## A Parameter Studies

We now report two additional parameter studies. They were done with the setting denoted "Ours", with one difference: original LBDs were still used instead of the Deactivated-LBDs setting. Each run consisted of 396 instances with 300 s timeout on 8 nodes (384 cores).

The first study explores clause database reduction. Kissat offers parameters reduce-low (default 500) and reduce-high (default 900), which control the aggressiveness of database reductions. The default parameters correspond to reductions by 50% early in the run and by up to 90% later in the run. We tested four parameter settings, described briefly.

Reduce setting	#	+	_	PAR2
Default	323	153	170	137.9
Point	323	154	169	139.2
Gaussian	321	151	170	140.8
Range	318	149	169	144.2

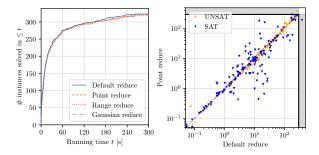


Figure 12 Effects of diversifying Kissat's reduce-low and reduce-high parameters.

**Default reduce**: Default reduce parameters. **Point reduce**: Value  $r \in [0, ..., 1000]$  is uniformly sampled per solver and both reduce-low and reduce-high are set to it. This creates some extreme solvers that keep all clauses forever (r=0) and others that delete every clause almost immediately (r=1000). **Range reduce**: A value  $r \in [-200, 1200]$  is uniformly sampled per thread; then we set reduce-low=max(0,r-200) and reduce-high=min(1000,r+200). Intuitively this slides the default interval [500,900] randomly to higher or lower values and leaves per solver the flexiblity of shifting from low to high reductions. **Gaussian reduce**: A value r is sampled from a Gaussian distribution with mean 700 and standard deviation 150, then r is clipped to be within [300,980] and both reduce-low and reduce-high are set to it. This sampling specifically avoids the extremes from the other two settings.

The results of the four reduce settings are shown in Fig. 12. Default reduce performs overall best, whereas Point reduce performs strongly on some SAT instances, which might be due to some aggressive solvers being allowed to eliminate almost all learned clauses.

The second study focuses on the decay of (E)VSIDS scores controlled by the decay parameter. Its default value is 50 (per mille), corresponding to an update of variables activity scores to 95% of their former value. Higher decay results in more aggressive updates.

Decay setting	#	+	_	PAR2
Uniform [1,50]	324	154	170	135.5
Default [50]	323	153	170	137.9
Uniform [1,200]	322	152	170	140.1
Uniform [50,200]	321	151	170	141.1

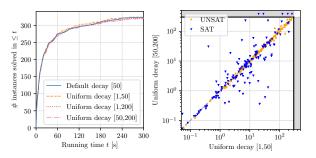


Figure 13 Effects of diversifying Kissat's decay parameter.

Kissat accepts values in the range of [1,...,200]. We explore this full range by testing

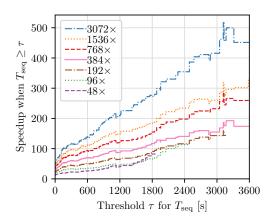
three settings: Uniform[1,50], Uniform[1,200] and Uniform[50,200]. In each setting every solver thread samples its decay value uniformly from the given interval. The third setting is thus much more eager than the default, while the first is more conservative.

The results of the different decay settings are shown in Fig. 13. Regarding PAR2 scores, the conservative updating with decay at or below 50 performs better than the more aggressive choices. However, similar to the database reductions, the more eager approaches perform better on some SAT instances, observable in the direct comparison plot.

## B Supplementary Data

Procedure	Kissat	<b>768</b> × <b>d</b>	768×s-o
backbone	0.12	0.18	_
congruence	0.46	1.85	_
eliminate	1.01	1.33	_
extend	0.00	0.00	_
factor	0.55		_
fastel	0.30	2.96	_
focused	43.39	44.65	49.97
lucky	0.08	1.34	1.59
parse	0.15	_	_
preprocess	0.83	4.77	_
$\operatorname{probe}$	11.15	13.52	_
reduce	1.37	2.68	3.24
search	86.32	79.15	95.41
$_{ m simplify}$	12.61	13.86	1.77
$\operatorname{stable}$	42.93	34.50	45.44
substitute	0.66	1.39	_
subsume	0.39	0.36	_
sweep	2.18	1.54	_
transitive	0.17	0.20	_
vivify	7.03	8.35	_
walking	0.96	0.65	1.77

Table 2 Percentages of total ("CPU") time spent in different procedures of Kissat's SAT solving, for sequential Kissat, 768-core default setup, and 768-core search-only setup. Note that some categories subsume each another (e.g., focused and stable are disjoint sub-categories of search).



**Figure 14** Weak Scaling of KCL configuration (as in Fig. 11).

Family	#	Avg. time	Speedup
miter-unsat	14	34.86	0.30
profitable-robust-production-sat	5	7.19	0.35
heule-nol-sat	7	18.50	0.43
social-golfer-sat	6	8.23	0.52
grs-fp-comm-unsat	8	75.60	0.62
scheduling-unsat	9	26.66	0.80
software-verification-unsat	10	56.29	0.97
cryptography-simon-sat	8	0.13	0.98
random-circuits-sat	5	24.89	1.01
hamiltonian-unsat	11	7.11	1.05
cryptography-ascon-unsat	6	8.58	1.05
argumentation-unsat	18	7.45	1.06
satcoin-unsat	5	16.36	1.28
brent-equations-sat	7	0.96	1.29
hamiltonian-sat	12	2.14	1.35
maxsat-optimum-sat	5	5.78	1.36
scheduling-sat	9	40.00	1.59
heule-folkman-sat	5	81.82	1.82
school-timetabling-sat	8	21.01	2.00
cryptography-sat	6	12.77	2.05
set-covering-sat	14	11.07	2.09
mutilated-chessboard-unsat	6	31.48	2.27

■ Table 3 Geom. mean speedup of "search-only" configuration over default Kissat-only configuration, at 768 cores, for each GBD benchmark family and result (SAT/UNSAT) group with data on  $\geq 5$  instances ("#"). "Avg. time" denotes the default configuration's according average running time.

Family	#	Avg. time	Speedup
set-covering-sat	6	0.21	0.04
heule-folkman-sat	6	5.82	0.08
register-allocation-unsat	11	0.12	0.10
random-circuits-sat	10	23.27	0.60
rbsat-sat	5	13.93	0.68
maxsat-optimum-unsat	5	19.11	0.70
hamiltonian-unsat	9	5.19	0.78
brent-equations-sat	9	0.63	0.81
argumentation-unsat	16	12.00	0.84
profitable-robust-production-sat	8	70.91	0.84
cryptography-ascon-unsat	10	8.12	0.88
quantum-kochen-specker-unsat	6	9.92	0.90
hamiltonian-sat	8	1.46	1.03
scheduling-unsat	6	28.64	1.04
scheduling-sat	17	24.12	1.08
satcoin-unsat	10	13.73	1.16
cryptography-sat	8	24.14	1.18
school-timetabling-sat	9	11.98	1.25
miter-sat	9	87.61	1.25
miter-unsat	23	29.96	1.26
coloring-unsat	5	24.48	1.26
software-verification-unsat	$\frac{5}{7}$	34.61	1.38
hashtable-safety-unsat		100.41	1.48
cryptography-ascon-sat	8	3.00	1.57
grs-fp-comm-unsat	6	65.93	1.63

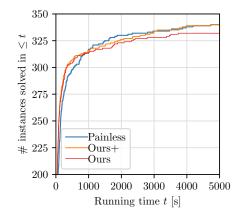
**Table 4** Geometric mean speedup of our new setup over KCL, at 3072 cores, split as in Table 3. "Avg. time" denotes the average running time of KCL on the respective instances.

cores	$ \frac{\mathbf{K}}{\# + - \text{PAR}  \mathbf{S}_q  \mathbf{S}_t} $	$ \begin{array}{c} \mathbf{KCL} \\ \# + - \mathrm{PAR}  \mathrm{S}_q  \mathrm{S}_t \end{array} $	$ \begin{array}{c} \mathbf{Ours} \\ \# + - \mathrm{PAR} \ \mathrm{S}_{q} \ \mathrm{S}_{t} \end{array} $
48	122 57 65 429.9 7.6 20.0	134 55 79 411.5 <b>12.8</b> 16.7	142 61 81 400.1 8.7 25.0
96	128 62 66 419.7 10.9 40.9	136 55 81 406.6 <b>16.7</b> 23.0	146 62 84 394.0 12.3 39.1
192	129 62 67 418.0 13.1 43.5	141 57 84 398.8 <b>20</b> .4 39.6	148 62 86 388.7 15.5 56.9
384	132 62 70 412.3 16.5 72.5	147 58 89 391.6 23.5 60.2	151 63 88 384.0 16.8 91.3
768	137 64 73 406.5 17.0 70.5	150 61 89 386.5 28.0 74.5	159 67 92 373.2 21.5 116.9
1536	142 66 76 398.8 18.1 80.5	151 60 91 384.4 30.8 81.5	157 65 92 374.5 23.4 120.6
3072	146 67 79 393.8 18.9 83.5	160 68 92 372.2 <b>33.2</b> 97.8	159 65 94 371.3 25.2 158.9

■ **Table 5** Performance as in Tab. 1, limited to the 209 randomly chosen instances from SAT Competition 2023.

cores		$ \begin{array}{c} \mathbf{KCL} \\ \# + - \mathrm{PAR}  \mathrm{S}_g  \mathrm{S}_t \end{array} $	$ \begin{array}{c} \mathbf{Ours} \\ \# + - \mathrm{PAR}  \mathrm{S}_g  \mathrm{S}_t \end{array} $
48	148 <b>75</b> 73 396.5 8.1 16.6	148 74 74 397.1 9.3 19.1	152 74 78 391.1 8.2 16.8
96	158 78 80 382.4 11.3 22.6	157 77 80 382.1 12.5 25.1	156 75 81 383.0 10.9 25.0
192	163 81 82 373.3 13.7 32.6	168 83 85 366.5 15.6 33.7	163 80 83 372.4 14.1 31.3
384	165 82 83 368.4 17.6 39.7	$168\ 82\ 86\ 363.5\ 20.1\ 42.5$	167 82 85 363.6 17.6 45.3
768	168 83 85 363.0 20.8 46.9	169 82 87 360.4 24.4 52.1	168 82 86 360.4 21.9 53.7
1536	<b>172</b> 85 87 357.0 24.1 55.8	172 84 88 354.6 29.6 64.4	172 84 88 352.9 25.8 76.8
3072	$172\ 85\ 87\ 354.7\ 28.0\ 67.6$	175 86 89 350.5 35.6 81.0	175 86 89 348.1 28.1 76.4

**Table 6** Performance as in Tab. 1, limited to the 191 randomly chosen instances from SAT Competition 2024.



	#	+	_	PAR2
Ours	332	148	184	1857.0
Ours+	340	154	186	1705.3
Painless	<b>340</b>	159	181	1721.4

Figure 15 Performance of our approach from the paper ("Ours"), an enhanced version ("Ours+") with added Lingeling-based preprocessing and each 20th thread running YalSAT, and state-of-the-art shared-memory solver PL-PRS-BVA-KISSAT, at a single node (48 cores) and for up to 5000 s of running time, as in the SAT Competition Parallel tracks. Note the y axis offset.