

$$1) f(t) = 1^2, t \in]-L, L[$$

$$p = 4$$

$$L \mapsto L^1$$

$$F(t) = \frac{a_0}{L} + \sum_{n=1}^{\infty} a_n \cdot \cos\left(\frac{n\pi \cdot t}{L}\right) + b_n \cdot \sin\left(\frac{n\pi \cdot t}{L}\right)$$

$$a_0 = \frac{2}{L} \cdot \int_{-L}^L f(t) \cdot dt = \frac{2}{L} \cdot \int_{-L}^L 1^2 \cdot dt = \frac{8}{3}$$

function is even

$$\int_{-L}^L 1^2 \cdot \cos\left(\frac{n\pi t}{L}\right) \cdot dt = \int_0^L 1^2 \cdot \cos\left(\frac{n\pi t}{L}\right) \cdot dt$$

function is odd, but $f(t) = 1^2$ is even, thus $b_n = 0$.

$$a_n = \frac{2}{L} \cdot \int_{-L}^L f(t) \cdot \cos\left(\frac{n\pi t}{L}\right) dt = \frac{1}{L} \cdot \int_{-L}^L 1^2 \cdot \cos\left(\frac{n\pi t}{L}\right) dt$$

$$b_n = \frac{2}{L} \cdot \int_{-L}^L f(t) \cdot \sin\left(\frac{n\pi t}{L}\right) dt = 0$$