$$v_{1} := \begin{bmatrix} 2I \\ -1 \\ 0 \\ 0 \end{bmatrix}$$
 (1)

 $v_2 := Vector([I, 0, 3, 1])$

$$\mathbf{v}_{2} \coloneqq \begin{bmatrix} \mathbf{I} \\ \mathbf{0} \\ \mathbf{3} \\ \mathbf{1} \end{bmatrix} \tag{2}$$

 $u_1 := \frac{v_1}{Norm(v_1, 2)}$

$$u_{-}1 := \begin{bmatrix} \frac{2I}{5}\sqrt{5} \\ -\frac{\sqrt{5}}{5} \\ 0 \\ 0 \end{bmatrix}$$
 (3)

> $u_2 := \frac{(v_2 - (u_1 \cdot v_2) \cdot u_1)}{Norm(v_2 - (u_1 \cdot v_2) \cdot u_1, 2)}$

$$u_{2} := \begin{bmatrix} \frac{I}{255} \sqrt{255} \\ \frac{2\sqrt{255}}{255} \\ \frac{\sqrt{255}}{17} \\ \frac{\sqrt{255}}{51} \end{bmatrix}$$
(4)

> w := Vector([3, 1 - I, 2 + I, 1])

(5)

$$w := \begin{bmatrix} 3 \\ 1 - I \\ 2 + I \\ 1 \end{bmatrix}$$
 (5)

> $proj := (u_1 \cdot w) \cdot u_1 + (u_2 \cdot w) \cdot u_2$

$$proj := \begin{bmatrix} 2 - \frac{2I}{5} + \frac{I\left(\left(\frac{32}{255} + \frac{2I}{51}\right)\sqrt{255} + \frac{\sqrt{255}}{51}\right)\sqrt{255}}{255} \\ \frac{1}{5} + I + \frac{2\left(\left(\frac{32}{255} + \frac{2I}{51}\right)\sqrt{255} + \frac{\sqrt{255}}{51}\right)\sqrt{255}}{255} \\ \frac{\left(\left(\frac{32}{255} + \frac{2I}{51}\right)\sqrt{255} + \frac{\sqrt{255}}{51}\right)\sqrt{255}}{17} \\ \frac{\left(\left(\frac{32}{255} + \frac{2I}{51}\right)\sqrt{255} + \frac{\sqrt{255}}{51}\right)\sqrt{255}}{51} \end{bmatrix}$$

 \gt simplified := simplify(proj)

$$simplified := \begin{bmatrix} \frac{100}{51} - \frac{13 \, \mathrm{I}}{51} \\ \frac{25}{51} + \frac{55 \, \mathrm{I}}{51} \\ \frac{37}{17} + \frac{10 \, \mathrm{I}}{17} \\ \frac{37}{51} + \frac{10 \, \mathrm{I}}{51} \end{bmatrix}$$

$$(7)$$