

1)

a.

$$\forall x, \forall y, p(x, y)$$

b.

$$\forall x, \exists y, p(x, y)$$

c.

$$\forall x, \exists y, p(y, x)$$

d.

$$\forall y, \exists x, p(y, x)$$

e.

$$\exists(x, y, z), \neg p(x, (y, z)), \neg p(y, (x, z)), \neg p(z, (x, y))$$

f.

$$\forall x, \exists y, \neg p(x, y)$$

g.

$$\forall y, \exists x, \neg p(x, y)$$

h.

$$\forall y, \exists x, p(x, x) \wedge \neg p(y, x)$$

i.

$$\forall x, \exists(y), \neg(x = y) \wedge p(y, x)$$

j.

$$\exists x, \exists y, \exists z, (p(x, y) \wedge p(x, z) \rightarrow p(x, x))$$

k.

$$\forall z, \forall q, \exists x, \exists y, p(x, z) \wedge p(y, q) \wedge (\neg(z = q))$$

l.

$$\forall x, \forall y, (p(x, x) \wedge (\neg p(x, y))) \rightarrow (\neg p(y, x))$$

m.

$$\exists x, \exists y, \exists z, ((\neg(x = y)) \wedge (\neg(x = z)) \wedge (\neg(y = z))) \wedge (p(x, y) \wedge p(y, z) \wedge (\neg p(x, z)))$$

2)

a.

$$\forall x, \exists y, pred(y, x)$$

b.

$$\forall x, \exists y, pred(x, y)$$

c.

$$\forall x, \forall y, \exists z, pred(x, z) \wedge (\neg pred(x, y))$$

d.

$$\exists x, \forall y, \forall z, pred(x, y) \leftrightarrow (\neg pred(x, z))$$

e.

$$\forall x, \neg pred(x, x)$$

f.

$$\forall x, \forall y, pred((\neg even(x)), even(y))$$

g.

$$\forall x, \forall y, \exists z, (x < y) \leftrightarrow (pred(x, y) \vee (pred(z, y) \wedge (x < z)))$$