

2)

To look identical:

$$\frac{f}{g_n} = \frac{f'}{g_n} + h \quad \Leftrightarrow \quad f' = f + h g_n$$

$$f < \frac{f_n}{2}, \text{ so } 0 < f \leq \frac{f_n}{2}, \quad \text{so you want } f' \text{ to be in } \frac{f_n}{2} \leq f' \leq f_n$$

this happens when $h = 1$

$$\Rightarrow f' = f_n - f.$$