

Chapter 5 Homework

Due 2-4-2018

Problem 5.28

a) Is there substantial evidence ($\alpha = 0.01$) that the additive reduces the mean absorption from its current value?

Hypothesis

$$\begin{aligned} H_0 : \mu &= 35 \\ H_a : \mu &< 35 \end{aligned}$$

Test Statistic

With an $n = 50$, we can assume a z test statistic will be appropriate. $z_0 = \frac{\bar{y} - \mu_0}{\sigma / \sqrt{n}} = \frac{33.6 - 35}{9.2 / \sqrt{40}} = -1.076$

Rejection Region

Reject if $z_0 \leq z_{\alpha}$; $z_{0.01} = -2.575$

P-Value

With a confidence level of 99% to compare to, my P-value ends up being 0.141.

Conclusion / Interpretation

We fail to reject the null hypothesis. There is not sufficient evidence to suggest that the number of improperly issued tickets is less than 35.

b) What is the level of significance(p-value) of your test results?

The level of significance(p-value) is 0.141.

d) Estimate the mean absorption using a 99% confidence interval. Is the confidence interval consistent with your conclusions from the hypothesis test?

Confidence Interval

$$C.I. = \bar{y} \pm z_{1-\frac{\alpha}{2}} \left(\frac{\sigma}{\sqrt{n}} \right) \quad (1)$$

Where our $s = 9.2$,

Conclusion

Since my $\mu = 35$ sits between the two values of my confidence interval, this fits my Conclusion to my hypothesis test that we don't have significant enough data to reject the Null Hypothesis.

Problem 41

a) **Place a 95% confidence on the mean dissolved oxygen level during the 2-month period.**

Confidence Interval

Since my sample size is small ($n = 8$) and I don't have σ , I'll leverage a confidence interval based on Student's t Distribution.

Equation

$$C.I. = \bar{y} \pm t_{1-\frac{\alpha}{2}} \left(\frac{s}{\sqrt{n}} \right) \quad (2)$$

$$\bar{y} = 4.95, s = 0.45, n = 8, t_{1-\frac{\alpha}{2}} = 2.365$$

$$C.I. = 4.95 \pm 2.365 \left(\frac{0.45}{\sqrt{8}} \right) \quad (3)$$

$$C.I. \approx (4.5737, 5.3263) \quad (4)$$

b) **Using the confidence interval from part (a), does the mean oxygen level appear to be less than 5 ppm?**

Conclusion

With the left tail of the Confidence Interval being less than 5 ppm, it does appear that the population mean(μ) could be less than 5 ppm.

c) **Test the research hypothesis that the mean oxygen level is less than 5 ppm. What is the level of significance of your test? Interpret your findings.**

Hypothesis

$$H_0 : \mu = 5$$

$$H_A : \mu < 5$$

Test Statistic

Since we used a Confidence Interval based on the t distribution, we will use the same distribution just as a 95% Hypothesis Test since it wasn't stated in the problem.

$$t = \frac{\bar{y} - \mu_0}{s/\sqrt{n}} \quad (5)$$

$$t = \frac{4.95 - 5}{0.45/\sqrt{8}} \quad (6)$$

$$t = -0.314 \quad (7)$$

Rejection Region

Since this is a one-sided t-test, we will check what the rejection region is for a t distribution with 7 degrees of freedom and an α of 0.05.

The rejection region for the Null Hypothesis would be any t-score ≤ -1.895 .

P-value

Additionally, the p-value of such a $t = -0.314$

Conclusion / Interpretation