

# Diffusion Policy

Thursday, August 7, 2025 11:39 AM

## Diffusion Policy

### Core idea:

- Diffusion Policy applies diffusion models (forwarding generation) to generate robot trajectories & control policies
- Model learns to refine random noise into coherent action sequence by iteratively denoising

## Simple Example (1D)

### Step 1 - Setup State Space

$S \in \mathbb{R}^G$   
 $S = [0, 10]$   
Action space =  $[-5, +5]$  Continuous Action Space  
Trajectory =  $[a_i]$  Timesteps  
Goal: Generate trajectory  $0 \rightarrow 3$   
so 1 timestep  
Perfect Trajectory =  $[+3.0]$

Neural Net:

$$f(\text{noisy-trajectory}, \text{timestep}, \text{current-state}) \rightarrow \text{predicted-noise}$$
$$L = \|\hat{\epsilon} - \epsilon\|^2 \quad (\text{MSE})$$

### Training Phases:

#### Step 1: Collect goal train data

Sample 1	Sample 2	Sample 3
Initial State: 0.0	0.0	0.0
Goal: 3.0	3.0	3.0
Goal Trajectory: $[+3.0]$	$[+2.8]$	$[+3.3]$
Result: $0.0 + 3.0 = 3$	$0 + 2.8 = 2.8$	$0 + 3.3 = 3.3$

### Step 2: Forward Diffusion (Training adding noise)

#### Noise schedule

- timestep 0: No noise
- timestep 1:  $x_0 + N(0, \sigma=0.3)$  Add noise from normal distribution This makes it easier for the NN's to learn the noise
- timestep 2:  $x_1 + N(0, \sigma=0.7)$
- timestep 3:  $x_2 + N(0, \sigma=1.5)$

For  $[+3.0]$  NN training ( $[NT, T, CS]$ , true noise)  
 $t=0$  (clean)  $x_0 = [3.0]$   
 $x_1 = x_0 + N(0, \sigma^2)$   $([+3.2], 1, 0.0], [+0.2])$   
"When I see  $[+3.2]$  at  $t=1$  w/  $CS=0.0$ , the noise is  $[+0.2]$ "  
 $t=1$  (light noise)  
 $x_2 = x_1 + N(0, \sigma^2)$   $([+3.7], 2, 0.0], [+0.5])$   
"When I see  $[+3.7]$  at  $t=2$  w/  $CS=0.0$ , the noise is  $[+0.5]$ "  
 $t=2$  (medium)  
 $x_3 = x_2 + N(0, \sigma^2)$   $([+4.8], 3, 0.0], [+1.1])$   
"When I see  $[+4.8]$  at  $t=3$  w/  $CS=0.0$ , the noise is  $[+1.1]$ "

## Generation Phase

### Step 1 - Start w/ noise

CS - 0.0 (start position)

Goal: 3.0

Random starting trajectory:  $x_0 = [+5.1]$

Would result in  $0.0 + 5.1 = 5.1 > 3.0$  overshoot!

### Step 2 - Reverse Diffusion (Remove Noise iteratively)

$t = 3 \rightarrow 2$  (Remove heavy noise)

Noisy-trajectory:  $[+5.1]$

timestep: 3

current state: 0.0

$$f([+5.1], 3, 0.0) = [+1.1] \quad (\text{predicted noise})$$

$$x_2 = x_1 - \text{noise} = [+5.1] - [+1.1] = [+4.0]$$

$t = 2 \rightarrow 1$  (Remove medium noise)

$$f([+4.0], 2, 0.0) = [+0.5]$$

$$x_1 = x_2 - \text{noise} = [+4.0] - [+0.5] = [+3.5]$$

$t = 1 \rightarrow 0$

$$f([+3.5], 1, 0.0) = [+0.2]$$

$$x_0 = x_1 - \text{noise} = [+3.5] - [+0.2] = [+3.3]$$

Goal Check:  $|3.3 - 3.0| = .3$  very close!

## Execution Phase

generated trajectory =  $[+3.3]$

execute  $[+3.3]$

Answers:

state: 3.3

Goal: 3.0

Goal Achieved! (otherwise replan!)