# Isotropic smoothing of image via Heat equation

### import library

```
import numpy as np
import matplotlib.image as img
import matplotlib.pyplot as plt
from matplotlib import cm
import matplotlib.colors as colors
from skimage import color
from skimage import io
```

### load input image

• filename for the input image is 'barbara\_color.jpeg'

### check the size of the input image

#### convert the color image into a grey image

```
number of rows of I = 512
number of columns of I = 512
```

#### normalize the converted image

• normalize the converted grey scale image so that its maximum value is 1 and its minimum value is 0

### define a function to compute the derivative of input matrix in x(row)-direction

• forward difference : I[x+1,y]-I[x,y]

```
In [ ]: compute_derivative_x_forward(I).shape
Out[ ]: (512, 512)
```

• backward difference : I[x, y] - I[x - 1, y]

### define a function to compute the derivative of input matrix in y(column)-direction

• forward difference : I[x, y+1] - I[x, y]

• backward difference : I[x,y] - I[x,y-1]

define a function to compute the laplacian of input

#### matrix

- $\Delta I = \nabla^2 I = \frac{\partial^2 I}{\partial x^2} + \frac{\partial^2 I}{\partial y^2}$
- $\Delta I = I[x+1,y] + I[x-1,y] + I[x,y+1] + I[x,y-1] 4 * I[x,y]$
- ullet  $\Delta I$  = derivative\_x\_forward derivative\_x\_backward + derivative\_y\_forward derivative\_y\_backward

## define a function to compute the heat equation of data $\boldsymbol{I}$ with a time step

•  $I = I + \delta t * \Delta I$ 

### run the heat equation over iterations

```
#
# +++++++
return l_update
```

### functions for presenting the results

```
In [ ]: | def function_result_01():
             plt.figure(figsize=(8,6))
             plt.imshow(I0)
             plt.show()
In [ ]: | def function_result_02():
             plt.figure(figsize=(8,6))
             plt.imshow(I, cmap='gray', vmin=0, vmax=1, interpolation='none')
             plt.show()
In [ ]: | def function_result_03():
             L = compute_laplace(I)
             plt.figure(figsize=(8,6))
             plt.imshow(L, cmap='gray')
             plt.show()
In [ ]: def function_result_04():
             time\_step = 0.25
             l_update = heat_equation(I, time_step)
             plt.figure(figsize=(8,6))
             plt.imshow(l_update, vmin=0, vmax=1, cmap='gray')
             plt.show()
In [ ]: | def function_result_05():
             time_step
                                = 0.25
             number_iteration = 128
             L_update = run_heat_equation(I, time_step, number_iteration)
             plt.figure(figsize=(8,6))
             plt.imshow(l_update, vmin=0, vmax=1, cmap='gray')
             plt.show()
In [ ]: def function_result_06():
             time_step
                               = 0.25
             number_iteration = 512
             I_update = run_heat_equation(I, time_step, number_iteration)
```

```
plt.figure(figsize=(8,6))
             plt.imshow(l_update, vmin=0, vmax=1, cmap='gray')
             plt.show()
In [ ]:
        def function_result_07():
             L = compute_laplace(I)
             value1 = L[0, 0]
             value2 = L[-1, -1]
             value3 = L[100, 100]
             value4 = L[200, 200]
             print('value1 = ', value1)
             print('value2 = ', value2)
             print('value3 = ', value3)
             print('value4 = ', value4)
In [ ]: | def function_result_08():
              time\_step = 0.25
              l_update = heat_equation(I, time_step)
             value1 = I_update[0, 0]
             value2 = I_update[-1, -1]
             value3 = I_update[100, 100]
             value4 = I_update[200, 200]
             print('value1 = ', value1)
             print('value2 = ', value2)
             print('value3 = ', value3)
print('value4 = ', value4)
In [ ]: | def function_result_09():
                                  = 0.25
              time_step
                                = 128
             number_iteration
              L_update = run_heat_equation(I, time_step, number_iteration)
             value1 = I_update[0, 0]
             value2 = I_update[-1, -1]
             value3 = I_update[100, 100]
             value4 = I_update[200, 200]
             print('value1 = ', value1)
             print('value2 = ', value2)
             print('value3 = ', value3)
print('value4 = ', value4)
In []: def function_result_10():
                                 = 0.25
              time_step
             number_iteration = 512
              I_update = run_heat_equation(I, time_step, number_iteration)
             value1 = I_update[0, 0]
             value2 = I_update[-1, -1]
             value3 = I_update[100, 100]
             value4 = I_update[200, 200]
```

```
print('value1 = ', value1)
print('value2 = ', value2)
print('value3 = ', value3)
print('value4 = ', value4)
```

### results







