

$$2) \langle f, g \rangle = \int_{-\infty}^{+\infty} f(t) \cdot g(t) dt$$

$$f(t) = t \cdot e^{-t/2}$$

$$i) f_0(t) = \frac{f(t)}{\text{Norm}(f_0)}$$

$$f_1(t) = \frac{f(t) - (f, f_0) \cdot f_0}{\text{Norm}}$$

$$ii) f(t) = e^{-t/2} \cos(2t)$$

$$\rightarrow \text{proj}_{\mathcal{H}} f = (f_0, f) f_0 + (f_1, f) f_1 + (f_2, f) f_2 + (f_3, f) f_3 + (f_4, f) f_4$$