- with(VectorCalculus): with(LinearAlgebra):
- $J := Jacobian([a \cdot r \cdot \sin(\text{theta}) \cdot \cos(\text{phi}), b \cdot r \cdot \sin(\text{theta}) \cdot \sin(\text{phi}), c \cdot r \cdot \cos(\text{theta})], [r, \text{theta}, \text{phi}])$

$$J \coloneqq \begin{bmatrix} a \sin(\theta) \cos(\phi) & a r \cos(\theta) \cos(\phi) & -a r \sin(\theta) \sin(\phi) \\ b \sin(\theta) \sin(\phi) & b r \cos(\theta) \sin(\phi) & b r \sin(\theta) \cos(\phi) \\ c \cos(\theta) & -c r \sin(\theta) & 0 \end{bmatrix}$$
 (1)

 \rightarrow J := Determinant(J)

$$J := a \sin(\theta)^3 \cos(\phi)^2 b r^2 c + b \sin(\theta)^3 \sin(\phi)^2 a r^2 c$$

$$+ \sin(\theta) \cos(\phi)^2 \cos(\theta)^2 a b c r^2 + \sin(\theta) \sin(\phi)^2 \cos(\theta)^2 a b c r^2$$
(2)

 \rightarrow result := simplify(J)

$$result := a b c r^2 \sin(\theta)$$
 (3)

- _> # Dit is de jacobiaan bitches
- > # In een sferische situatie is r: 0..1, phi:0..2pi, theta:0..pi
- > $output := int(int(int(result, r = 0..1), theta = 0..Pi), phi = 0..2 \cdot Pi)$

$$output := \frac{4 a b c \pi}{3}$$
 (4)

> simplify(output)

$$\frac{4 a b c \pi}{3} \tag{5}$$