

Exploration of Structures of Two-Dimensional Boron–Silicon Compounds with sp^2 Silicon

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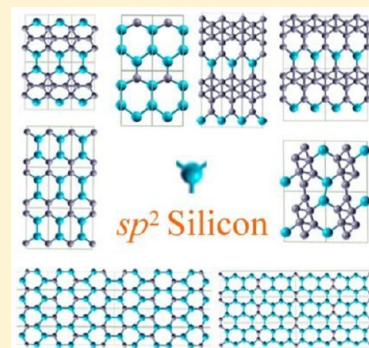
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S Supporting Information

ABSTRACT: The most stable structures of two-dimensional (2D) boron–silicon (B–Si) compounds containing planar sp^2 -bonding silicon (sp^2 -Si) are explored using the first-principles calculation-based particle-swarm optimization method. Among 10 B–Si compounds considered, we find that for BSi_4 , BSi_3 , BSi , B_2Si , B_3Si , B_5Si , and B_6Si , each Si atom is bonded with three B or Si atoms within the same plane, representing a preference of planar sp^2 -Si structure in B–Si compounds. For BSi_2 and B_4Si , the predicted lowest-energy structures entail a small out-of-plane buckling. Furthermore, a planar-tetracoordinated Si (ptSi) atom bonded with four B atoms within the same plane is observed in the lowest-energy structure of B_7Si compound. Dynamical stabilities of the predicted 10 2D B–Si compounds are confirmed via phonon-spectrum calculation. The lowest-energy 2D B–Si compounds are all metals, regardless of the B–Si stoichiometry considered in this study.

SECTION: Molecular Structure, Quantum Chemistry, and General Theory



Since the first isolation of two-dimensional (2D) graphene in 2004,^{1–4} an era of exploring novel 2D nanomaterials has arisen. Although graphene is currently at the center stage of 2D materials research owing to its fascinating properties, such as massless Dirac Fermion and quantum Hall effect, research efforts toward other 2D materials in general and monolayer materials with single-atom-thickness in particular have increased considerably. For example, free-standing 2D boron-nitride (BN) monolayers have been successfully fabricated through a layer-by-layer sputtering process.⁵ Monolayer MoS_2 sheets have also been isolated using micromechanical cleavage technique.⁶ Coleman et al. reported a liquid exfoliation technique that can efficiently produce monolayer sheets of various of inorganic layered materials such as BN, MoS_2 , WS_2 , $MoSe_2$, $MoTe_2$, $TaSe_2$, $NbSe_2$ and $NiTe_2$.⁷ By adopting a modified liquid exfoliation method, Xie et al. successfully synthesized monolayer VS_2 ,^{8,9} and SnS_2 ,¹⁰ as well as monolayer structures of nonlayered ZnSe and ZnS materials.¹¹

Silicon and boron are two nearest-neighbors of carbon in the periodic table, and both are believed to possess 2D monolayer structure (e.g., silicene).^{12–22} Silicene has attracted increasing attention recently because of the existence of Dirac fermion¹⁴ and its compatibility with silicon-based nanotechnology. A silicon atom has a larger ionic radius than carbon, which tends to promote sp^3 hybridization. As a result, free-standing monolayer silicene prefers a low-buckled structure,^{14,15,23} although bilayer hexagonal silicon can be a metastable planar

structure when formed within a slit nanopore as suggested from a previous classical molecular dynamics simulation.²⁴ Although silicene may not be isolated by using the exfoliation method as for the graphene, silicene nanoribbons fabricated by deposition of silicon atoms on a Ag(110) surface have been reported in the literature.^{25–28} Very recently, epitaxial growth of silicene sheets on Ag(111)^{29–31} and $NbB_2(0001)$ ³² substrate has also been realized in the laboratory. It was found that the silicene sheet on Ag(111) surface has similar electronic properties as the graphene, such as the electronic dispersion resemblance to relativistic Dirac fermions,³¹ and that on $NbB_2(0001)$ surface, a direct π -electronic band gap is detected.³² Recently, many low-energy forms of 2D monolayer boron have been predicted,^{16–21} namely, α -sheet, $g_{1/8}$ and $g_{2/15}$ sheets, and α_1 , α_2 , β_1 , and β_2 -sheets, whose cohesive energies are nearly degenerate with each other (though predicted relativities are functional dependent). These 2D boron sheets can be viewed as selective removal of boron atoms from a closed-packed triangular boron sheet. Most of these monolayer sheets are predicted to be flat and metallic, except for the α -sheet, which is a nonplanar buckled structure with a modest band gap (semiconducting).²¹ Besides elemental boron and silicon, monolayer structures of boron–carbon

Received: December 4, 2012

Accepted: January 28, 2013

Published: January 31, 2013

compounds,^{33,34} Si₂C,³⁵ nitrogen-graphene alloys,³⁶ ZnO,³⁷ and group III–V compounds^{38,39} have also been predicted.

Because boron is one of the most important p-type dopants used in silicon industry, boron–silicon compounds have attracted considerable attention. The existence of silicon–boron compounds was reported more than a century ago. Moissan and Stock discovered SiB₃ and SiB₆ through fusion of the elements.⁴¹ A more well-known silicon boride is SiB₄, which was first reported in 1960.⁴² The crystalline structures of silicon borides are closely related to the boron icosahedra structure. For example, SiB₃ is based on 12-atom, boron rich icosahedra in which some boron atoms are substituted by silicon atoms. SiB₄ is isomorphic to B₄C, and it is composed of Si–B–Si chains and B₁₂ icosahedra. Additionally, the crystal structure of SiB₆ contains icosahedra, icosihexahedra, as well as isolated silicon and boron atoms. These B–Si compounds are also known for their mechanical hardness. More recently, theoretical calculations have been performed to investigate properties of boron-doped silicon nanocrystal⁴² and cubic silicon.⁴³

Since both boron and silicon can possess 2D monolayer structure, boron-doped silicene or silicon-doped boron sheets are likely to exist. Very recently, Hansson et al. reported a 2D BN-like hexagonal SiB crystal (*h*-SiB).⁴⁴ To determine whether this structure is the ground-state or not requires a global search of all the low-energy structures of 2D BSi. Another question is whether the boron–silicon compounds can possess a planar monolayer structure at certain stoichiometry. To address this question, we adopt a global optimization method based on the particle-swarm optimization (PSO) techniques⁴⁵ to predict 2D structures of silicon–boron compounds with a wide distribution of B composition. The lowest-energy monolayer structures of BSi₄, BSi₃, BSi₂, BSi, B₂Si, B₃Si, B₄Si, B₅Si, B₆Si, and B₇Si are predicted, and the B–Si compounds with higher boron composition are energetically more preferable due to higher cohesive energies. Moreover, our density functional theory (DFT) calculations suggest that all these monolayer boron–silicon compounds are metallic. Interestingly, in the predicted monolayer structures of BSi₄, BSi₃, BSi, BSi₂, BSi₃, BSi₅ and BSi₆, each Si atom is bonded with three B or Si atoms within the same plane, representing a preference of the planar sp²-bonding for Si in 2D B–Si compounds. On the other hand, BSi₂ and B₄Si monolayers exhibit a small out-of-plane buckling.

Geometrical Properties. 2D B–Si compounds with 10 different B–Si stoichiometric compositions are considered, namely, BSi₄, BSi₃, BSi₂, BSi, B₂Si, B₃Si, B₄Si, B₅Si, B₆Si, and B₇Si. The predicted lowest-energy structures are shown in Figure 1, and other low-energy structures (for BSi₃ and B₃Si, only one stable structure is found) are illustrated in the Supporting Information (Figures S1–S8). Here, we use I, II, and III to label the energy ranking of the low-energy structures (for example, BSi₄-I denotes the lowest-energy structure, and BSi₄-II is the second low-lying structure). Note that the lowest-energy structure possesses the greatest cohesive energy.

For silicon-rich compounds, i.e., BSi₄, BSi₃ and BSi₂, their structures can be viewed as boron-doped graphene-like silicon monolayers. The lowest-energy BSi₄ (BSi₄-I) exhibits a planar graphene-like structure that is composed of parallel armchair-type silicon nanoribbons separated by boron-dimer chains, as shown in Figure 1a. Although the free-standing silicene is known to exhibit a weakly buckled structure, it is interesting that the silicon nanoribbons in BSi₄-I can be stabilized within the same plane through connecting with boron dimer chains. Here we do not use the term silicene ribbon because it may

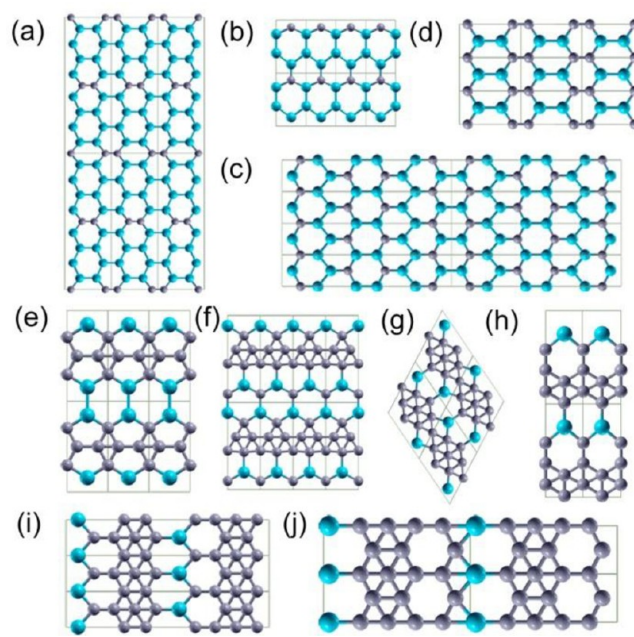


Figure 1. Predicted lowest-energy monolayer structures of (a) BSi₄-I, (b) BSi₃-I, (c) BSi₂-I, (d) BSi-I, (e) B₂Si-I, (f) B₃Si-I, (g) B₄Si-I, (h) B₅Si-I, (i) B₆Si-I, and (j) B₇Si-I from the PSO structural search. Si and B atoms are denoted by cyan and gray spheres.

give a false impression that the nanoribbons assume the nonplanar buckled structure.

In BSi₄-II structure, silicon atoms form square rings, and each boron atom is bonded with four silicon square rings at their corner, i.e., silicon and boron atoms are packed into a mosaic of square silicon rings and hexagonal B₂Si₄ rings (see Figure S1). Different from BSi₄-I, the structure of BSi₄-II is weakly buckled with an out-of-plane distance of 0.75 Å. The BSi₄-III monolayer is strictly planar, and the silicon and boron atoms are packed into a mosaic of silicon rhombus rings and hexagonal B₂Si₄ rings with two neighboring rhombus rings sharing a planar-tetracoordinated silicon (ptSi) atom, akin to the planar-tetracoordinated carbon (ptC).⁴⁶ Hence, 25% silicon atoms are bonded with four silicon atoms, forming the planar-tetracoordinated structure similar to that of the previously reported 2D boron-carbide sheet and SiC₂ sheet.^{33–35} Note that the existence of ptSi atoms with Si–Si bonds has not been reported in the literature. Our DFT calculation indicates that BSi₄-I is energetically more favorable than BSi₄-II and BSi₄-III by 95.0 meV/atom and 103.2 meV/atom, respectively. The large differences in the cohesive energy might be due to the presence of the silicon squares and rhombus in BSi₄-II and BSi₄-III, respectively.

For BSi₃ (Figure 1b), only one stable monolayer structure is obtained based on the PSO global search. This planar structure can be viewed as an alternate arrangement of zigzag single-silicon chains and silicon–boron chains. In BSi₂-I and BSi₂-II (Figure 1c and Figure S2), the zigzag single-silicon chains are separated by B–Si nanoribbon-composed B₃Si₃ six-membered rings. However, the BSi₂-I is slightly buckled with an out-of-plane distance of about 0.29 Å. The structural difference between BSi₂-I and BSi₂-II is the atomic arrangement of boron and silicon in the six-membered rings. BSi₂-I is energetically more stable than BSi₂-II by 21.1 meV/atom.

When the mole fraction of boron and silicon is the same (BSi), the compound has two competing monolayer structures.

The 2D h -SiB⁴⁴ predicted by Hanson et al. is identical to BSi-II, which possesses a slightly smaller cohesive energy (about 5 meV/atom) than that of BSi-I. Both BSi-I and BSi-II exhibit strictly planar honeycomb structure like graphene. The structure of BSi-I (Figure 1d) is composed of uniformly distributed boron-dimer and silicon-dimer, while in BSi-II, the boron and silicon atoms are distributed alternately in the honeycomb lattice (Figure S3). Their relative stability suggests that in the BSi sheet, B–B and Si–Si bonds are energetically favorable. Since only BSi-I has Si–Si and B–B bonding, it will result in a distinct vibration signal that may be used to differentiate itself from other B–Si compounds once synthesized.

For B-rich systems, boron atoms present multibonding structural characteristics and form ribbon or cluster structures. For B₂Si, the structure of B₂Si-I has an alternate arrangement of one-dimensional (1D) linear boron-atom chains and B₂Si₄ hexagonal-ring chains. Moreover, the neighboring four boron atoms form B₄ rhombus, as shown in Figure 1(e). The B₂Si-II has a similar structure as that of B₂C, but with different arrangement of silicon and boron atoms.³³ For B₂Si-III, the structure is similar to that of B₂Si-I, which has an alternate arrangement of B₃Si₃ hexagonal-ring chains and atomic boron chains (see Figure S4). B₂Si-I is energetically more favorable than B₂Si-II and B₂Si-III by 59.8 meV/atom and 75.1 meV/atom, respectively. The existence of Si–Si π bonding in B₂Si-I (with a Si–Si bond length of 2.30 Å) may help stabilization of the structure. In B₂Si-III, silicon exhibits two bonding characteristics, a planar sp² bonding and an inequivalent planar-tetracoordinated bonding.

For B₃Si, only one stable monolayer structure is found from the PSO global search. The structure of B₃Si sheet has an alternate arrangement of narrow boron ribbons and B₃Si₃ hexagonal-ring chains (Figure 1f). The planar structure contains B₃Si₃ six-membered rings, B₄Si five-membered rings, B₄Si₂ six-membered rings, and boron triangles. The Si atoms are isolated in the structure, and thus only B–Si and B–B bonds exist in the sheet.

From B₄Si to B₇Si, their monolayer sheets have one common structural feature, that is, all structures can be viewed as parallel boron ribbons connected by silicon atoms or silicon–boron dimers (Figure 1g–j, and Figures S5–S8). In B₄Si-I (Figure 1g), boron atoms form 1D prismatic B₉ chains and the parallel B₉ chains are covalently connected via sparse Si–B bonds. The structure of B₄Si-III is composed of two zigzag double-B-atomic chains and one single-Si-atomic chain in the unit cell. An exception is the metastable B₄Si-II, which contains B₃Si₂ five membered rings, B₅Si six-membered rings, B₆Si seven-membered rings, and boron triangles. The B₃Si₂ rings in the sheet form 1D infinite chain. B₄Si-I is energetically more favorable than B₄Si-II and B₄Si-III by 16.8 and 24 meV/atom, respectively. Additionally, B₄Si-I is slightly buckled (the largest out-of-plane distance is 0.54 Å), while B₄Si-II and B₄Si-III are dynamically stable in the planar form.

The energy difference between the two predicted low-energy structures of B₅Si is less than 1 meV/atom, indicating polymorphic nature of B₅Si sheet. The structure of B₅Si-I has an alternate arrangement of zigzag BSi atomic chain and double-B-atomic chains (Figure 1h). B₅Si-II has a similar structure as B₂Si-II with less silicon composition, which is composed of 1D prismatic B₄ and B₃Si chains (Figure S6). Si atoms in B₅Si-II sheet are planar tetracoordinated.

For B₆Si, the lowest-energy structure (B₆Si-I) can be viewed as a stacking of BSi zigzag chains and edge-sharing B₇ hexagon (B₆ hexagon with an extra B at center) chains. Connected with edge boron atoms in the B₇ chain, B and Si atoms in the BSi chain form B₅Si and B₄Si₂ (with Si at 1, 3 positions) six-membered rings. Metastable B₆Si-II has a similar structure as B₄Si-I, which contains B₆Si seven-membered rings and B₄Si five-membered rings. The structure of B₆Si-III can be viewed as zigzag prismatic B₄ chains connected by Si atoms with large B₆Si₂ holes. B₆Si-II and B₆Si-III have a higher energy of 34 meV/atom and 39.4 meV/atom, respectively, than B₆Si-I. The structure of B₇Si is closely related to that of B₅Si. If one inserts 1D zigzag boron chains into the interfacial regions between the building units of B₅Si, B₅Si-I and B₅Si-II would turn into B₇Si-II and B₇Si-I, respectively.

In summary, 2D boron–silicon sheets present versatile morphologies depending on the Si–B stoichiometry. (1) For Si-rich and B–Si compounds, a general structural feature of 2D sheets is a graphene-like honeycomb with various arrangements of boron and silicon atoms. B–B and Si–Si bonding are energetically favored. (2) For B-rich compounds, boron atoms prefer to form ribbon structures due to the tendency of multibonding characteristic of boron while silicon atoms prefer to form single-atomic chain by itself (single-Si-atomic chain) or with boron (BSi atomic chain). (3) Silicon can form planar-tetracoordinated bonding structure with boron or other silicon atoms. Especially, ptSi surrounded by four silicon atoms is predicted to be stable in the metastable BSi₄-III sheet and B₅Si-II sheet, as well as B₇Si-I sheet. (4) Except for BSi₂, B₄Si, and B₇Si, silicon atoms in the lowest-energy B–Si sheets favor sp² hybridization.

Structural Stability. To confirm the structural stability of predicted 2D boron silicon sheets, we perform lattice dynamics calculations (phonon-spectrum calculations at 0 K) using the linear response theory.⁴⁷ Note that at low temperature, all vibrational motions in the crystal can be decomposed into nearly independent phonon modes (i.e., normal modes). Therefore, at low temperature, phonon instability is both necessary and sufficient conditions for mechanical instability of a crystal. No imaginary phonon frequencies are observed in the Brillouin zone for all 2D B–Si compounds (see Figure 2 for representative phonon band structures), indicating the inherent dynamical stability of these B–Si sheets. The highest zone-center phonon frequencies are 792 cm^{−1}, 1036 cm^{−1}, and 1234 cm^{−1} for BSi₂-I, BSi-I, and B₂Si-I, respectively. The lower frequency for BSi₂-I than that of BSi-I and B₂Si-I is due to the difference in bonding type. For BSi-I and B₂Si-I, the phonon mode with the highest frequency is the B–B stretching mode, while for BSi₂-I, it is a B–Si stretching mode. The B–B mode possesses higher frequency due to lighter atomic mass of boron and shorter bond length. The difference in zone-center phonon modes for different 2D B–Si compounds can be used to identify the structures of the compound once synthesized. For example, the highest zone-center phonon mode of BSi-I and B₂Si-I are Raman active modes, while the one for BSi₂ is both Raman and IR active. Hence, some of these phonon modes can be used as a fingerprint in the spectrum to determine structures of 2D B–Si compounds.

To evaluate relative stabilities among the predicted 2D B–Si compounds, we compute their cohesive energies (E_{coh}). Computed values of E_{coh} with respect to boron composition are presented in Figure 3 (see Supporting Information Table S1 for the average cohesive energies of all low-energy boron–

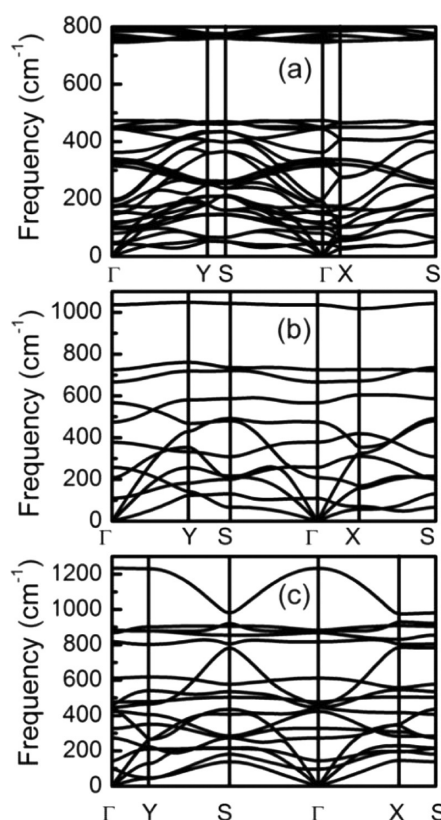


Figure 2. Phonon band structures of (a) BSi₂-I, (b) BSi-I, and (c) B₂Si-I. $\Gamma(0.0, 0.0, 0.0)$, Y(0, 0.5, 0.0), S(0.5, 0.5, 0), and X(0.5, 0.0, 0.0) refer to special points in the first Brillouin zone.

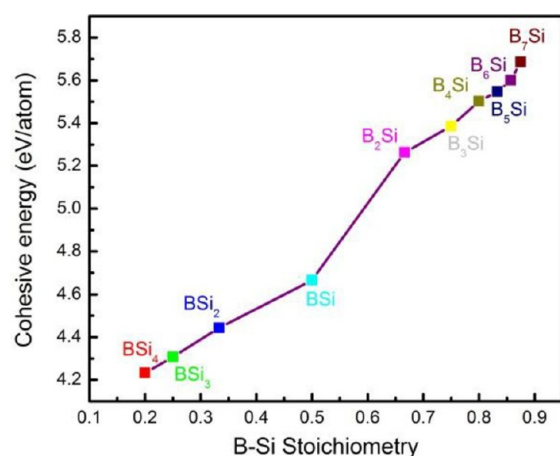


Figure 3. Cohesive energies of the lowest-energy 2D B–Si compounds with respect to B_xSi_y stoichiometry $x/(x+y)$.

silicon sheets). It can be seen that E_{coh} values increase with increasing boron composition. B₇Si has the highest E_{coh} value, suggesting higher structural stability, compared to other B–Si sheets.

Electronic Properties. Electronic band structure calculations suggest that all the 2D B–Si compounds predicted are metallic, as are most 2D boron sheets^{16,20,21} and 2D B–C compounds.^{33,34} The metallicity stems from the delocalized p_z π electrons of boron and silicon. To gain more insight into the electronic structures, the partial density of states (PDOS) of the 2D B–Si compounds are also analyzed. Representative PDOSs for BSi₂-I, BSi-I, and B₂Si-I are shown in Figure 4. The s and p

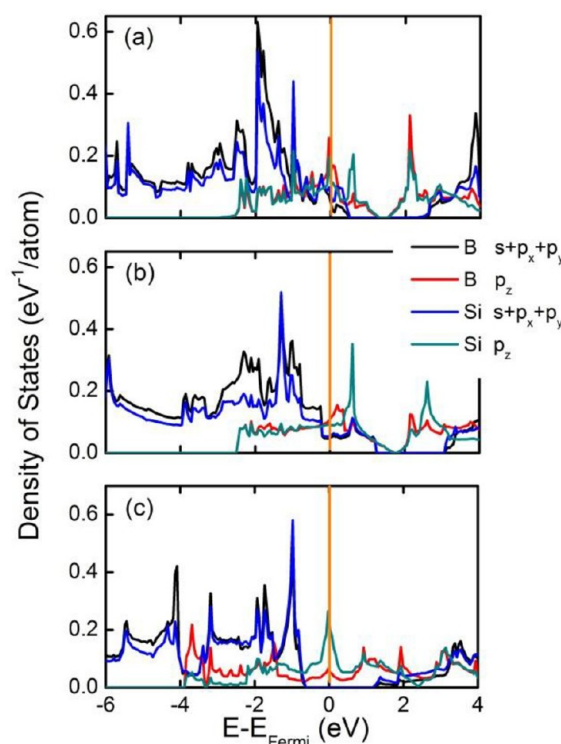


Figure 4. PDOS for (a) BSi₂-I, (b) BSi-I, and (c) B₂Si-I. The vertical orange lines denote the Fermi level.

orbitals are separated into in-plane σ states (the sum of s , p_x , and p_y) and out-of-plane π states (p_z). The mixing between σ and π states is prohibited by the symmetry since, in 2D systems, s , p_x , and p_y orbitals are symmetric with respect to the mirror plane, while p_z is antisymmetric. Clearly, the p_z states in Figure 4 are partially occupied. Another feature in Figure 4 is that the bonding σ states and antibonding σ^* states are well separated. As an example, in BSi₂-I (Figure 4a), the hybrid B–Si bonding σ states end at 0.5 eV (black & blue lines) above the Fermi level, which means the bonding σ states are hole doped, while the antibonding σ^* states start at 2.1 eV (black & blue lines). Similar to BSi₂-I, the hybrid B–Si σ states that end at 1.3 eV above the Fermi level are also hole doped, while the antibonding σ^* states start at 3.1 eV. Interestingly, in B₂Si-I, the bonding σ states are fully occupied, and the antibonding σ^* states are empty. Such a hallmark that the Fermi level lies in the gap of in-plane PDOS has been used previously to explain the stability of the lowest-energy boron sheets since the in-plane bonds formed from overlapping of sp^2 hybrids are stronger than the out-of-plane π bonds.^{16,20,21} Here, except for B₂Si-I, we find that the lowest-energy structures of BSi₄ and B₃Si (see Figures S9 and S10) also entail this hallmark electronic feature, i.e., having optimal occupation of in-plane σ states.

To understand the bonding nature of the predicted 2D B–Si compounds, we also perform electron localization function (ELF) analysis.^{48,49} We plot iso-surfaces of ELF for the lowest-energy 2D B–Si compounds with a relatively large iso-value of 0.75 in Figure 5 to highlight the in-plane σ states. For silicon-rich compounds (BSi₄-I, BSi₃-I, and BSi₂-I) and BSi-I, all B and Si atoms are 3-fold coordinated, and the ELF localizes at the bond center of B–Si, Si–Si, and B–B bonds (see Figure 5a–d), similar to the ELF pattern in graphene. For B₂Si-I, we can see clearly one Si–Si σ bond, one B–B two-center σ bond, four B–Si σ bonds, and two three-center B bonds per unit cell. Similar

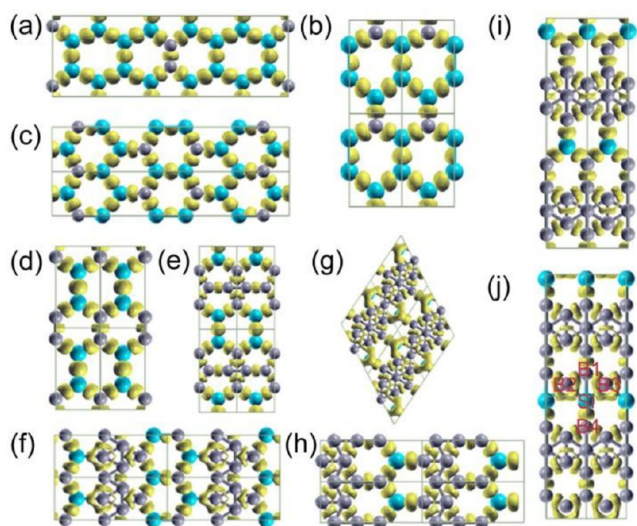


Figure 5. Iso-surfaces of ELF with the value of 0.75 for (a) BSi₄-I, (b) BSi₃-I, (c) BSi₂-I, (d) BSi-I, (e) B₂Si-I, (f) B₃Si-I, (g) B₄Si-I, (h) B₅Si-I, (i) B₆Si-I, and (j) B₇Si-I.

to B₂Si-I, one can see that ELF distributes around the center of boron triangles for boron-rich B₃Si-I, B₅Si-I and B₆Si-I, indicating the existence of boron three center bonds. For B₇Si-I, the ELF around ptSi is mainly distributed over silicon and B₂, B₃, and B₄ (Figure S5j and Figure S12), while the bonding between Si and B₁ appears to be very weak (see ELF and computed deformation electron density in Figure S12c), suggesting a partial fourth bond. Interestingly, although the structures of BSi₂-I and B₄Si-I are buckled, the ELF around silicon atoms shows different characteristics: In BSi₂-I, the ELF localizes at the center of B–Si and Si–Si bonds, while in B₄Si-I, the ELF around the silicon shows a pyramid-like structure, indicating sp³-like bonding. The sp³-like bonding of silicon in B₄Si-I is also proven in PDOS of B₄Si-I (see Figure S11), in which the peaks of silicon p_z states and in-plane states clearly show some overlap around –1 and 1.8 eV.

In conclusion, we have performed a global search of monolayer structures of B–Si compounds based on the PSO algorithm combined with first-principles calculations. The most stable structures of 2D B–Si compounds are predicted for a wide range of B–Si stoichiometries, many for the first time. Stabilities of these predicted structures are verified via lattice dynamics calculations as well as electronic structure calculations. Our calculations suggest that (1) all 2D B–Si compounds are metallic; (2) the structures of silicon-rich 2D B–Si compounds and BSi are likely to exhibit a graphene-like honeycomb structure, while in boron-rich 2D B–Si compounds, boron atoms tend to form triangles as in 2D boron sheets; (3) except for BSi₂, B₄Si, and B₇Si, silicon atoms in 2D B–Si compounds favor sp² hybridization. To our knowledge, such a preference to sp² bonded silicon in low-dimensional condensed matter has not been previously reported in the literature. If confirmed, this prediction will enrich the family of silicon chemical structures, in light of the fact that silicon tends to form multiple bonds and hyper-coordinated bonds.

■ COMPUTATIONAL METHODS

PSO Calculations. The PSO algorithm within the evolutionary scheme as implemented in the CALYPSO (Crystal structure AnaLYsis by Particle Swarm Optimization) code⁴⁵ is employed

to search for low-energy structures of 2D boron–silicon compounds. As an unbiased global optimization method, the PSO algorithm was inspired by the choreography of a bird flock and can be viewed as a distributed-behavior algorithm that performs multidimensional search.⁵⁰ We selected the PSO algorithm because it is very fast and efficient compared to other methods, and it requires few parameters to adjust.⁵¹ The PSO algorithm, coupled with DFT optimization, has been utilized in predicting low-energy structures of 2D boron-carbide compounds,³⁴ 2D boron sheets,²¹ as well as 3D structures of elements and compounds.^{52–54} In the PSO structural search, the population size is set to be 30, and the number of generation is maintained at 30. All possible supercell sizes are considered with the total number of atoms no more than 20 in the supercell. As an example, for BSi, supercells with up to 10 unit-cells are considered. In the first generation, random structures are constructed by generating atomic coordinates using crystallographic symmetry operations. Next, the structures are optimized using a DFT method (below). Third, the best 60% structures are selected by PSO to generate the next generation, and other structures in the new generation are generated randomly, which guarantee the structural diversity.

DFT Calculations. DFT within PBE-type general gradient approximation (GGA) as implemented in VASP 5.2^{55,56} is used to relax the structures and compute the cohesive energies. The ion-electron interaction is treated using the projector augment wave (PAW) technique. For geometric optimization, both lattice constants and atomic positions are relaxed until the forces on atoms are less than 0.02 eV/Å and the total energy change is less than 1.0×10^{-5} eV. The vacuum distance is set to about 20 Å to neglect the interlayer interaction. The Brillouin zone is sampled using *k*-points with 0.02 Å^{–1} spacing in the Monkhorst–Pack scheme.⁵⁷ For the cohesive energy calculation, we used the formula $E_{\text{coh}} = (xE_{\text{B}} + yE_{\text{Si}} - E_{\text{B}_x\text{Si}_y})/(x + y)$, where E_{B} , E_{Si} , and $E_{\text{B}_x\text{Si}_y}$ are total energies of a single B-atom, a single Si-atom, and 2D B_xSi_y compound (per unit cell), respectively. Previous benchmarks on eight simple main-group solids show that PBE-type GGA underestimates the cohesive energies by –0.04 eV/atom on average, which is almost exact.⁵⁸ ELF analysis is used to understand the bonding nature of 2D B–Si compounds. Note that ELF is related to the total electron density and its gradient. The topological analysis of ELFs has been shown to be a rigorous approach to distinguishing different chemical bonds. ELF values range from 0 to 1 according to the definition, and for localized in-plane σ states, the ELF value should be close to 1, while for delocalized π state, the ELF value should be smaller than 0.5.

Phonon Spectrum Calculations. In the PSO structure search, each system is constrained to a plane. This constraint is removed during the geometrical optimization in DFT calculations. So it is still conceivable that the predicted structures are not a local minimum due to the removal of the constraint and prefer out-of-plane buckling. To ensure predicted structures are local minima, we carry out phonon spectrum calculations to examine the dynamical stability of all predicted low-energy structures. The phonon spectra are computed based a DFT perturbation method with the linear response as implemented in the QUANTUM ESPRESSO package.⁴⁷ We collect the structures without imaginary phonon modes, and for the structures having imaginary modes at the Γ point, we distort positions of the atoms along the vibration

eigenvectors of the zone center soft phonon mode to achieve a new stable structure.

■ ASSOCIATED CONTENT

■ Supporting Information

Table of calculated cohesive energies, low-energy structures of 2D B–Si compounds, ELF for $\text{BSi}_2\text{-I}$ and $\text{B}_7\text{Si-I}$, and PDOS for $\text{BSi}_4\text{-I}$, $\text{B}_3\text{Si-I}$, and $\text{B}_4\text{Si-I}$ are collected. This material is available free of charge via the Internet at <http://pubs.acs.org>.

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Notes

The authors declare no competing financial interest.

■ ACKNOWLEDGMENTS

USTC group is supported by the National Basic Research Programs of China (Nos. 2011CB921400, 2012CB 922001), the NSFC (Grant Nos. 21121003, 11004180, 51172223), the One Hundred Person Project of CAS, the Shanghai Supercomputer Center, and the Hefei Supercomputer Center. The UNL group is supported by ARL (Grant No. W911NF1020099), NSF (Grant No. DMR-0820521), and a grant from USTC for (1000plan) Qianren-B summer research.

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