

$$\begin{cases} y''(t) + 4y'(t) + 4y(t) = 0 & (1) \\ y(0^+) = 1 \\ y'(0^+) = 1 \end{cases}$$

we define:

$$\begin{cases} L(y'') = n^2 \gamma(n) - n \gamma(0) - \gamma'(0^+) \\ L(y') = n \gamma(n) - \gamma(0) \\ L(y) = \gamma(n) \end{cases}$$

$$(1) \quad n^2 \gamma(n) - n \gamma(0) - \gamma'(0) + 4(n \gamma(n) - \gamma(0)) + 4 \gamma(n) = 0$$

$$\Leftrightarrow n^2 \gamma(n) - n - n + 4n \gamma(n) - 4 + 4 \gamma(n) = 0$$

$$\Leftrightarrow n^2 \gamma(n) + 4n \gamma(n) + 4 \gamma(n) - (n+5) = 0$$

$$\Leftrightarrow \frac{n+5}{n^2 + 4n + 4} = \gamma(n) \stackrel{\text{Laplace}}{=} \underbrace{(3t+1)}_{\text{heaviside function}} e^{-2t} \cdot \theta(t)$$