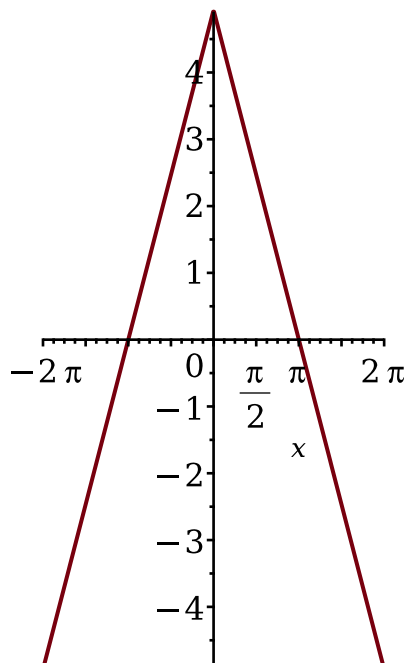


> restart:

> $f := x \mapsto \frac{\pi^2}{2} \cdot \left(1 - \frac{\text{abs}(x)}{\text{Pi}}\right) :$

> plot(f(x), x = -2·Pi..2·Pi)



> $a := n \mapsto \frac{1}{2 \cdot \text{Pi}} \cdot \text{int}\left(f(x) \cdot \cos\left(\frac{n \cdot x}{2}\right), x = -2 \cdot \text{Pi}..2 \cdot \text{Pi}\right)$

$$a := n \mapsto \frac{\int_{-2 \cdot \pi}^{2 \cdot \pi} f(x) \cdot \cos\left(\frac{n \cdot x}{2}\right) dx}{2 \cdot \pi} \quad (1)$$

> a(0)

$$0 \quad (2)$$

> a(1)

$$4 \quad (3)$$

> a(2)

$$0 \quad (4)$$

> a(3)

$$\frac{4}{9} \quad (5)$$

> odd_a := simplify(a(2·n + 1) assuming (n, posint))

$$\text{odd_a} := \frac{4}{(2n + 1)^2} \quad (6)$$

> f_approx := evalf(add(odd_a · cos($\frac{n \cdot x}{2}$), n = 0..1000)) :

> simplify(subs(x = 0, f_approx))

$\left[\begin{array}{l} \text{=} \\ \text{>} \end{array} \right]$	$evalf\left(\frac{\pi^2}{2}\right)$	4.933803198	(7)
		4.934802202	(8)