

> # Define the homogeneous equation  
 $LL := m \cdot \text{diff}(u(t), t^2) + \gamma \cdot \text{diff}(u(t), t) + k \cdot u(t);$

# Solve the homogeneous equation  
 $\text{hom\_sol} := \text{dsolve}(LL = 0, u(t)) \text{ assuming } \gamma^2 < 4 \cdot k \cdot m;$

$$LL := m \left( \frac{d^2}{dt^2} u(t) \right) + \gamma \left( \frac{d}{dt} u(t) \right) + k u(t)$$

$$\text{hom\_sol} := u(t) = c_1 e^{-\frac{\gamma t}{2m}} \sin\left(\frac{\sqrt{-\gamma^2 + 4km} t}{2m}\right) \quad (1)$$

$$+ c_2 e^{-\frac{\gamma t}{2m}} \cos\left(\frac{\sqrt{-\gamma^2 + 4km} t}{2m}\right)$$

>  $\text{part\_sol\_coeff} := \text{solve}(\{-m \cdot \alpha \cdot \omega^2 + \beta \cdot \omega \cdot \gamma + k \cdot \alpha = A,$   
 $-m \cdot \beta \cdot \omega^2 - \alpha \cdot \omega \cdot \gamma + k \cdot \beta = 0\},$   
 $\{\alpha, \beta\});$

$$\text{part\_sol\_coeff} := \left\{ \alpha = \frac{(-m \omega^2 + k) A}{m^2 \omega^4 + \gamma^2 \omega^2 - 2km \omega^2 + k^2}, \beta \right. \quad (2)$$

$$\left. = \frac{\gamma \omega A}{m^2 \omega^4 + \gamma^2 \omega^2 - 2km \omega^2 + k^2} \right\}$$

> # Dus de particuliere oplossing is dan:

>  $\text{particuliere\_oplossing} := \text{rhs}(\text{part\_sol\_coeff}[1] \cdot \sin(\omega \cdot t)$   
 $+ \text{part\_sol\_coeff}[2] \cdot \cos(\omega \cdot t))$

$$\text{particuliere\_oplossing} := \frac{\sin(\omega t) (-m \omega^2 + k) A}{m^2 \omega^4 + \gamma^2 \omega^2 - 2km \omega^2 + k^2} \quad (3)$$

$$+ \frac{\cos(\omega t) \gamma \omega A}{m^2 \omega^4 + \gamma^2 \omega^2 - 2km \omega^2 + k^2}$$

> # De algemene oplossing is dan

> # Solve the full equation  
 $\text{full\_sol} := \text{dsolve}(LL = A \cdot \sin(\omega \cdot t), u(t)) \text{ assuming } \gamma^2 < 4 \cdot k \cdot m;$

$$\text{full\_sol} := u(t) = e^{-\frac{\gamma t}{2m}} \sin\left(\frac{\sqrt{-\gamma^2 + 4km} t}{2m}\right) c_2 \quad (4)$$

$$+ e^{-\frac{\gamma t}{2m}} \cos\left(\frac{\sqrt{-\gamma^2 + 4km} t}{2m}\right) c_1 + \frac{A ((-m \omega^2 + k) \sin(\omega t) - \cos(\omega t) \gamma \omega)}{m^2 \omega^4 + (\gamma^2 - 2km) \omega^2 + k^2}$$