \\ &=& (a_1^{(3)} - t_1^{(3)}) \times sigmoid(z_1^{(3)}) \times (1 - sigmoid(z_1^{(3)})) \times 1 \\ &\longrightarrow &= (a_1^{(3)} - t_1^{(3)}) \times a_1^{(3)} \times a_1^{(3)} \times (1 - a_1^{(3)}) \times 1 \\ \end{array}$$

## Self Study



$$\frac{\partial E}{\partial w_{12}^{(3)}} = (a_1^{(3)} - t_1^{(3)}) \times a_1^{(3)} \times (1 - a_1^{(3)}) \times a_2^{(2)}$$

$$\frac{\partial E}{\partial w_{21}^{(3)}} = (a_2^{(3)} - t_2^{(3)}) \times a_2^{(3)} \times (1 - a_2^{(3)}) \times a_1^{(2)}$$

$$\frac{\partial E}{\partial w_{22}^{(3)}} = (a_2^{(3)} - t_2^{(3)}) \times a_2^{(3)} \times (1 - a_2^{(3)}) \times a_2^{(2)}$$

$$\frac{\partial E}{\partial b_2^{(3)}} = (a_2^{(3)} - t_2^{(3)}) \times a_2^{(3)} \times (1 - a_2^{(3)}) \times 1$$