

# 1 Fancy Fence

You want to build a fence around the trees in your garden. There are  $n$  trees, each tree is planted at integer coordinates (see Fig. 1, left). The fence consists of horizontal and vertical segments of length 1 and diagonal segments of length  $\sqrt{2}$ , where each segment joins two integer points (see Fig. 1, right). The objective is to build such a fence of minimum perimeter that encloses all the trees. The fence is allowed to pass through the trees.

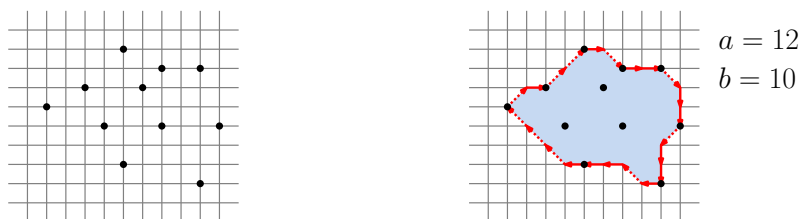


Figure 1: Fancy fence.

Letting  $a$  denote the number of horizontal and vertical fence segments, and letting  $b$  denote the number of diagonal segments, the total length of the fence is  $a + b\sqrt{2}$ . Write a program that inputs the tree coordinates and outputs the values  $a$  and  $b$ .

You may assume that  $1 \leq n \leq 10^5$  and each point's coordinates lie in the interval  $[-10^9, 10^9]$ .

Input and output files can be found at: <http://challengebox.cs.umd.edu/2019/Fence>

## Input:

The first line contains a single integer  $n$ , the number of trees in the garden. Each of the next  $n$  lines contains two space-separated integers  $x_i$  and  $y_i$ , indicating the coordinates of the  $i$ th tree.

## Output:

The output consists of the two numbers  $a$  and  $b$ , where  $a$  indicate the total number of horizontal-vertical segments.

## Example:

Given the input  $p_1 = (0,0)$ ,  $p_2 = (3,0)$ ,  $p_3 = (0,3)$  the minimum-perimeter fence consists of 3 horizontal segments from  $p_1$  to  $p_2$ , 3 diagonal segments from  $p_2$  and  $p_3$ , and 3 vertical segments from  $p_3$  to  $p_1$ , for a final answer of  $a = 6$  and  $b = 3$ .

Input:	Output:
3	6 3
0 0	
3 0	
0 3	