•
$$integral := int(int(int(rho, rho = 0..sqrt(a^2 - z^2)), z = c..b), theta = 0..2 \cdot Pi)$$

restart: with(LinearAlgebra):
integral := int(int(int(rho, rho = 0..sqrt(
$$a^2 - z^2$$
)), $z = c..b$), theta = 0..2·Pi)
integral := $a^2 (b - c) \pi - \frac{b^3 \pi}{3} + \frac{c^3 \pi}{3}$ (1)

simplify (integral)

$$\pi \left(a^2 \left(b - c \right) - \frac{b^3}{3} + \frac{c^3}{3} \right)$$
 (2)