

## Errata and Notes

Mistakes are marked with **red** and their fixes with **blue**.

## Introduction

1. End of page vi: “which shows the existence of sequences of Goppa codes **which** exceed the Gilbert-Varshamov bound.” should have been: “which shows the existence of sequences of Goppa codes **with parameters that** exceed the Gilbert-Varshamov bound.”

## 1 Error Correcting Codes

1. Middle of page 3: “This implies that **the**  $n - k$  rows of  $H$  are  $\mathbb{F}_q$ -linearly independent.” should have been: “This implies that **there exists**  $n - k$  rows of  $H$  **which** are  $\mathbb{F}_q$ -linearly independent.”
2. Middle of page 5 (in Example 1.21)  $P := \{P_1, P_2, \dots, P_n\}$  should have been:  
 $P := (P_1, P_2, \dots, P_n)$

## 2 Algebraic Geometry

### Algebraic Preliminaries

1. Middle of page 10 (in the proof of Theorem 2.8):  $F$  is both defined as a finite field and a polynomial (Polynomials were originally written using lower case letters.).

### Algebraic Geometry

1. Bottom of page 14 (Proposition 2.28 (iii) and the proof of Corollary 2.29): Should have noted that  $\mathcal{I}$  may be uncountable, and there is also a spare parenthesis (in 2.28).
2. Middle of page 16 (in the proof of Theorem 2.35): “Then multiplying both sides of Equation (2.1) by  $Y^n$  we see that:” should have been: “Then multiplying both sides of Equation (2.1) by  $Y^k$  we see that:”
3. Middle of page 19 (Proof of Proposition 2.43): “hence either  $F_1(P) = 0$  or  $F_2(P)$  for all  $P \in V$ .” should have been: “hence either  $F_1 \in I(V)$  or  $F_2 \in I(V)$  which is a contradiction.”
4. Middle of page 20: Needs an explanation as to why  $\mathbb{k}(\mathcal{X})$  and  $\mathbb{k}(\mathcal{X}^*)$  are isomorphic. However this follows as  $\mathbb{k}[\mathcal{X}]$  and  $\mathbb{k}[\mathcal{X}^*]$  are isomorphic.

### Algebraic Plane Curves

1. Third last paragraph, strictly speaking Proposition 2.8 only concerns finite fields with a prime number of elements.
2. Page 25 onwards: The extended valuation  $v_P$ , that is to the domain  $\overline{\mathbb{F}}_q(\mathcal{X})$  has codomain  $\mathbb{Z} \cup \{\pm\infty\}$  not  $\mathbb{Z} \cup \{\infty\}$ .

3. Bottom of Page 27, onwards: When we speak of a principal divisor  $(f)$ , i have sometimes assumed that  $f \in \overline{\mathbb{F}}_q[\mathcal{X}] \setminus \{0\}$ , this is of cause a mistake and should have been  $f \in \overline{\mathbb{F}}_q(\mathcal{X}) \setminus \{0\}$ .
4. Page 29 (proof of Lemma 2.87):  $f$  having no zeros or poles implies that  $f \in \overline{\mathbb{F}}_q^*$ , however the result still holds as we get  $L(D) = \overline{\mathbb{F}}_q^* \cup \{0\}$ .

### 3 Algebraic Geometry Codes

1. Second last paragraph of page 32: “The vector space  $L(D)$  will only consist of rational divisors...” should have been: “The vector space  $L(D)$  will only be considered when  $D$  is rational...”
2. From page 34, onwards: I seem to have forgotten to convert  $C_{D,G}$  to  $\mathcal{C}_{D,G}$  at some places.