

## ► Oefening 1

## ▼ Oefening 2

```
> restart:with(inttrans):with(plots):
  assume(t>0):assume(sigma>0):assume(d>0):
```

Initiële verdeling

```
> phi0 := x -> n0*exp(-x**2/sigma**2);
```

$$\phi_0 := x \mapsto n_0 \cdot e^{-\frac{x^2}{\sigma^2}} \quad (2.1)$$

```
> PHI0 := simplify(fourier(phi0(x), x, k));
```

$$PHI0 := n_0 e^{-\frac{k^2 \sigma^2}{4}} \sigma \sqrt{\pi} \quad (2.2)$$

```
> PHI := exp(-d*(k**2+K**2)*t)*PHI0;
```

$$PHI := e^{-d \sim (K^2 + k^2) t \sim} n_0 e^{-\frac{k^2 \sigma^2}{4}} \sigma \sqrt{\pi} \quad (2.3)$$

```
> simplify(invfourier(PHI, k, x));
```

$$\frac{\sigma \sim n_0 e^{\frac{-4 K^2 d \sim t \sim - K^2 d \sim \sigma^2 t \sim - x^2}{4 d \sim t \sim + \sigma^2}}}{\sqrt{4 d \sim t \sim + \sigma^2}} \quad (2.4)$$

Visualisatie

```
> phi := (x,t) -> simplify(invfourier(PHI, k, x));
```

$$\phi := (x, t) \mapsto \text{simplify}(\text{invfourier}(PHI, k, x)) \quad (2.5)$$

```
> subst := subs({sigma=2, d=2, K=1, n0=1});
```

$$\text{subst} := \{K = 1, d \sim = 2, n_0 = 1, \sigma \sim = 2\} \quad (2.6)$$

```
> animate(plot, [subs(subst, phi(x,t)), x=-10..10, thickness=5],
  t=0..3, frames=200);
```

