

UNIT - I
CO2 - Partial differentiation

1. $f(x, y) = x^2 + xyz + z$ Find f_x at (1,1,1)
a) 0 b) 1 c) 3 d) -1

2. $f(x, y) = \sin(xy) + x^2 \ln(y)$ Find f_{yx} at $(0, \pi/2)$
a) 33 b) 0 c) 3 d) 1

3. $f(x, y) = x^2 + y^3$; $X = t^2 + t^3$; $y = t^3 + t^9$ Find df/dt at $t=1$.
a) 0 b) 1 c) -1 d) 164

4. $f(x, y) = \sin(x) + \cos(y) + xy^2$; $x = \cos(t)$; $y = \sin(t)$ Find df/dt at $t = \pi/2$
a) 2 b) -2 c) 1 d) 0

5. $f(x, y, z, t) = xy + zt + x^2 yzt$; $x = k^3$; $y = k^2$; $z = k$; $t = \sqrt{k}$
Find df/dt at $k = 1$
a) 34 b) 16 c) 32 d) 61

6. $f(x, y) = \sin(y + yx^2) / 1 + x^2$ Value of f_{xy} at (0,1) is
a) 0 b) 1 c) 67 d) 90

7. Necessary condition of euler's theorem is _____
a) z should be homogeneous and of order n
b) z should not be homogeneous but of order n
c) z should be implicit
d) z should be the function of x and y only

8. If $u = x^2 \tan^{-1}(y/x) - y^2 \tan^{-1}(x/y)$ then $\frac{\partial^2 u}{\partial x \partial y}$ is
a) $\frac{x^2+y^2}{x^2-y^2}$ b) $\frac{x^2-y^2}{x^2+y^2}$ c) $\frac{x^2}{x^2+y^2}$ d) $\frac{y^2}{x^2+y^2}$

9. If $f(x,y)$ is a function satisfying euler's theorem then?

- a) $x^2 \frac{\partial^2 f}{\partial x^2} + 2xy \frac{\partial^2 f}{\partial x \partial y} + y^2 \frac{\partial^2 f}{\partial y^2} = n(n-1)f$
b) $\frac{1}{x^2} \frac{\partial^2 f}{\partial x^2} + \frac{2}{xy} \frac{\partial^2 f}{\partial x \partial y} + \frac{1}{y^2} \frac{\partial^2 f}{\partial y^2} = n(n-1)f$
c) $x^2 \frac{\partial^2 f}{\partial x^2} + 2xy \frac{\partial^2 f}{\partial x \partial y} + y^2 \frac{\partial^2 f}{\partial y^2} = nf$
d) $y^2 \frac{\partial^2 f}{\partial x^2} + 2xy \frac{\partial^2 f}{\partial x \partial y} + x^2 \frac{\partial^2 f}{\partial y^2} = n(n-1)f$

10. In euler theorem $x \frac{\partial z}{\partial x} + y \frac{\partial z}{\partial y} = nz$, here 'n' indicates?
a) order of z b) degree of z c) neither order nor degree d) constant of z

11. For homogeneous function with no saddle points we must have the minimum value as

- a) 90 b) 1 c) equal to degree d) 0

12. $f(x, y) = \sin(y/x)x^3 + x^2y$ find the value of $f_x + f_y$ at $(x,y)=(4,4)$.

- a) 0 b) 78 c) $4^2 \cdot 3(\sin(1) + 1)$ d) -12

13. $f(x, y) = x^3 + xy^2 + 901$ satisfies the Euler's theorem.

- a) True b) False

14. If $z = x^n f(y/x)$ then?

- a) $y \frac{\partial z}{\partial x} + x \frac{\partial z}{\partial y} = nz$ b) $\frac{1}{y} \frac{\partial z}{\partial x} + \frac{1}{x} \frac{\partial z}{\partial y} = nz$
c) $x \frac{\partial z}{\partial x} + y \frac{\partial z}{\partial y} = nz$ d) $\frac{1}{x} \frac{\partial z}{\partial x} + \frac{1}{y} \frac{\partial z}{\partial y} = nz$

15. If $z = e^{\frac{x^2+y^2}{x+y}}$ then, $x \frac{\partial z}{\partial x} + y \frac{\partial z}{\partial y}$ is?

- a) 0 b) $z \ln(z)$ c) $z^2 \ln(z)$ d) z

16. Relative error in x is?

- a) δx b) $\delta x/x$ c) $\delta x/x \cdot 100$ d) 0

19. The Jacobian of p, q, r w.r.t x, y, z given $p = x + y + z, q = y + z, r = z$ is _____

- a) 0 b) 1 c) 2 d) -1

20. Given $u = \frac{yz}{x}, v = \frac{zx}{y}, w = \frac{xy}{z}$ then the value of $\frac{\partial(u,v,w)}{\partial(x,y,z)}$ is _____

- a) 4 b) -4 c) 0 d) 1

21. If $u = x + 3y^2 - z^3, v = 4x^2yz, w = 2z^2 - xy$ then $\frac{\partial(u,v,w)}{\partial(x,y,z)}$ at $(1,1,1)$.

- a) -184 b) -90 c) 20 d) 40

22. If $x = r \cos \theta, y = r \sin \theta$ then the value of $\frac{\partial(x,y)}{\partial(r,\theta)}$ is _____

- a) 1 b) 0 c) r d) $\frac{1}{r}$

23. If $u + v = e^x \cos y$ and $u - v = e^x \sin y$ the value of $J\left(\frac{u,v}{x,y}\right)$ is _____

- a) e^{2x} b) $\frac{e^{2x}}{2}$ c) $\frac{-e^{2x}}{2}$ d) 0

24. Which among the following is the definition of Jacobian of u and v w.r.t x and y ?

- a) $J\left(\frac{x,y}{u,v}\right)$ b) $J\left(\frac{u,v}{x,y}\right)$ c) $\frac{\partial(x,y)}{\partial(u,v)}$ d) $\frac{\partial(u,v)}{\partial(x,y)}$

25. Given $f(x,y) = e^x \cos y$, what is the value of the fifth term in Taylor's series near $(1, \frac{\pi}{4})$ where it is expanded in increasing order of degree & by following algebraic identity rule?

- a) $\frac{-e^{(x-1)}(y-\frac{\pi}{4})}{\sqrt{2}}$ b) $-\sqrt{2}e^{(x-1)}(y-\frac{\pi}{4})$
c) $\frac{e^{(x-1)^2}}{\sqrt{2}}$ d) $\frac{e^{(y-\frac{\pi}{4})^2}}{\sqrt{2}}$

26. Consider the $f(x, y) = x^2 + y^2 - a$. For what values of a do we have critical points for the function.

- a) independent of a b) for any real number except zero
c) $a \in (0, +\infty)$ d) $a \in (-1, 1)$

27. $f(x, y) = \sin(x) \cdot \cos(y)$ Which of the following is a critical point?

- a) $\left(\frac{\pi}{4}, \frac{\pi}{4}\right)$ b) $\left(-\frac{\pi}{4}, \frac{\pi}{4}\right)$ c) $\left(0, \frac{\pi}{4}\right)$ d) $(0, 0)$

28. The point $(0,0)$ in the domain of $f(x, y) = \sin(xy)$ is a point of _____

- a) Saddle b) Minima c) Maxima d) Constant

29. Maximize the function $x + y - z = 1$ with respect to the constraint $xy = 36$.

- a) 0 b) -8 c) 8 d) No Maxima exists

30. A partial differential equation requires

- a) exactly one independent variable b) more than one dependent variable
c) two or more independent variables d) equal number of dependent and independent variables

31. If $u = e^x(x \cos y - y \sin y)$, then $\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} = \dots$

- a) 0 b) u c) eu d) none

32. If $x = uv$, $y = u/v$ then $\frac{\partial(x,y)}{\partial(u,v)}$ is,

- a) $-2u/v$ b) $-2v/u$ c) 0 d) 1

33. If $J_1 = \frac{\partial(u,v)}{\partial(x,y)}$, $J_2 = \frac{\partial(x,y)}{\partial(u,v)}$ then $J_1 J_2$ is

- a) 2 b) 0 c) 1 d) none

34. If $u = x^y$, then $\frac{\partial u}{\partial x}$ is

- a) 0 b) $y x^{y-1}$ c) $x^y \log x$ d) none

35. If $u = x^y$, then $\frac{\partial u}{\partial y}$ is

- a) 0 b) $y x^{y-1}$ c) $x^y \log x$ d) none

36. If $u = x^3 + y^3$, then $\frac{\partial^2 u}{\partial x \partial y}$ is equal to

- a) -3 b) 3 c) 0 d) $3x + 3y$

37. If $u = x^2 + 2xy + y^2 + x + y$ then $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y}$ is equal to

- a) $2u$ b) u c) 0 d) none

38. If $u = \log \frac{x^2}{y}$ then $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y}$ is equal to

- a) $2u$ b) $3u$ c) u d) 1

39. If $A = f_{xx}(a, b)$, $B = f_{xy}(a, b)$, $C = f_{yy}(a, b)$ then $f(x, y)$ will have a maximum at (a, b) if

- a) $f_x = 0, f_y = 0, AC < B^2$ and $A < 0$ b) $f_x = 0, f_y = 0, AC = B^2$ and $A > 0$
c) $f_x = 0, f_y = 0, AC > B^2$ and $A > 0$ d) $f_x = 0, f_y = 0, AC > B^2$ and $A < 0$

40. If $z = \sin^{-1} \frac{\sqrt{x^2+y^2}}{x+y}$ then $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y}$ is equal to
a) 0 b) $1/2$ c) 1 d) 2
41. If $u = \sin^{-1}(x/y) + \tan^{-1}(y/x)$, then $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y}$ is equal to
a) u b) 2u c) 3u d) 0
42. If an error of 1% is made in measuring its length and breadth, the percentage error in the area of a rectangle is
a) 0.2% b) 0.02% c) 2% d) 1%
43. $\frac{\sqrt{x}-\sqrt{y}}{\sqrt{x}+\sqrt{y}}$ is a homogeneous function of degree.....
a) 1 b) 2 c) 0 d) $1/2$
44. If u and v are functions of r, s where r, s are functions of x, y then $\frac{\partial(u,v)}{\partial(r,s)} \cdot \frac{\partial(r,s)}{\partial(x,y)} = \dots$
a) $\frac{\partial(u,v)}{\partial(x,y)}$ b) $\frac{\partial(u,v)}{\partial(r,s)}$ c) $\frac{\partial(r,s)}{\partial(x,y)}$ d) none
45. The necessary conditions for a function $f(x, y)$ to have an extreme at (a, b) are.....
a) $f_x > 0, f_y > 0$ b) $f_x < 0, f_y > 0$ c) $f_x = 0, f_y = 0$ d) $f_x < 0, f_y < 0$
46. If $u = (x - y)^4 + (y - z)^4 + (z - x)^4$, then $\frac{\partial u}{\partial x} + \frac{\partial u}{\partial y} + \frac{\partial u}{\partial z}$ is
a) 1 b) u c) 4u d) 0
47. If $u = \cos^{-1}(x/y) + \tan^{-1}(y/x)$ then $x^2 u_{xx} + 2xy u_{xy} + y^2 u_{yy}$ is
a) u b) 2u c) 0 d) 1
48. If $u = f(x + ay) + g(x - ay)$ then $\frac{\partial^2 u}{\partial y^2}$ equals
a) $\frac{\partial^2 u}{\partial x^2}$ b) $a \frac{\partial^2 u}{\partial x^2}$ c) $a^2 \frac{\partial^2 u}{\partial x^2}$ d) $\frac{\partial^2 u}{\partial x \partial y}$
49. If $u = x^4 + y^4 + 3x^2 y^2$, then $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y}$ is
a) u b) 3u c) 4u d) 2u
50. If $u = f(y/x)$ then
a) $x \frac{\partial u}{\partial x} - y \frac{\partial u}{\partial y} = 0$ b) $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} = 0$
c) $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} = 2u$ d) $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} = 1$

Answers: 1)c 2)d 3.)d 4)b 5)b 6)a 7)a 8.)b 9)a 10)a 11)d 12)c 13)b 14)c 15)b 16)b 17)a 18)a 19)b 20)a 21)a 22)c 23)c 24)b 25)a 26)a 27)c 28)d 29)d 30) 31)a 32)b 33)c 34)b 35)c 36)c 37)d 38) 39)d 40)a 41)a 42)d 43)c 44)a 45)c 46)d 47)c 48)c 49.)c 50)b