

$$P(A) = \frac{\int_a^d f(x) dx}{\int_c^d f(x) dx} = \int_c^d f(x) dx$$

$$\text{Note: } \int_a^b f(x) dx = 1$$

$$f(x) = 3x^2$$

$$[c, d] = \left(\frac{2}{3}, 1\right)$$

$$\int_{2/3}^1 3x^2 dx = (1)^3 - \left(\frac{2}{3}\right)^3 = .29$$


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$$E(x) = \int_a^b xf(x) dx$$

$$= \int_0^1 x(3x^2) dx = \int_0^1 3x^3 dx = \left(\frac{3}{4}\right)(x^4) \Big|_0^1 = 3/4$$


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$$f(x) = \frac{1}{2} \sin(x)$$

$$x = [0, \pi]$$

$$\int_0^\pi \frac{1}{2} (x) \sin(x) dx = \frac{1}{2} \int_0^\pi (x) \sin(x) dx$$

$$u = x, du = dx$$

$$dv = \sin(x) dx, v = -\cos(x)$$

$$= \frac{1}{2} [-\cos(x)] \Big|_0^\pi = \frac{1}{2} [-\cos(\pi) - (-\cos(0))] = \frac{1}{2} [1 + 1] = 1$$


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$$f(x) = x$$

$$x = [0, 1]$$

$$\int_0^n (x) 2x dx = \int_0^n 2x^2 dx = \frac{2x^3}{3} \Big|_0^n = \frac{2n^3}{3}$$